

research report

Experimental and Numerical Comparison of Flexural Capacity of Light Gage Cold Formed Steel Roof Deck

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Experimental and Numerical Comparison of Flexural Capacity of Light Gage Cold Formed Steel Roof Deck

A Report Submitted to
American Iron and Steel Institute
Steel Deck Institute
and National Roofing Contractors Association

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Abstract

This paper presents an analysis of experimental data and compares it to two numerical analysis methods of light gage cold formed steel roof deck. The flexural capacity was determined upon the first failure mode of the light gage cold formed steel roof deck. A comparison of the experimental data was made to both the effective width method and the direct strength method. The objective of the comparison was to have a physical test provide the actual behavior of the light gage cold formed steel roof deck and grade how well the numerical analysis, effective width and direct strength methods, compare against the results. Material testing samples were taken from the steel roof deck and evaluated for the actual yield stress. This allowed for the most accurate comparison between the experimental results with the numerical analysis since the exact yield strength was used in calculation. It was found that the effective width method and the direct strength method vary in their prediction of the nominal moment capacity across material grades and deck thickness but tend to converge to a constant ratio, M_{nDSM}/M_{nEWM} , at thicker deck gages. The effective width method was found to be more accurate for thinner gage steel roof deck, while the direct strength method was found to be more accurate for thicker gage steel roof deck. The effective width method is better at predicting the strength of steel roof deck, particularly the thinner gage ones, while the direct strength method provided a much quicker process to find the flexural capacity of the deck. Both methods can be used to determine the capacity of the deck and it is up to the end user to determine which method is appropriate for the given application.

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Nomenclature

Symbols

<i>Degrees</i>	=	measure of the angle between the flange and web
F_y	=	yield stress of material,ksi
<i>ksi</i>	=	kips per square inch
<i>kip-ft</i>	=	kip-feet
<i>kip-in.</i>	=	kip-inch
<i>lb</i>	=	pound
M_{crd}	=	critical elastic distortional buckling moment (kip-in.)
M_{cre}	=	critical elastic lateral-torsional buckling moment (kip-in.)
M_{crl}	=	critical elastic local buckling moment (kip-in.)
M_n	=	nominal flexural strength (kip-in.)
M_{nd}	=	nominal flexural strength for distortional buckling (kip-in.)
M_{ne}	=	nominal flexural strength for lateral-torsional buckling (kip-in.)
M_{nl}	=	nominal flexural strength for local buckling (kip-in.)
M_y	=	yield moment ($S_g F_y$) (kip-in.)
M_{NDSM}	=	nominal flexural strength using Direct Strength Method (kip-in.)
M_{EWM}	=	nominal flexural strength using Effective Width Method (kip-in.)
<i>Radians</i>	=	measure of the angle between the flange and web
S_g	=	elastic section modulus of gross section (kip-in.)

Abbreviations

AISI	=	American Iron and Steel Institute
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CSEC	=	Construction Science and Engineering Center
CUFSM	=	Cornell University Finite Strip Method
DL	=	Dead Load
DSM	=	Direct Strength Method
EWM	=	Effective Width Method
HSS	=	Hollow Structural Section
LVDT	=	Linear Variable Differential Transformer
MSOE	=	Milwaukee School of Engineering
MTS	=	MTS Systems Corporation

Glossary

Linear Variable Differential Transformer (LVDT) – a type of electrical transformer used for measuring linear displacement.

MTS System (MTS) – a data collection system that applies a specified load using hydraulic rams and collects force and displacement readings.

Chapter 1.

Introduction, Literature Review and Numerical Analysis Methods

1.0 Introduction

1.0.1 Project Origin

This project stemmed from a proposal for testing steel roof deck for membrane fastener pullout. Mechanically attached roofing membranes load the steel roof deck in uplift in a more severe manner than uniformly adhered membranes. Quantifying the additional usable strength of the deck will improve the overall competitiveness of steel deck roofs. The project evolved into a larger project where the flexural capacity of the roof deck would be evaluated and compared to numerical results. A prior study conducted at the University of Florida [1] on the application of the Direct Strength Method (DSM) and Effective Width Method (EWM) to metal roof deck showed differing results, and more investigation was necessary to identify the source of discrepancy and the accuracy of the numerical models as compared to in-situ testing.

1.0.2 Description of the Project

The current research initiative intends to close the loop by testing the flexural strength of thin gage, cold formed steel deck roof panels and comparing the results from the experimental study to the capacities predicted by both DSM and EWM results. The current study will set the stage for additional steel deck flexural studies, particularly those related to floor deck panels with different profiles than those used for roof deck.

1.0.3 Justification of the Project

Studies conducted at the University of Florida [1] uncovered discrepancies between numerical results found using the DSM and EWM when evaluating roof deck in flexure. Future studies were recommended as a conclusion of that project. The current research initiative follows that recommendation and adds to the body of knowledge of the flexural capacity of light gage roof deck. The author hopes that the results of this study will impact current provisions in the American Iron and Steel Institute (AISI) S100 Standard.

1.1 Literature Review

There have been many studies [1, 2, 3, 4, 5] conducted on the behavior of cold formed steel shapes in recent years and many new developments have been made to more quickly and accurately numerically determine the capacity of these different shapes.

The cross-sections typically used in cold-formed steel member design are thin, light and efficient [4]. These shapes allow for economy in construction, being able to provide a substantial strength-to-weight ratio and ease of manufacturing. The design cost that often comes with these shapes is that their thin elements buckle in more complex fashions than heavier, hot-rolled shapes [4]. There are a few key buckling modes that cold-formed steel cross-sections exhibit, including local buckling, distortional buckling and lateral-torsional buckling. Local buckling is where an individual plate element within the shape's cross-section buckles when a compressive stress is applied to the cross-section. Distortional buckling is when a local rotation is observed in one or more of the plate elements within the cross-section. Lateral torsional buckling occurs when the entire

cross-section is affected and a global rotation occurs, often with no other local deformations on the cross-sectional shape [5].

These complex failure modes happen at different half wavelengths. The half wavelengths are the length of the buckled area along the length of the member. The buckle length is half of a typical sine wave, which is where the name is derived. For local buckling this length is often short in length, as the name implies. The length of these half wavelengths increases as one goes from local buckling to distortional buckling and finally to lateral torsional buckling [4].

Attempting to determine the flexural capacity of these shapes and being able to evaluate all failure modes can be mathematically complex. The unique challenge with cold-formed steel is that the entire cross-section will not be able to contribute equally to the strength. The different plate elements that make up the cross-section may become ineffective at, for example, the middle of a wider section or at the end of an unstiffened edge. This leads to a more exhaustive analysis of cross-sections prone to local failures. Fortunately, through the aid of recent software advances, one can efficiently determine a cross-section's capacity.

One such software is the Cornell University Finite Strip Method (CUFSM) [4]. The finite strip method divides the cross-section into small strips like that of a finite element analysis. Figure 1 shows an illustrated view of how a typical cross-section is divided into strips, the degrees of freedom that each of the strips are allowed to have and how a “traction edge vector” applies. This illustration is from a conventional finite strip method example; however, the CUFSM is based on this method and adds the feature of decomposing the different buckling modes allowing for a more detailed solution.

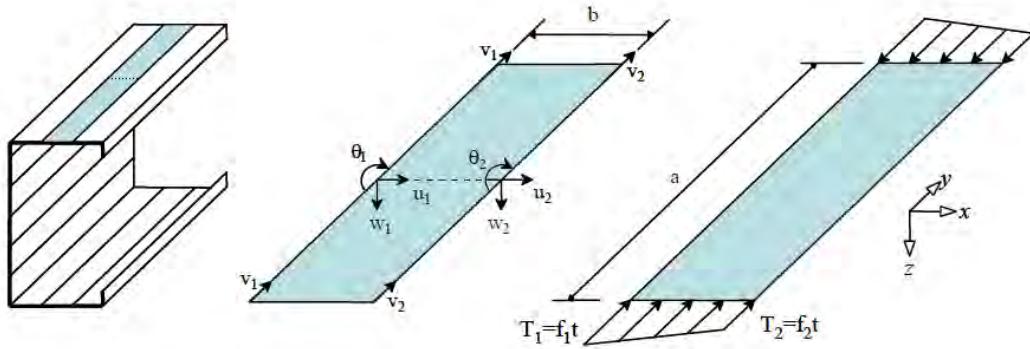


Figure 1: Finite Strip Method Example [4].

The finite strip method is similar to a finite element analysis with fewer degrees of freedom. A finite element analysis model is difficult to do for a cold-formed steel cross-section such as steel deck. Typical difficulties arise, such as selection of an appropriate element type to represent the steel deck. Using a finite strip effectively solves issues such as these and reduces the size of the model.

1.1.1 General CUFSM Analysis Procedure

The software package utilized in the current research is, coincidentally, also called CUFSM [2]. This software employs the direct strength method of analysis which uses cross-section elastic buckling solutions as the primary input to the strength prediction. This software is utilized to develop a numerical solution of steel deck's flexural capacity. The title screen for the software is shown in Figure 2 (in order to show the version and reference for the program).

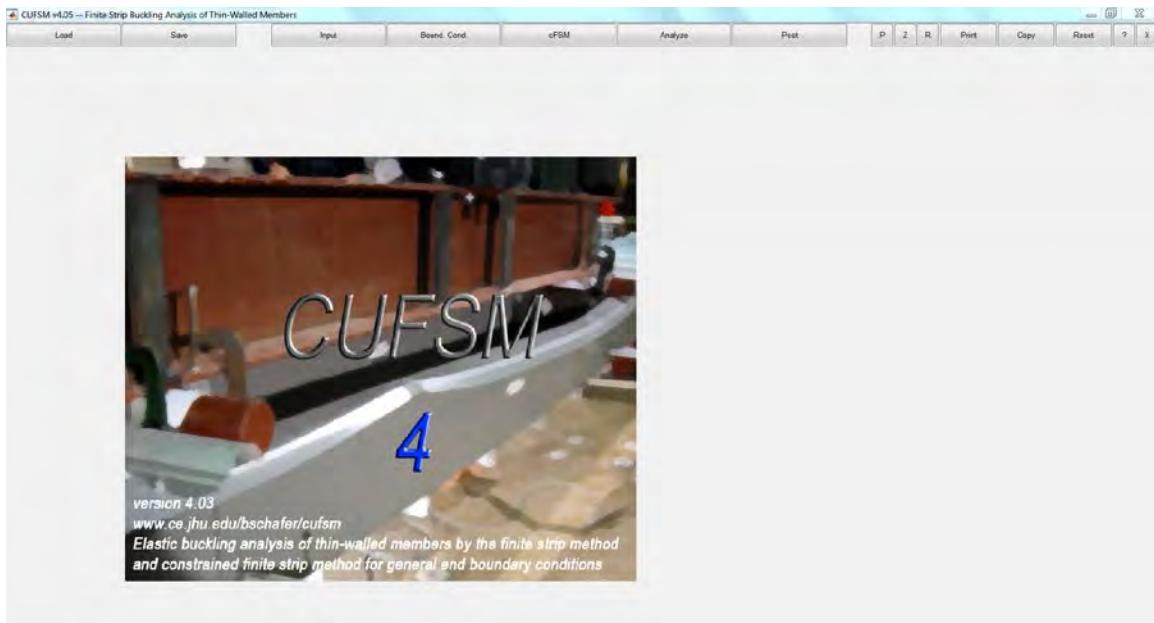


Figure 2: CUFSM Main Menu.

The user inputs a geometry using nodes, elements and material types into the user interface. Figure 3 shows the general input menu (i.e., preprocessor) of the CUFSM software.

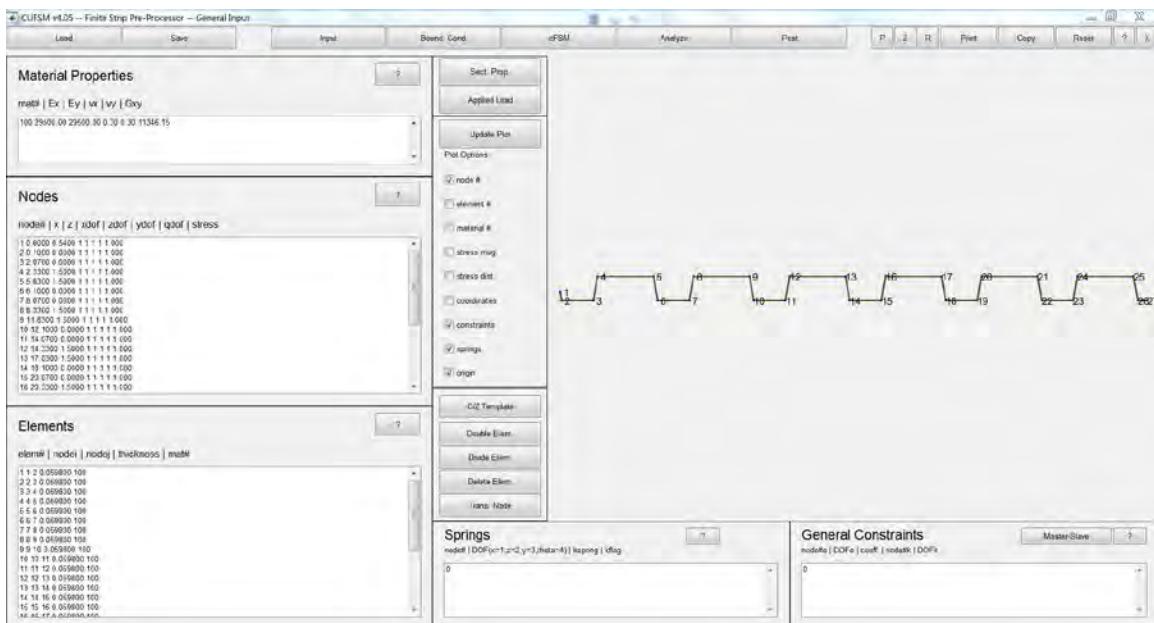


Figure 3: Cross-Section Definition (Input).

The user can then define a loading on the cross-section in the form of a stress distribution. This covers the possibilities of using shapes as tension, compression or flexural members. The software allows a yield stress to be input and a maximum moment that would cause initial yield. Figure 4 illustrates the sub-menu in the input section.

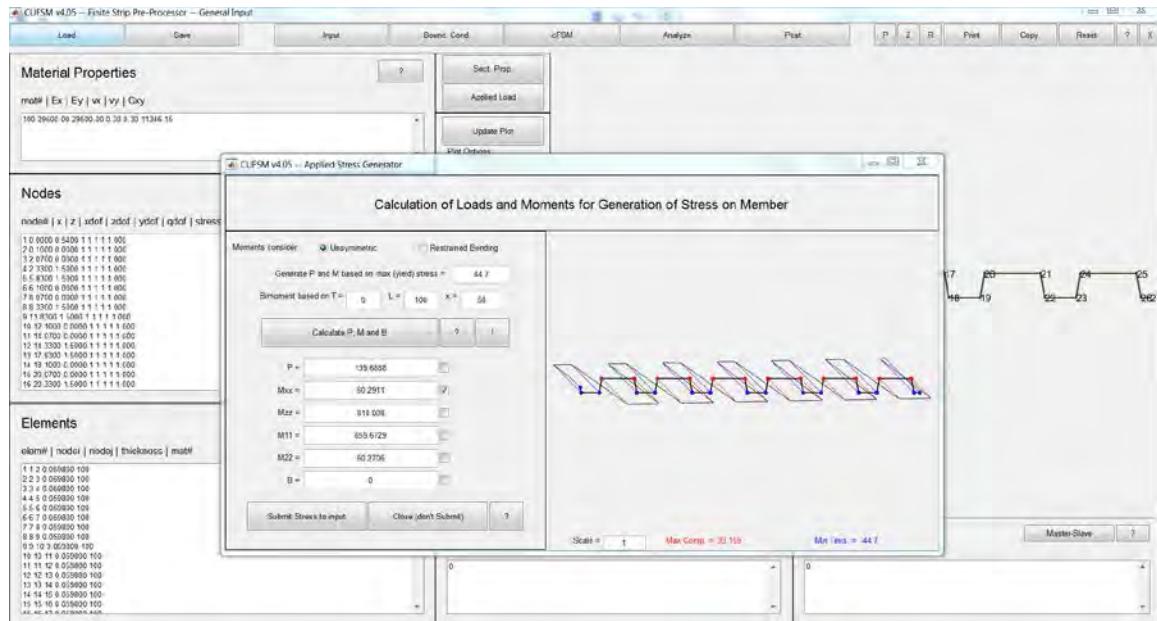


Figure 4: Stress Distribution Input.

The next step is to input the half wavelength that the software will use to determine when the failure mode will occur. For the current research, a preprocessor was utilized that generates half wavelengths for the user to input into CUFSM [1]. Figure 5 illustrates the input of these values. The number and difference between values is important here as the more values input, the greater the accuracy of the final answer as the software can analyze buckling over more lengths.

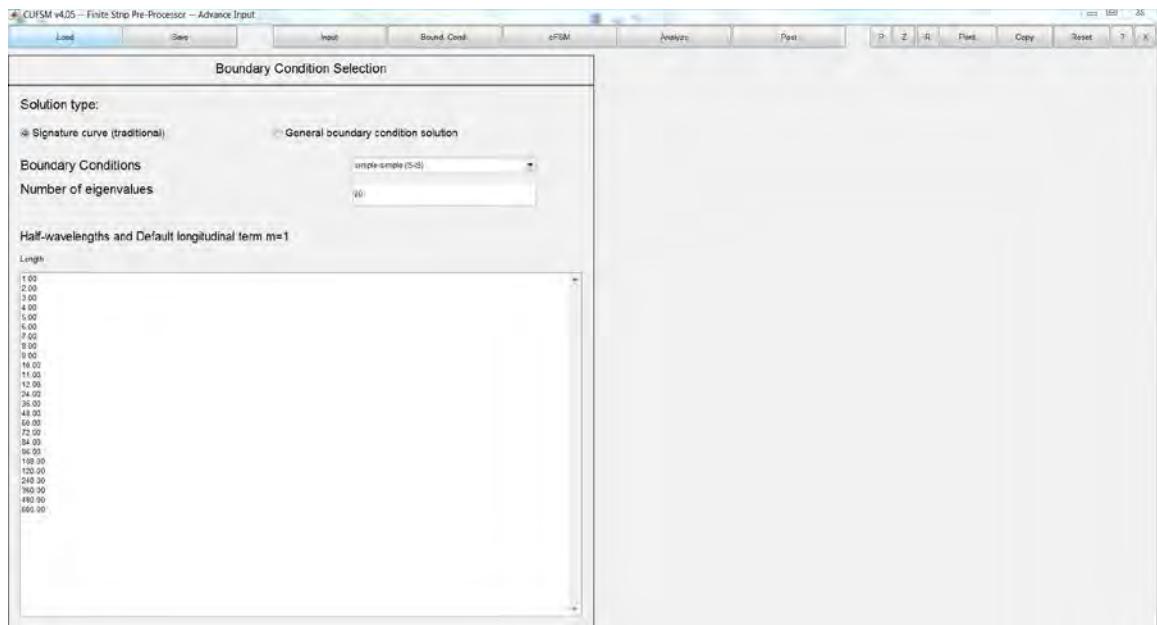


Figure 5: Half Wavelength Input.

The final step before analyzing the shape is to turn on the base vectors so all the different failure modes (local, distortional, global) can be classified in post processing if so desired. The base vectors are the normalized version of each buckling type (global, distortional, local and other) [2]. This is done so that the results can be compared correctly in the signature curve. The software can automatically determine these vectors based on the geometry input and the density of the mesh. Figure 6 shows how the base vectors are input to the program.

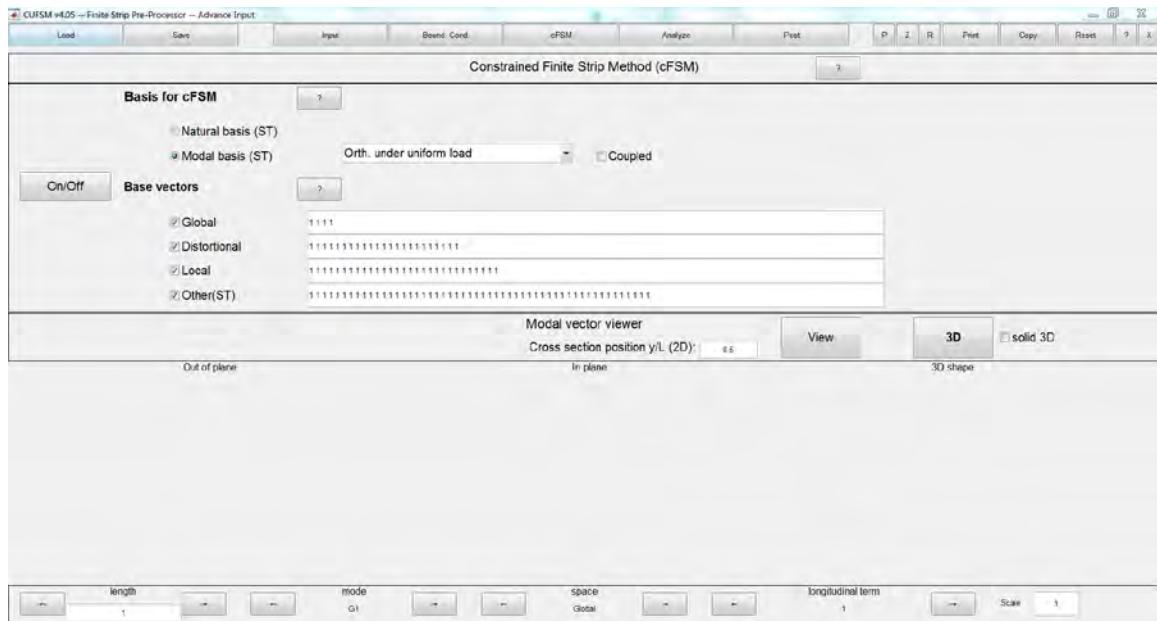


Figure 6: Base Vector Input.

Once the user has completed all of these steps, the model can be analyzed.

1.2 Effective Width Method

The Effective Width Method can be used to analyze a cold formed steel shape.

The concept behind the effective width method is that not all of the cross-section is effective and contributing equally, or even significantly, to the flexural capacity [1]. For example, the top of the flute in a cross-section of a steel roof deck that is not stiffened is so thin and flexible that it does not completely contribute to the flexural strength when a compressive stress is applied to it. The areas that are more effective are typically around the corners and bends of a shape as the corner is much stiffer than the midspan of the flute. Figures 7 and 8 illustrate how the stress is theoretically distributed across the cross-section.



Figure 7: Effective Compression Flange [1].

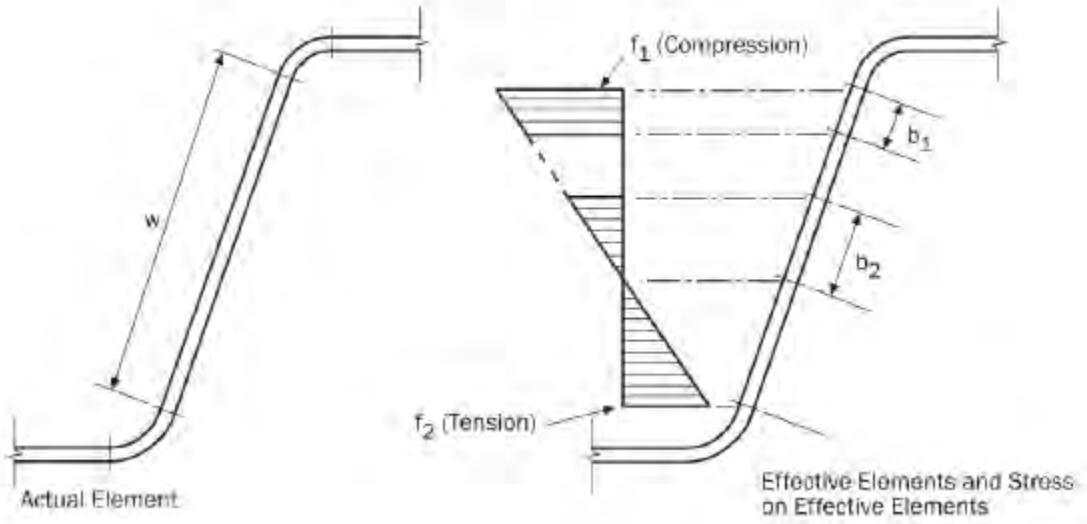


Figure 8: Effective Web Sections [3].

Figures 7 shows the effective width of the compression flange and how the stresses are concentrated around the corners. A similar approach is applied to the web as shown in Figure 8, where only a portion of the web is considered effective. The stress is a linear distribution along the entire depth of the section where either the extreme tension or compression fiber are at first yield. The portion of the web that is in compression has two areas that can be considered as effective. The first area is right next to the bend that leads to the compression flange. The other area is just above the neutral axis of the stress distribution. Finally, the portion of the cross-section that is in tension is fully effective

since there is no buckling in this region because the entire section below the neutral axis is in tension. Since the lengths of the effective width in the web portion of the shape are based on the location of the neutral axis, the location of the neutral axis is assumed and then verified by comparing the total tension and compression force couple. This is an iterative process of assuming a location for the neutral axis, solving for the effective widths and subsequent areas from the assumed neutral axis and comparing the resultant tension force with the compression force. Once the forces balance, it is assumed that the correct neutral axis location has been determined and the resulting flexural capacity can be accurately calculated.

1.3 Direct Strength Method

Once the CUFSM software analyzed the cross-section a signature curve was produced. A signature curve is a graph that lists points of interest where a particular failure mode exists. The horizontal coordinate is the half wavelength at which the failure occurs and the vertical coordinate is a load factor that is used in equations that evaluate the different buckling and yield failure modes [1, 6]. Figure 9 illustrates an example of a signature curve for typical 16 gage steel roof deck.

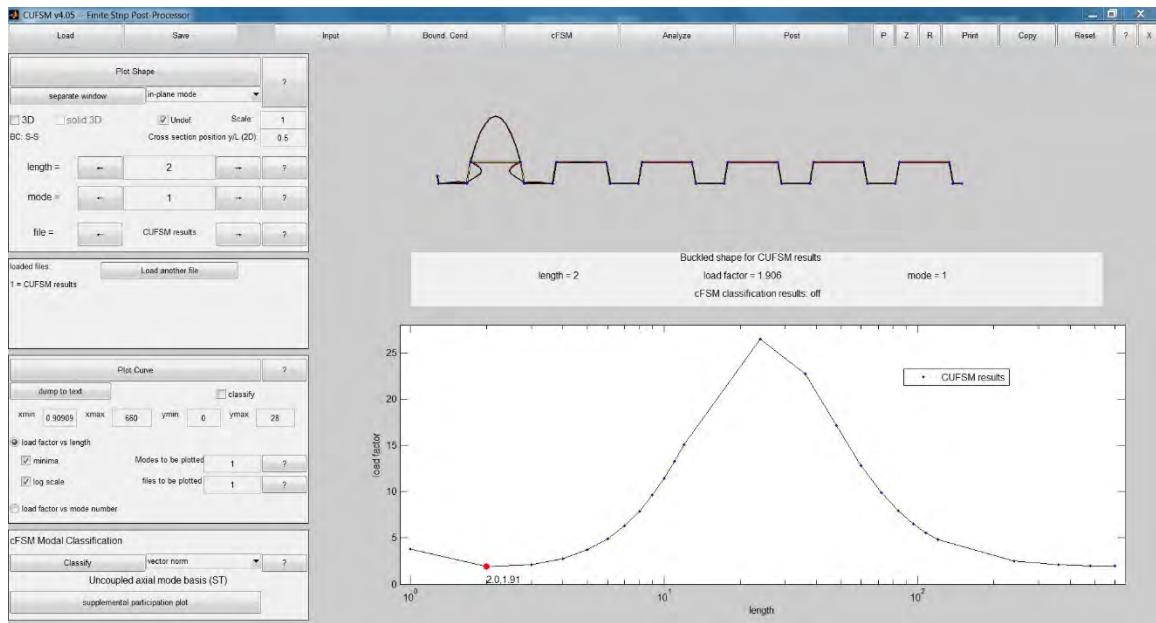


Figure 9: Example of a Signature Curve for 16 Gage Deck Signature Curve.

The results from the finite strip analysis are used to determine a flexural capacity based on lateral torsional buckling, local buckling, yielding and distortional buckling.

For the limit state of yielding,

$$M_y = F_y S_{\pm} \quad (1)$$

where

F_y = yield strength from material testing [ksi],

S_{\pm} = positive or negative elastic section modulus [in^3].

The next step is to extract the values from the signature curve and use them in their respective capacity calculations. The third minima value from the signature curve is typically used in the calculation of lateral torsional buckling; however, since lateral-torsional buckling not a realistic failure mode due to the wide, flat shape of the deck, the highest value from the signature curve can also be taken. The load factor is input to the equation for critical elastic moment:

$$M_{cre} = \text{Load Factor}_{LTB} \times M_y. \quad (2)$$

Next, some comparisons are made to apply the correct formula to calculate the actual flexural capacity with respect to lateral torsional buckling:

For $M_{cre} < 0.56 \times M_y$,

$$M_{ne} = M_{cre}. \quad (3)$$

For $2.78 \times M_y \geq M_{cre} \geq 0.56 \times M_y$,

$$M_{ne} = \frac{10}{9} \times M_y \times \left(1 - \frac{10 \times M_y}{36 \times M_{cre}}\right). \quad (4)$$

For $M_{cre} > 2.78 \times M_y$,

$$M_{ne} = M_y. \quad (5)$$

The next capacity calculation is for local buckling. The local buckling load factor is the first minima value from the signature curve. Therefore:

$$M_{crl} = \text{Load Factor}_{LOCAL} \times M_y. \quad (6)$$

Next, determine which equation is used to determine the local buckling strength:

For $\lambda_l \leq 0.776$,

$$M_{nl} = M_e. \quad (7)$$

For $\lambda_l > 0.776$,

$$M_{nl} = \left(1 - 0.15 \times \left(\frac{M_{crl}}{M_{ne}}\right)^{0.4}\right) \times \left(\frac{M_{crl}}{M_{ne}}\right)^{0.4} \times M_{ne}, \quad (8)$$

$$\text{where } \lambda_l = \sqrt{\frac{M_{ne}}{M_{crl}}}. \quad (9)$$

Finally, the distortional buckling strength is calculated. Its load factor is typically the second minima on the signature curve. Similar to lateral torsional buckling, this is

also typically an unrealistic failure mode for steel roof deck so the highest value on the signature curve can be taken as the load factor. Thus,

$$M_{crd} = \text{Load Factor}_{DIST} \times M_y.$$

And

For $\lambda_d \leq 0.673$,

$$M_{nd} = M_y. \quad (11)$$

For $\lambda_d > 0.673$,

$$M_{nd} = \left(1 - 0.22 \times \left(\frac{M_{crd}}{M_y} \right)^{0.5} \right) \times \left(\frac{M_{crd}}{M_y} \right)^{0.5} \times M_y, \quad (12)$$

$$\text{where } \lambda_d = \sqrt{\frac{M_y}{M_{crd}}}. \quad (13)$$

The flexural capacity is the minimum of M_{nd} , M_{ne} and M_{nl} .

Now, the results from the finite strip analysis shown in Figure 9 are used to determine a flexural capacity based on lateral torsional buckling, local buckling, yielding and distortional buckling. For the limit state of yielding,

$$M_y = F_y S_{\pm}. \quad (1)$$

This example will use a yield stress of 44.7 ksi. This yield stress magnitude was determined through material testing. Details related to the material testing results will be discussed later in this report.

The positive or negative elastic section modulus are taken from the CANAM steel roof deck catalog [7] for the steel roof deck used in the experimental program. For this example, a value of 1.23 in.³ is used. Therefore, the yield moment would equal:

$$M_y = (44.7 \text{ ksi})(1.23 \text{ in.}^3), \quad (1)$$

$$M_y = 54.98 \text{ kip-in.}$$

The third minima value from the signature curve is typically used in the calculation of lateral torsional buckling; however, since lateral-torsional buckling is not a realistic failure mode due to the wide, flat shape of the deck, the highest value from the signature curve is taken at 26.464. The load factor is input to the equation for critical elastic moment:

$$M_{cre} = \text{Load Factor}_{LTB} \times M_y, \quad (2)$$

$$M_{cre} = 26.464 \times 54.98 \text{ kip-in.}$$

$$M_{cre} = 1,455 \text{ kip-in.}$$

Next, some comparisons are made to apply the correct formula to calculate the actual flexural capacity with respect to lateral torsional buckling:

$$\text{For } M_{cre} < 0.56 \times M_y,$$

$$M_{ne} = M_{cre}. \quad (3)$$

$$\text{For } 2.78 \times M_y \geq M_{cre} \geq 0.56 \times M_y,$$

$$M_{ne} = \frac{10}{9} \times M_y \times \left(1 - \frac{10 \times M_y}{36 \times M_{cre}}\right). \quad (4)$$

$$\text{For } M_{cre} > 2.78 \times M_y,$$

$$M_{ne} = M_y. \quad (5)$$

In this case, Equation (1) controls and the lateral torsional buckling capacity is the same as that for yielding. The local buckling load factor is the first minima value from the signature curve at 1.91. Therefore:

$$M_{crl} = \text{Load Factor}_{LOCAL} \times M_y, \quad (6)$$

$$M_{crl} = 1.91 \times 54.98 \text{ kip-in.}$$

$$M_{crl} = 105 \text{ kip-in.}$$

Next, determine which equation is used to determine the local buckling strength:

For $\lambda_l \leq 0.776$,

$$M_{nl} = M_{ne}. \quad (7)$$

For $\lambda_l > 0.776$,

$$M_{nl} = \left(1 - 0.15 \times \left(\frac{M_{crl}}{M_{ne}}\right)^{0.4}\right) \times \left(\frac{M_{crl}}{M_{ne}}\right)^{0.4} \times M_{ne}, \quad (8)$$

$$\text{where } \lambda_l = \sqrt{\frac{M_{ne}}{M_{crl}}} = \sqrt{\frac{54.98 \text{ kip-in.}}{105 \text{ kip-in.}}} = 0.723 < 0.776. \quad (9)$$

In this case, lambda (λ_l) is less than 0.776, so the local buckling strength is equal to the critical elastic buckling moment, M_{crl} .

The distortional buckling strength load factor is typically the second minima on the signature curve. Similar to lateral torsional buckling, this also would not control as a rotation in the cross-section would be needed. Therefore, the highest value of 26.464 on the signature curve was taken as the load factor:

$$M_{crd} = \text{Load Factor}_{DIST} \times M_y, \quad (10)$$

$$M_{crd} = 26.464 \times 54.98 \text{ kip-in.},$$

$$M_{crd} = 1,455 \text{ kip-in.}$$

For $\lambda_d \leq 0.673$,

$$M_{nd} = M_y. \quad (11)$$

For $\lambda_d > 0.673$,

$$M_{nd} = \left(1 - 0.22 \times \left(\frac{M_{crd}}{M_y}\right)^{0.5}\right) \times \left(\frac{M_{crd}}{M_y}\right)^{0.5} \times M_y, \quad (12)$$

$$\text{where } \lambda_d = \sqrt{\frac{M_y}{M_{crd}}} = \sqrt{\frac{54.98 \text{ kip-in.}}{1455 \text{ kip-in.}}} = 0.194 < 0.673. \quad (13)$$

In this case, λ_d was less than 0.673, so the distortional buckling strength is equal to the yield strength, M_y .

The flexural capacity is the minimum of M_{nd} , M_{ne} and M_{nl} . Since all the different checks for the different buckling modes resulted in the yield strength controlling the flexural capacity, the actual flexural capacity is:

$$M_n = 54.98 \text{ kip-in.}$$

1.4 Comparing DSM and EWM Results

A prior study by Dudenbostel [1] considered the flexural capacity of 1.5B deck using both the DSM and the EWM. Roof deck gages 16, 18, 20, 22 and 24 were included in the study. Table 1 shows a comparison between the nominal moment capacity using the DSM and EWM for 40 ksi steel roof deck. Both the positive and negative moment capacities are included in the table. Table 2 shows a similar comparison for 50 ksi roof deck.

Table 1: Nominal Moment Capacity - DSM and EWM Comparison ($F_y = 40$ ksi) [1].

Deck	Orientation	DSM M_n (kip-in.)	EWM M_n (kip-in.)
1.5WR22	Positive	16.86	20.29
1.5WR20	Positive	23.16	25.36
1.5WR18	Positive	36.45	34.69
1.5WR16	Positive	47.26	44.71
1.5WR22	Negative	23.52	22.21
1.5WR20	Negative	28.53	27.46
1.5WR18	Negative	37.62	36.22
1.5WR16	Negative	47.26	45.50

Table 2: Nominal Moment Capacity - DSM and EWM Comparison ($F_y = 50$ ksi) [1].

Deck	Orientation	DSM M_n (kip-in.)	EWM M_n (kip-in.)
1.5WR22	Positive	19.50	24.04
1.5WR20	Positive	26.86	31.20
1.5WR18	Positive	42.43	42.74
1.5WR16	Positive	59.08	55.22
1.5WR22	Negative	27.41	26.91
1.5WR20	Negative	35.66	34.32
1.5WR18	Negative	47.02	45.27
1.5WR16	Negative	59.08	56.88

The yield stresses that were used by Dudenbostel were 40 and 50 ksi, which are industry standards and commonly available [7]. The results of the DSM and EWM nominal moment capacity was then plotted as a ratio of the capacity to the thickness of the steel roof deck. Figures 10 and 11 illustrate the trends of how the two analysis methods compare to one another over various material thicknesses.

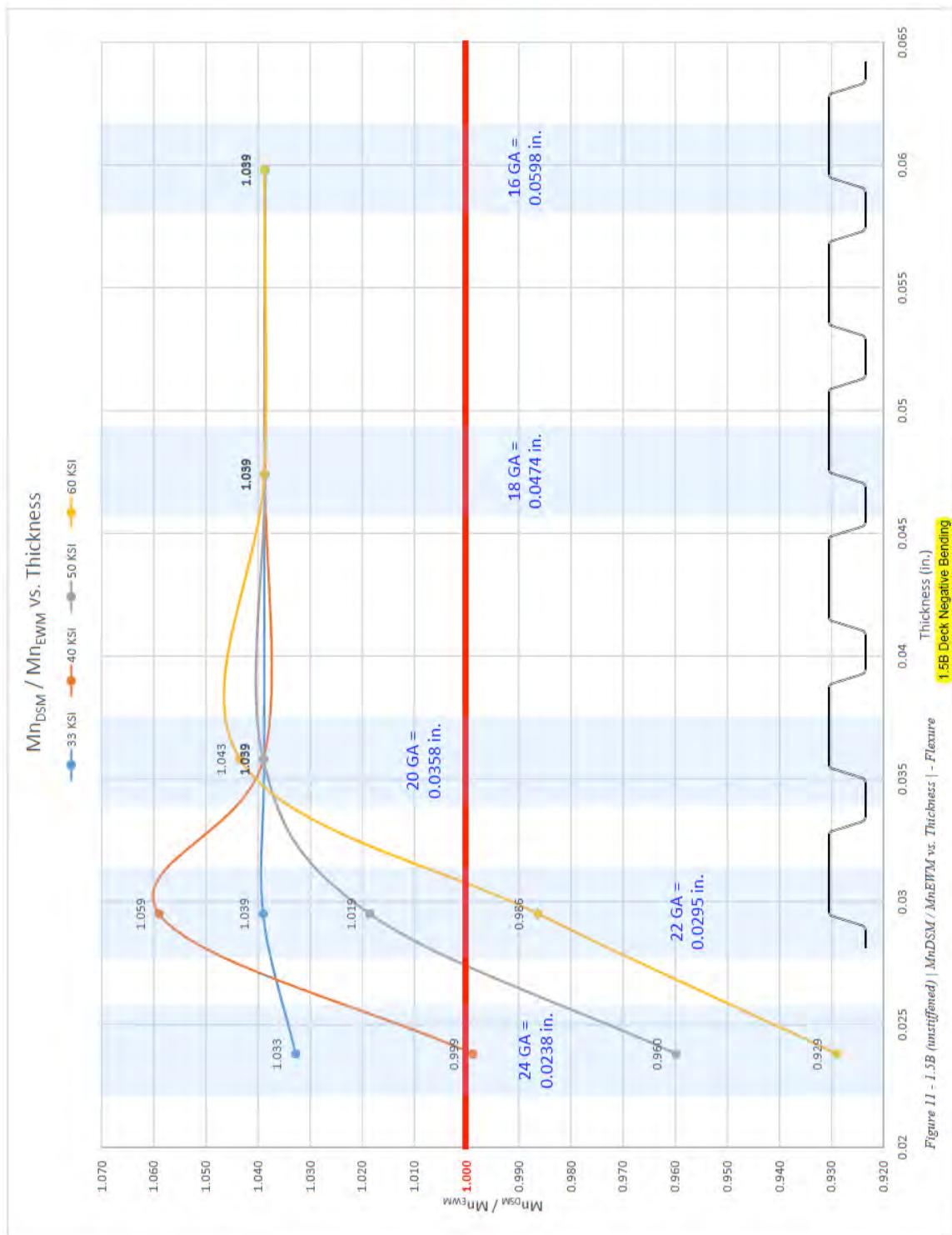


Figure 10: Mn_{DSM}/Mn_{EWIM} for Negative Bending [1].

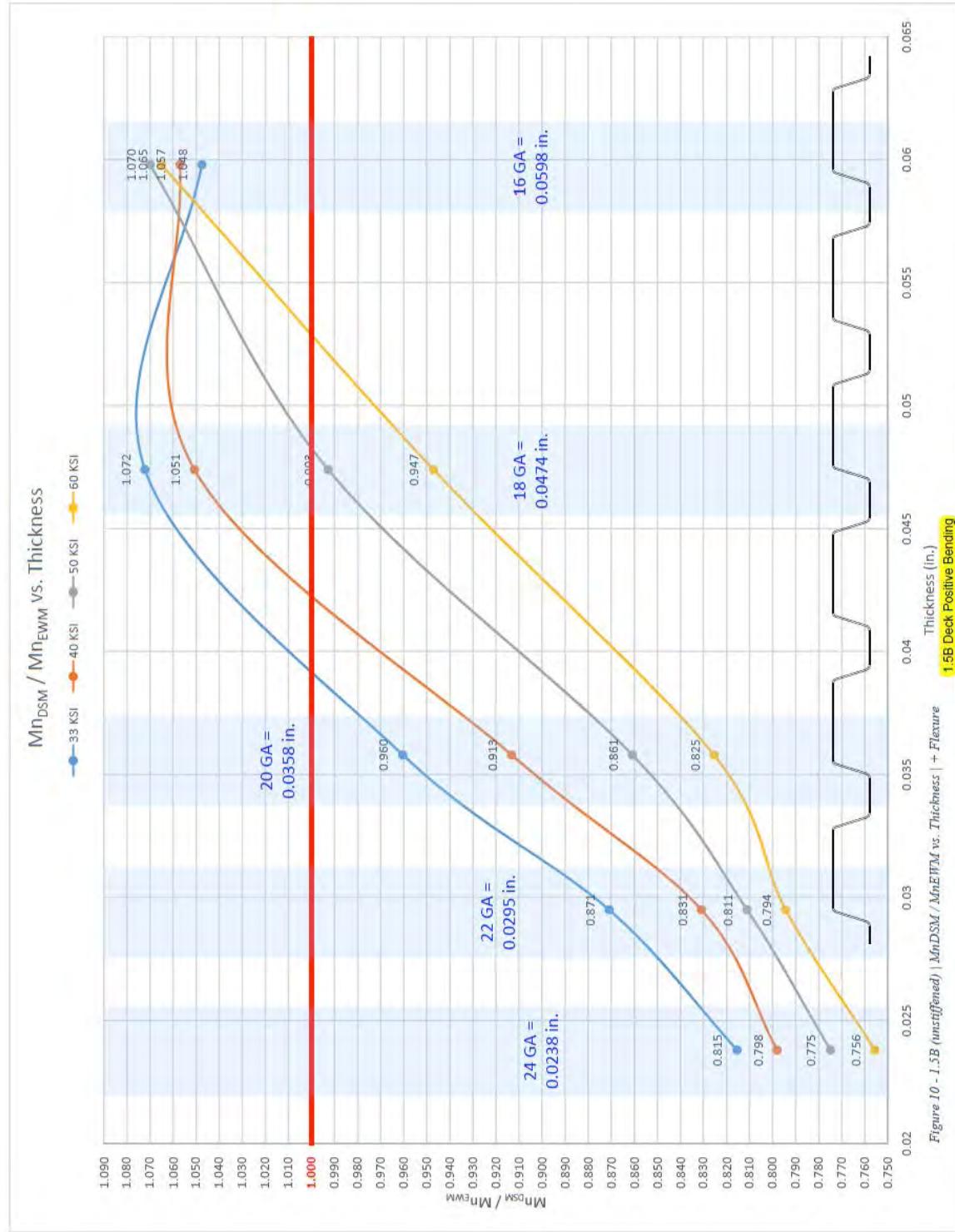


Figure 11: Mn_{DSM}/Mn_{EWM} for Positive Bending [1].

The general trend for negative bending is that the thinner gage decks have a varying M_{nDSM}/M_{nEWM} ratio from about 0.9 to 1.033 across the different yield stresses. As the deck becomes thicker, the yield stress makes less of an impact on the ratio. The ratio ends up converging on 1.039.

The general trend for positive bending shows that there is much more variation between different material strengths for the same steel deck thickness and ends up converging at the thicker gage deck. For 22 and 20 gage decks, the EWM reported a higher nominal moment strength than the DSM. Between the 20 gage and 18 gage thicknesses, the ratio switches and the DSM reports a higher nominal moment strength than the EWM. Note that for 18 gage, 50 ksi deck the nominal moment strengths for DSM and EWM are effectively equal (42.43 kip-in versus 42.74 kip-in.) All the different material strengths trend at the same rate and eventually approaches convergence at 16 gage thickness. At a ratio between 1.07 and 1.05 the DSM reports a higher value for the nominal moment strength than the EWM. With this variance between different yield strengths and material thickness, this study will be able to determine which analysis method more closely matches the experimentally measured moment capacity.

As previously discussed, the theoretical yield stress values were used in Dudenbostel's study. Past research by Ping [3] shows there can be a significant variance from the theoretical yield stress to the actual yield stress of the steel roof deck, anywhere from 26% higher to 66% higher than the nominal tensile strength. This is a very significant difference and needs to be incorporated in the numerical analyses.

For the experimental tests conducted as described in the next chapter, material samples were taken from the steel deck specimens. The measured yield stress from

material testing was used in calculations for accurate comparisons between analytical and numerical results.

Chapter 2: Experimental Program

2.0 Testing Setup

2.0.1 Test Frame and Apparatus

Testing was conducted in the Construction Science and Engineering Center (CSEC) at the Milwaukee School of Engineering (MSOE). An existing self-reacting test frame (Figure 12) was used. The test frame houses two MTS hydraulic actuators, of which one was used for the current project. The MTS actuator has the ability to measure force and displacement.



Figure 12: Existing Test Frame.

The test configuration is for a two-point bending setup. This consisted of a six-foot simply supported deck span and a rectangular steel load frame that, when pulled upward by the MTS actuator, applied a symmetrical line load application at two points

near the mid-span of the deck. The spacing between the lines of load was 18 in. Figure 13 illustrates the testing setup for the two-point bending tests.

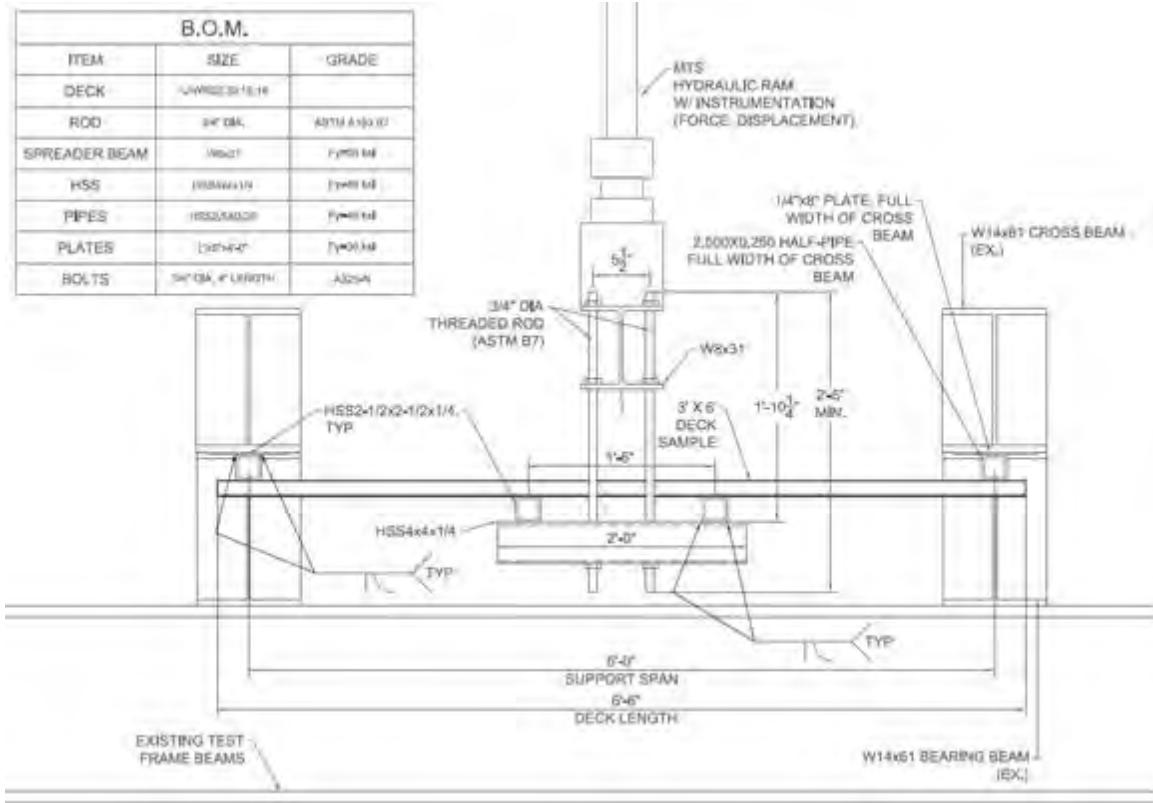


Figure 13: Four Point Bending Test Setup.

The roof deck was simply supported by HSS tubes strapped parallel to the length of the W14×61 cross beams. The W14×61 cross beams are bolted to the W14×61 bearing beams and the bearing beams are bolted to the test frame. The two HSS tubes strapped to the W14×61 cross beams allowed for adjustability to fine-tune the span to be exactly six feet between supports.

The load frame was fabricated out of larger HSS sections to apply the hydraulic actuator's load onto the roof deck. The 18 in. spacing between the lines of load created a constant moment region at the midspan of the deck. A photograph of the load frame is shown in Figure 14.



Figure 14: Load Frame.

The load frame was suspended from a spreader beam by $\frac{3}{4}$ in. diameter threaded rod from a spreader beam that was bolted to the hydraulic actuator. The threaded rod allows for adjustability to level the load frame. A photograph of the fully assembled load frame, threaded rod and cross beam as installed beneath the MTS actuator is shown in Figure 15.

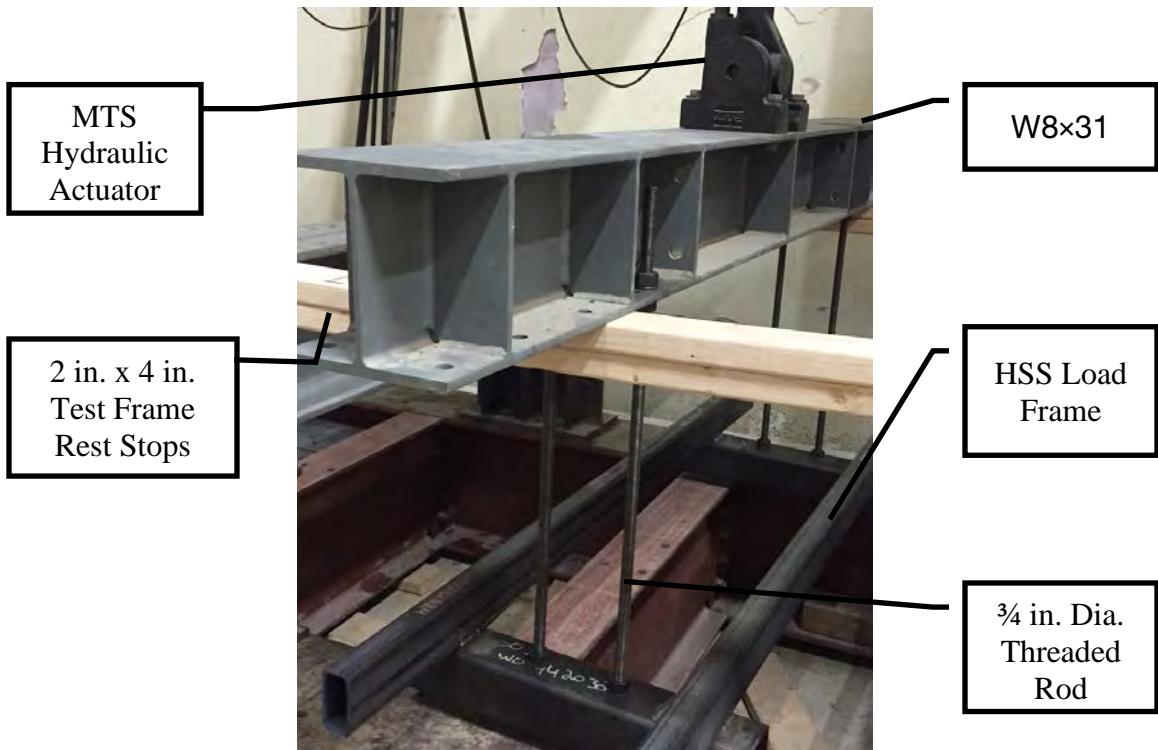


Figure 15: Fully Assembled Load Frame.

2.0.2 Methods of Data Collection

The methods of data collection consisted of numerical data sets, photographs and video. The numerical data consisted of displacement measurements obtained by means of LVDTs placed adjacent to the load frame to measure the deck displacement at different points throughout the duration of the test. The displacement measurements were recorded simultaneously with the force and displacement measurements taken through the MTS hydraulic actuator. Figure 16 shows a deck sample fully instrumented with all LVDTs in place and ready for the test to begin.

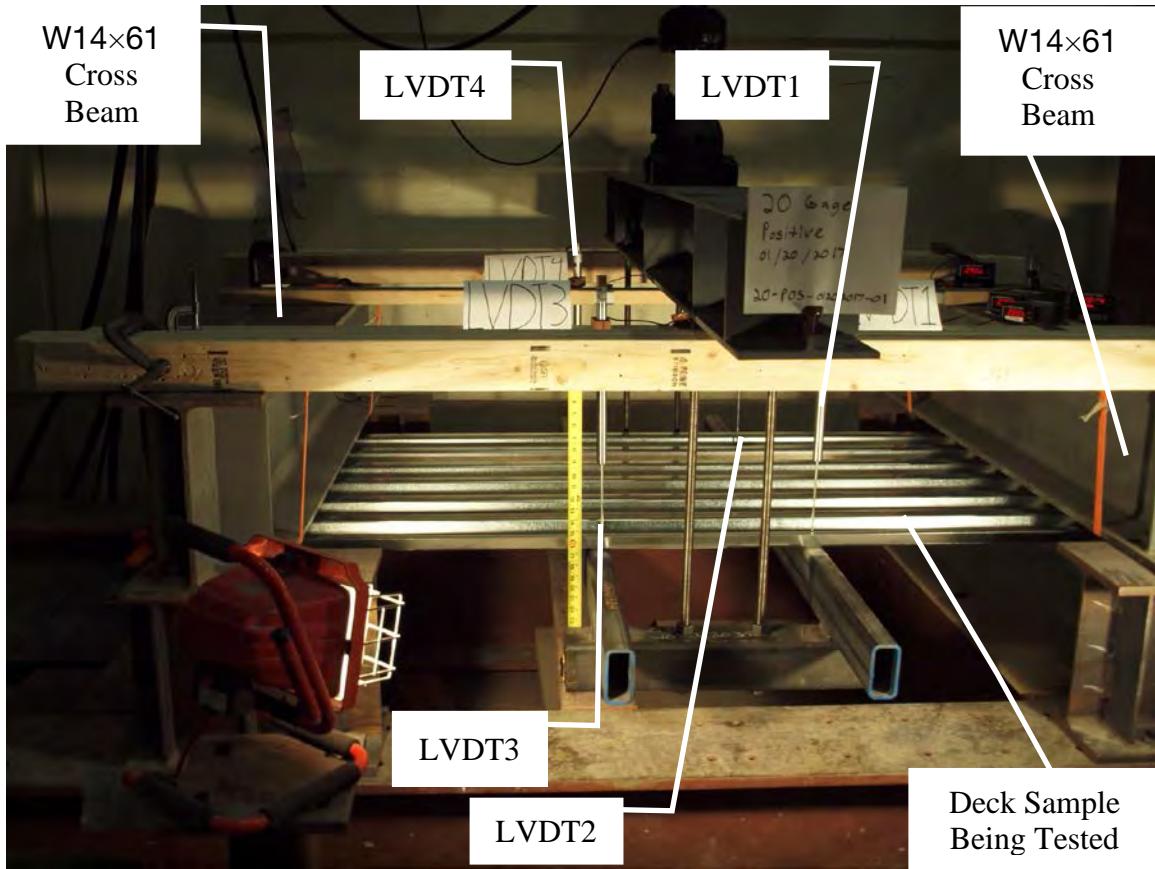


Figure 16: Test Frame with Full Instrumentation in Place.

Photographs and video were taken during each test. These are used to better identify the point of initial failure for each specimen. Photographs were also used to illustrate the progression of failure and to document the initial cause of failure. The video is a real time documentation of the test. The initial actuator force and displacement are read aloud at the beginning of the test and the final force and displacement magnitudes are read aloud at the end of the test.

2.0.3 Experimental Program

The experimental program included 24 total tests of four different gages of steel roof deck. Each of the four deck gages (16, 18, 20 and 22) were tested three times in both the positive and negative position. Table 3 summarizes the tests performed.

Table 3: Summary of Tests.

Deck	Orientation	Number of Tests	Size
1.5WR22	Positive	3	3'-0" x 6'-6"
1.5WR20	Positive	3	3'-0" x 6'-6"
1.5WR18	Positive	3	3'-0" x 6'-6"
1.5WR16	Positive	3	3'-0" x 6'-6"
1.5WR22	Negative	3	3'-0" x 6'-6"
1.5WR20	Negative	3	3'-0" x 6'-6"
1.5WR18	Negative	3	3'-0" x 6'-6"
1.5WR16	Negative	3	3'-0" x 6'-6"

The actuator was run in displacement mode, applying a uniform displacement of 5.5 inches in 10 minutes. Two initial tests were run slower with incremental displacement in order to learn about the deck's behavior prior to running multiple tests, and these two tests slightly deviated from the typical displacement rate. The slow displacement of the actuator allowed for the roof deck to accrue load slowly, and it resulted in a smooth collection of data and an opportunity to capture good quality photos and video during the test. The test was terminated when any one of the four LVDT's maximum stroke was reached (about 6 inches total stroke). Readings of force and displacement were manually recorded at the start and end of the test, and maximum force was noted during the test. This was done to confirm recorded data and to identify when key photographs were taken. Post-test photographs were taken both while the deck was still in the test frame and after it had been removed from the frame.

The test frame and testing setup was designed to apply the load to the steel roof deck as a tension load on the actuator. There was concern that, with higher loadings present especially in the 18 and 16 gage steel roof deck, stability issues for the testing apparatus may lead to results that are not representative of the actual failure. The testing apparatus could potentially displace laterally in the event the steel roof deck deforms in

an uneven manner. Applying the load as a tensile load eliminated the potential for this sort of instability.

The actuator has a clevis mount at the point where the cross beam mounts to it, as well as where the actuator itself mounts to the overall test frame. The clevis is attached to the actuator with a ball-and-socket connection, allowing the clevis to rotate about all three primary axes. This protects the actuator while it is applying a load and allows it to continue to apply an axial deformation to the test subject.

Efforts were made to install all frames, support points and deck samples symmetrically and with level alignment in order to minimize eccentricity. This helped to provide quality data consistent with the intent of the experimental setup, and allowed the experimental data to be compared accurately to the results from the computer model.

Web crippling and crushing was a concern at the beginning of the project. The expected loading that would be required to cause the deck to buckle was in the thousands of pounds and the concentrated forces at the reaction points was an area of concern. Originally, a pipe or an angle piece was to be clamped to the W14×61 cross beam but that was thought to not have enough bearing area, and localized force concentrations may artificially affect results. The final design used an HSS square tube as the reaction point where the deck is supported as it provides a sufficient bearing area so that localized concentrated loads would not occur. The HSS tube still allowed the end of the deck to rotate freely as a true pin support should.

Web crippling was checked using provisions from the AISI S100-2007 specification [1]. Equation (14) (Eq. C3.4.1-1 from AISI S100) was used to calculate the force required to fail one web element in the deck:

$$P_n = C t^2 F_y \sin \theta \left(1 - C_R \sqrt{\frac{R}{t}}\right) \left(1 + C_N \sqrt{\frac{N}{t}}\right) \left(1 - C_h \sqrt{\frac{h}{t}}\right), \quad (14)$$

where

- P_n = Nominal web crippling strength, kips
- C = Coefficient from Table C3.4.1-5 [6]
- t = web thickness, in.
- F_y = Yield Stress, ksi
- θ = Angle between plane of web and plane of bearing surface, degrees
- C_R = inside bend radius coefficient
- R = inside bend radius, in.
- C_N = bearing length coefficient from Table C3.4.1-5 [6]
- N = bearing length, in.
- C_h = web slenderness coefficient from Table C3.4.1-5 [6]
- h = flat dimension of web measured in plane of web, in.

Tables 4 through 7 show the parameters used to calculate web crippling capacities for the different deck gages. The web crippling limit differs depending on whether the load is applied at the end or middle of the steel roof deck sample. Table 8 summarizes the web crippling capacity versus demand for each deck gage.

Table 4: 22 Gage Web Crippling.

Exterior (End)			Interior (Load Point)		
C	3	-	C	8	-
t	0.0295	in.	t	0.0295	in.
F _y	47.1	ksi	F _y	47.1	ksi
θ	72.5	degrees	θ	72.5	degrees
θ	1.265364	radian	θ	1.265364	radian
C _R	0.04	-	C _R	0.1	-
R	0.2179	in.	R	0.2179	in.
C _N	0.29	-	C _N	0.17	-
N	2	in.	N	2	in.
C _h	0.028	-	C _h	0.004	-
h	1.3	in.	h	1.3	in.
P _n	0.288	kips/web	P _n	0.532	kips/web
Total P _n	3.46	kips	Total P _n	6.38	kips

Table 5: 20 Gage Web Crippling.

Exterior (End)			Interior (Load Point)		
C	3	-	C	8	-
t	0.0358	in.	t	0.0358	in.
F _y	48.6	ksi	F _y	48.6	ksi
θ	72.5	degrees	θ	72.5	degrees
θ	1.26536	radian	θ	1.26536	radian
C _R	0.04	-	C _R	0.1	-
R	0.2179	in.	R	0.2179	in.
C _N	0.29	-	C _N	0.17	-
N	2	in.	N	2	in.
C _h	0.028	-	C _h	0.004	-
h	1.3	in.	h	1.3	in.
P _n	0.423	kips/web	P _n	0.793	kips/web
Total P _n	5.08	kips	Total P _n	9.52	kips

Table 6: 18 Gage Web Crippling.

Exterior (End)			Interior (Load Point)		
C	3	-	C	8	-
t	0.0474	in.	t	0.0474	in.
F _y	42.6	ksi	F _y	42.6	ksi
θ	72.5	degrees	θ	72.5	degrees
θ	1.26536	radian	θ	1.26536	radian
C _R	0.04	-	C _R	0.1	-
R	0.2179	in.	R	0.2179	in.
C _N	0.29	-	C _N	0.17	-
N	2	in.	N	2	in.
C _h	0.028	-	C _h	0.004	-
h	1.3	in.	h	1.3	in.
P _n	0.616	kips/web	P _n	1.182	kips/web
Total P _n	7.39	kips	Total P _n	14.18	kips

Table 7: 16 Gage Web Crippling.

Exterior (End)			Interior (Load Point)		
C	3	-	C	8	-
t	0.0598	in.	t	0.0598	in.
F _y	44.9	ksi	F _y	44.9	ksi
θ	72.5	degrees	θ	72.5	degrees
θ	1.26536	radian	θ	1.26536	radian
C _R	0.04	-	C _R	0.1	-
R	0.2179	in.	R	0.2179	in.
C _N	0.29	-	C _N	0.17	-
N	2	in.	N	2	in.
C _h	0.028	-	C _h	0.004	-
h	1.3	in.	h	1.3	in.
P _n	0.988	kips/web	P _n	1.930	kips/web
Total P _n	11.90	kips	Total P _n	23.15	kips

Table 8: Web Crippling Capacity versus Demand.

Deck	Orient.	Ext. Cap. (kips)	Int. Cap. (kips)	Ext. Dem. (kips)	Int. Dem. (kips)
1.5WR22	Positive	3.46	6.38	0.891	0.891
1.5WR20	Positive	5.08	9.52	1.156	1.156
1.5WR18	Positive	7.39	14.18	1.583	1.583
1.5WR16	Positive	11.90	23.15	2.045	2.045
1.5WR22	Negative	3.46	6.38	0.997	0.997
1.5WR20	Negative	5.08	9.52	1.271	1.271
1.5WR18	Negative	7.39	14.18	1.677	1.677
1.5WR16	Negative	11.90	23.15	2.107	2.107

Table 8 suggests that the testing setup proposed and the expected loadings will not exceed the capacity of the webs of the steel roof deck. The failure is expected to be within the constant moment region, which is between the load points from the test frame.

The support points of the steel roof deck specimens were inspected for signs of localized damage (buckling or crippling). There was no observable damage at these locations for any of the tests.

Chapter 3: Results and Discussion

3.0 Numerical Results

Preliminary estimates of the flexural capacity of the steel roof deck were generated prior to testing using the effective width method. These values, along with their equivalent actuator loads, are presented in Table 9.

Table 9: Predicted Load Magnitude at Flexural Yield.

Deck	Orientation	Total Load (lb)	Moment (kip-in.)
1.5WR22	Positive	1,781	24.04
1.5WR20	Positive	2,311	31.20
1.5WR18	Positive	3,166	42.74
1.5WR16	Positive	4,090	55.22
1.5WR22	Negative	1,993	26.91
1.5WR20	Negative	2,542	34.32
1.5WR18	Negative	3,353	45.27
1.5WR16	Negative	4,213	56.88

The moments reported in Table 9 are interpolated from the effective width method capacities reported in Tables 1 and 2 for the measured average yield stress values shown in Table 10. The total load reported in Table 9 is the equivalent actuator load for simple support of the deck with two concentrated load points as illustrated in Figure 17.

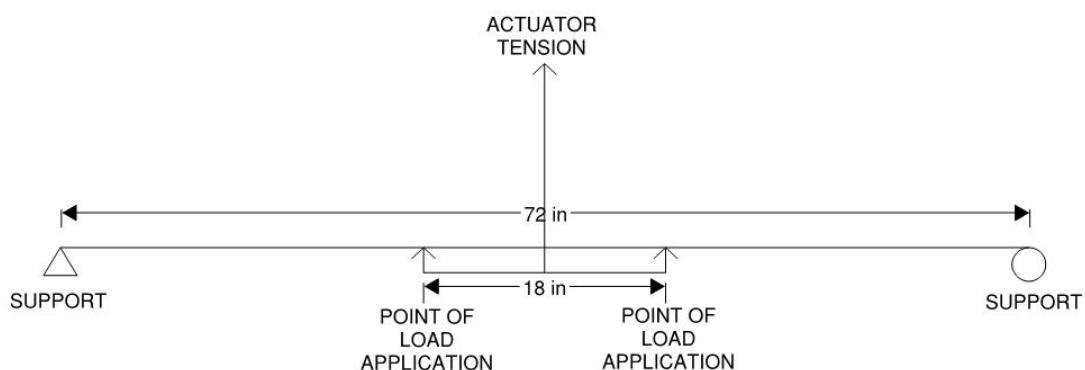


Figure 17: Preliminary Loading Diagram.

3.0.1 Material Testing Results

The steel roof deck that was donated from CANAM Group had additional samples cut from both the web and flute. These were then sent to a material test lab, which were subsequently cut into dog bone coupons and tested for yield and tensile limits using ASTM A1008. The results are summarized in Table 10 with the average column containing the average between the web and the flute that was used for calculations.

Table 10: Material Testing Results.

Deck	Flute Yield (ksi)	Flange Yield (ksi)	Average Yield (ksi)
1.5WR22	47.10	41.90	44.50
1.5WR20	48.60	45.90	47.25
1.5WR18	42.60	44.30	43.45
1.5WR16	44.90	44.50	44.7

3.0.2 Effective Width Results

The Effective Width Method was used to calculate the nominal moment capacity of the deck for initial comparison to the experimental results. Tables 11 and 12 show a comparison between the results from Dudenbostel [1] and current calculations. The moment capacities calculated are based on a 3 foot wide cross-section. Although both Dudenbostel's calculations and the current calculations used a 1.5B nominal roof deck, the current calculations were based on the profile of the physical deck specimens (measured width of the deck specimen, overall profile of the specimen) whereas Dudenbostel used a typical profile as published in manufacturers' data. The EWM calculations followed the discussion from Section 1.2 where effective widths for the web and flange were calculated and used to calculate the effective section modulus. Example calculations are included in Appendix A.

Table 11: EWM Comparison Fy = 40 ksi (Dudenbostel versus Gwozdz).

Deck	Orientation	Dudenbostel EWM Mn (kip-in.)	Gwozdz EWM Mn (kip-in.)
1.5WR22	Positive	20.29	18.46
1.5WR20	Positive	25.36	23.41
1.5WR18	Positive	34.69	33.88
1.5WR16	Positive	44.71	45.08
1.5WR22	Negative	22.21	21.54
1.5WR20	Negative	27.46	27.34
1.5WR18	Negative	36.22	39.15
1.5WR16	Negative	45.50	49.58

Table 12: EWM Comparison Fy = 50 ksi (Dudenbostel versus Gwozdz).

Deck	Orientation	Dudenbostel EWM Mn (kip-in.)	Gwozdz EWM Mn (kip-in.)
1.5WR22	Positive	24.04	23.07
1.5WR20	Positive	31.20	29.27
1.5WR18	Positive	42.74	42.36
1.5WR16	Positive	55.22	56.36
1.5WR22	Negative	26.91	26.92
1.5WR20	Negative	34.32	34.17
1.5WR18	Negative	45.27	48.94
1.5WR16	Negative	56.88	61.98

Table 13 summarizes the results of the EWM for each of the different deck gages in both positive and negative flexural orientation. These calculations used the actual yield stress as determined from material testing.

Table 13: Summary of Results Using Effective Width Method.

Deck	Orientation	Yield Stress (ksi)	EWM Mn (kip-in.)	Expected Load (lbs)*
1.5WR22	Positive	44.50	20.53	1521
1.5WR20	Positive	47.25	27.66	2049
1.5WR18	Positive	43.45	36.81	2726
1.5WR16	Positive	44.70	50.38	3732
1.5WR22	Negative	44.50	23.96	1775
1.5WR20	Negative	47.25	32.29	2392
1.5WR18	Negative	43.45	42.53	3150
1.5WR16	Negative	44.70	55.41	4104

* The “expected” load can be compared to the applied actuator load from Table 1. It is the load necessary to generate the nominal moment, M_n , in the four-point bending configuration used in experimental tests.

The results were compared to the effective sections that Dudenbostel found using the EWM [1]. While not perfectly comparable since Dudenbostel used theoretical yield stresses of 40 ksi and 50 ksi, the comparison could be used to benchmark the current EWM calculations. The results (Table 14) fell in between the 40 ksi and 50 ksi results found by Dudenbostel, which is to be expected since the yield strength from material testing fell between those magnitudes.

Table 14: EWM Comparison (As Tested versus Theoretical).

Deck	Orientation	Yield Stress (ksi)	EWM M_n (kip-in.) $F_y=40\text{ksi}$	EWM M_n (kip-in.) $F_y=\text{As Tested}$	EWM M_n (kip-in.) $F_y=50\text{ksi}$
1.5WR22	Positive	44.50	20.29	20.53	24.04
1.5WR20	Positive	47.25	25.36	27.66	31.20
1.5WR18	Positive	43.45	34.69	36.81	42.74
1.5WR16	Positive	44.70	44.71	50.38	55.22
1.5WR22	Negative	44.50	22.21	23.96	26.91
1.5WR20	Negative	47.25	27.46	32.29	34.32
1.5WR18	Negative	43.45	36.22	42.53	45.27
1.5WR16	Negative	44.70	45.50	55.41	56.88

3.0.3 Direct Strength Results

Similar to the EWM comparisons, Tables 15 and 16 show a comparison between Dudenbostel's DSM calculations and the current DSM calculations. The tables report a moment capacity based on a 3 foot width of steel roof deck.

Table 15: DSM Comparison $F_y = 40 \text{ ksi}$ (Dudenbostel versus Gwozdz).

Deck	Orientation	Dudenbostel DSM M_n (kip-in.)	Gwozdz DSM M_n (kip-in.)
1.5WR22	Positive	16.86	14.99
1.5WR20	Positive	23.16	21.18
1.5WR18	Positive	36.45	34.92
1.5WR16	Positive	47.26	49.20
1.5WR22	Negative	23.52	18.45
1.5WR20	Negative	28.53	24.47
1.5WR18	Negative	37.62	37.02
1.5WR16	Negative	47.26	49.20

Table 16: DSM Comparison Fy = 50 ksi (Dudenbostel versus Gwozdz).

Deck	Orientation	Dudenbostel DSM Mn (kip-in.)	Gwozdz DSM Mn (kip-in.)
1.5WR22	Positive	19.50	18.73
1.5WR20	Positive	26.86	25.37
1.5WR18	Positive	42.43	43.65
1.5WR16	Positive	59.08	61.50
1.5WR22	Negative	27.41	23.07
1.5WR20	Negative	35.66	30.59
1.5WR18	Negative	47.02	46.28
1.5WR16	Negative	59.08	61.50

Table 17 summarizes the results from the Direct Strength Method for determining the nominal moment capacity of the four different deck types in both positive and negative orientation.

Table 17: Summary of Results Using Direct Strength Method.

Deck	Orientation	Yield Stress (ksi)	DSM Mn (kip-in.)	Expected Load (lbs)*
1.5WR22	Positive	44.50	16.67	1,235
1.5WR20	Positive	47.25	23.98	1,853
1.5WR18	Positive	43.45	37.93	2,809
1.5WR16	Positive	44.70	54.98	4,072
1.5WR22	Negative	44.50	20.53	1,520
1.5WR20	Negative	47.25	28.91	2,141
1.5WR18	Negative	43.45	40.22	2,979
1.5WR16	Negative	44.70	54.98	4,072

* The “expected” load can be compared to the applied actuator load from Table 1. It is the load necessary to generate the nominal moment, M_n , in the four-point bending configuration used in experimental tests.

Table 18 further compares the Direct Strength Method results to Dudenbostel’s results at two different yield strengths.

Table 18: Summary of Results Using Direct Strength Method.

Deck	Orientation	Yield Stress (ksi)	DSM Mn (kip-in.) Fy=40ksi	DSM Mn (kip-in.) Fy=As Tested	DSM Mn (kip-in.) Fy=50ksi
1.5WR22	Positive	44.50	16.86	16.67	19.50
1.5WR20	Positive	47.25	23.16	23.98	26.86
1.5WR18	Positive	43.45	36.45	37.93	42.43
1.5WR16	Positive	44.70	47.26	54.98	59.08
1.5WR22	Negative	44.50	23.52	20.53	27.41
1.5WR20	Negative	47.25	28.53	28.91	35.66
1.5WR18	Negative	43.45	37.62	40.22	47.02
1.5WR16	Negative	44.70	47.26	54.98	59.08

* The “expected” load can be compared to the applied actuator load from Table 1. It is the load necessary to generate the nominal moment, M_n , in the four-point bending configuration used in experimental tests.

The nominal strength determined using the tested yield stress fell between the 40 ksi and 50 ksi magnitudes as calculated by Dudenbostel, with the exception of the 22 gage deck that fell just below the results for the 40 ksi deck. The lower capacity could be attributed to the differences between the deck cross-sections used. The values are still very similar.

3.1 Experimental Results

3.1.1 Graphical Results

The experimental results are displayed over the next several pages in a graphical format, as the graphs show measured load versus measured displacement throughout the duration of each test. The following naming scheme was used:

“(Gage of Deck)-(Positive or Negative Orientation)-(MMDDYYYY)-(Test Number)”.

For example, test 16-NEG-02102017-01 would identify the first 16 gage deck in its negative bending position conducted on February 10, 2017. The following graphs are the results of each of the four point moment testing done for each of the different steel roof deck gages. Figures 18, 19 and 20 show the results for the 16 gage roof deck tests for negative bending.

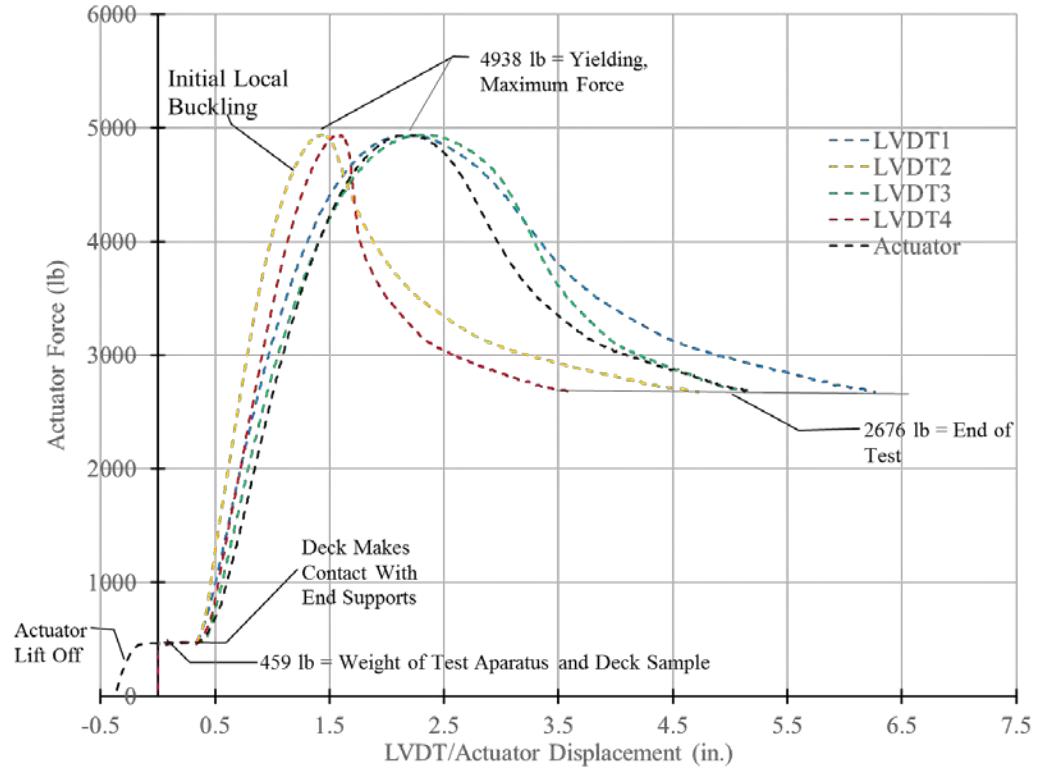


Figure 18: Results for Test 16-NEG-02102017-01.

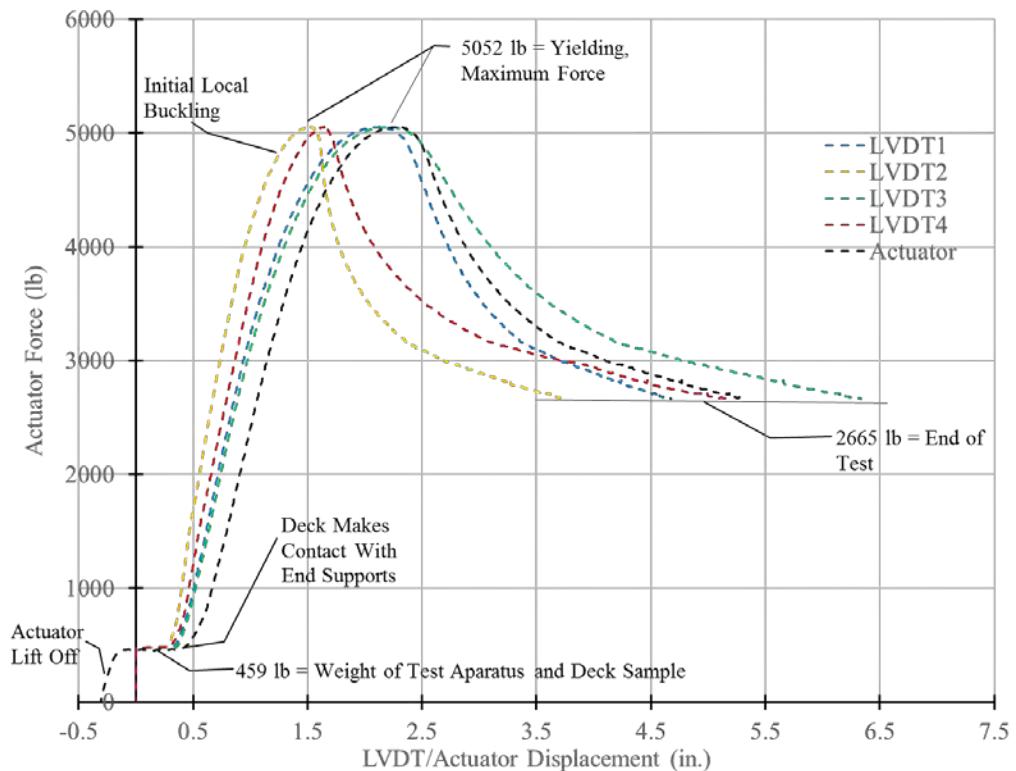


Figure 19: Results for Test 16-NEG-02222017-02.

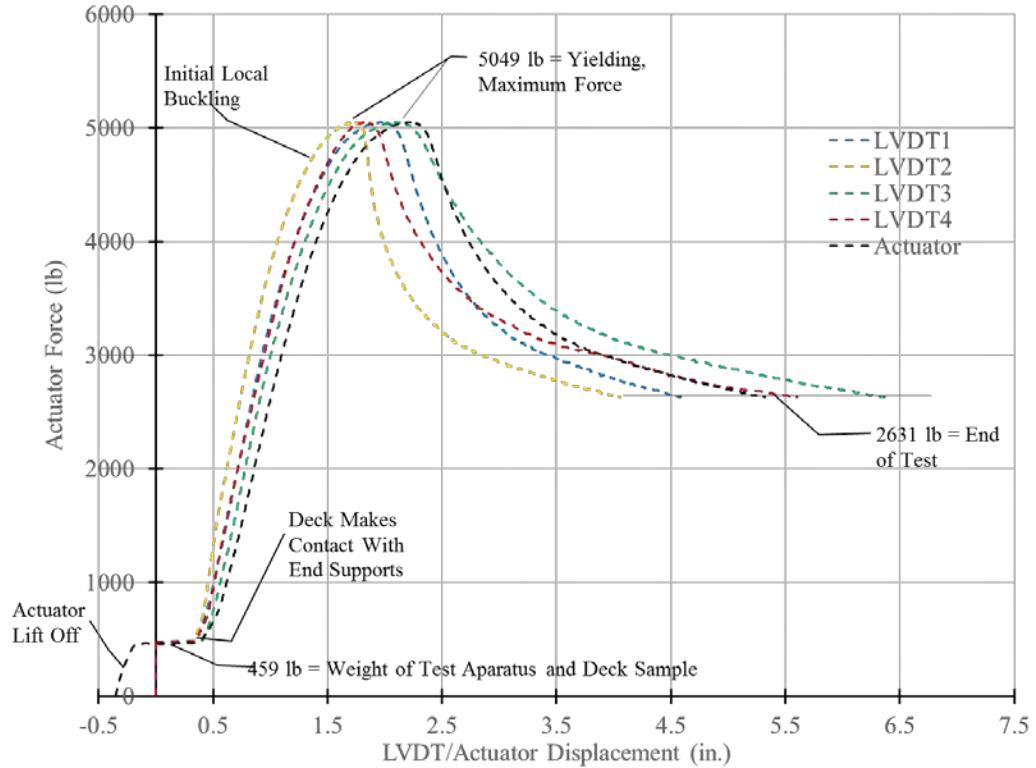


Figure 20: Results for Test 16-NEG-02222017-03.

Figure 21 shows the results from each of the three 16 gage negative tests overlaid on one another. There is excellent consistency among results. The overlay plot shows measured force versus measured displacement at the actuator (typical for all overlay plots in this section of the report).

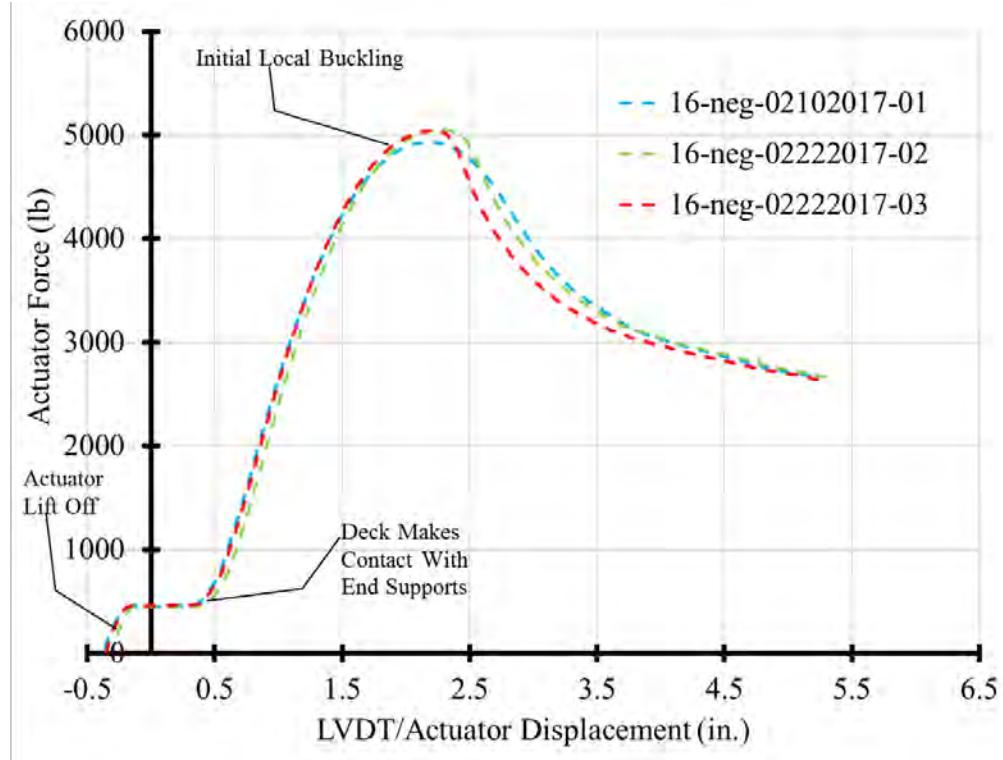


Figure 21: Overlay of 16 Gage Negative Test Results.

Figure 22 is a photograph of the 16 gage deck in negative bending showing the early signs of local buckling. Notice the webs starting to buckle laterally.

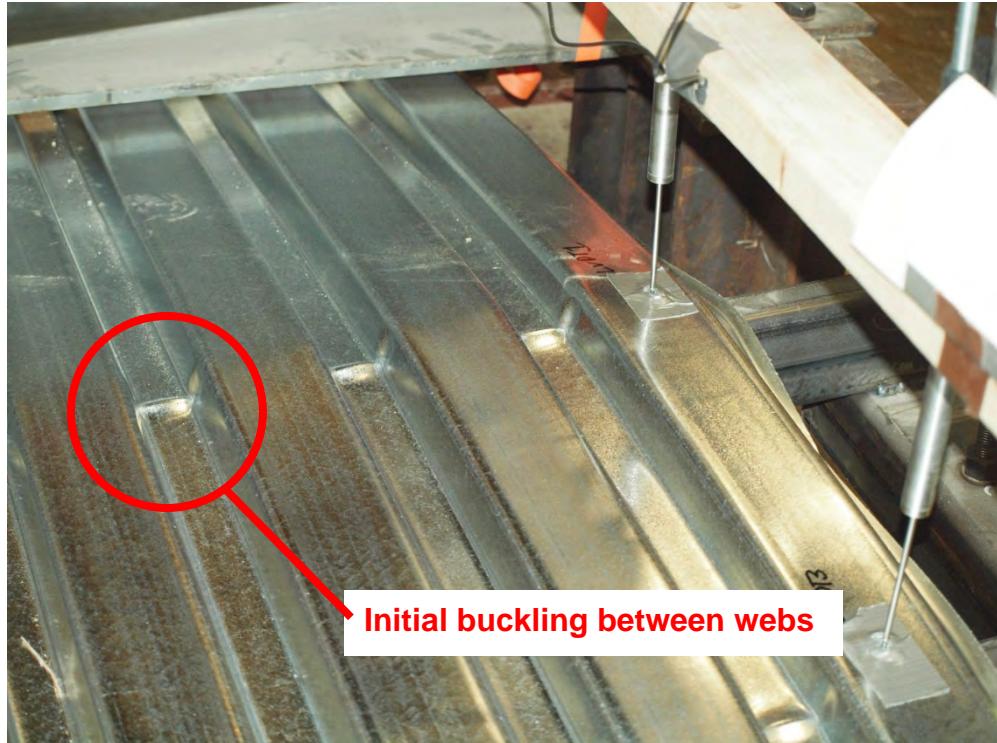


Figure 22: 16 Gage Deck Negative Bending - Initial Buckling.

Figure 23 is a photograph of the 16 gage deck in negative bending close to the maximum applied load. Notice the ribs severely buckle, particularly at the edge of the deck.

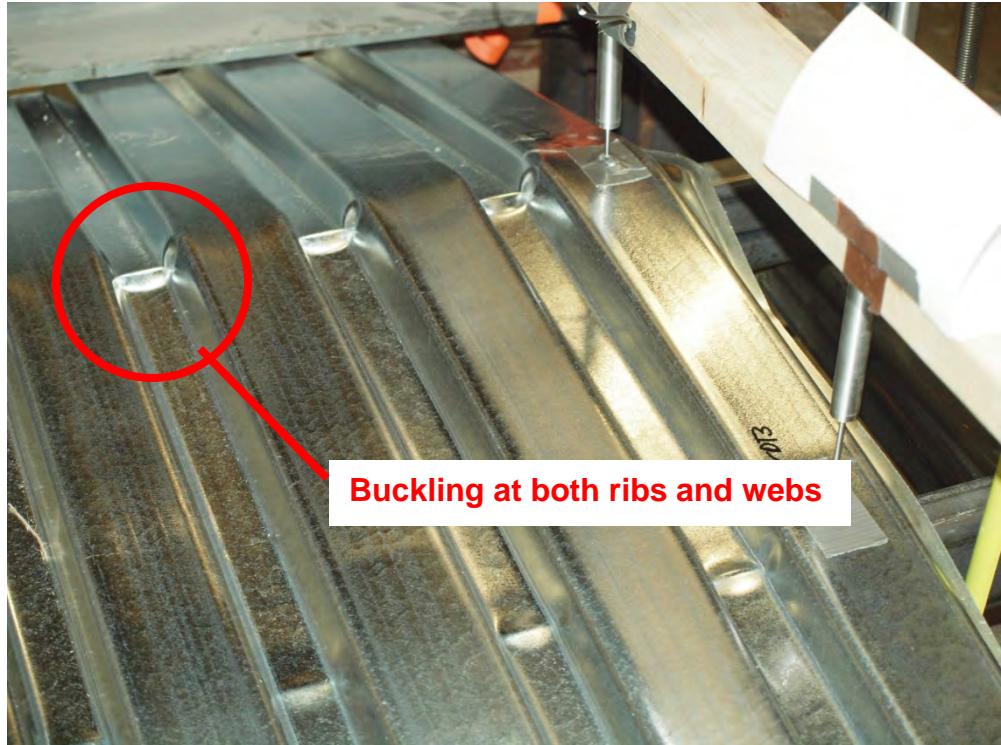


Figure 23: 16 Gage Deck Negative Bending - Further Buckling.

Figures 24 and 25 are photographs showing the final state of a 16 gage deck in negative bending. Note that the configuration is similar to that seen in Figure 23, only with more deformation.

Figure 26 is a photograph of the deck after it has been removed from the test frame. The deck is permanently deformed with both local and global buckling remaining visible.



Figure 24: 16 Gage Deck Negative Bending - Final State.



Figure 25: 16 Gage Deck Negative Bending – End of Test.



Figure 26: 16 Gage Deck Negative Bending – Specimen Removed.

Figures 27, 28 and 29 show the results for the 16 gage roof deck tests for positive bending.

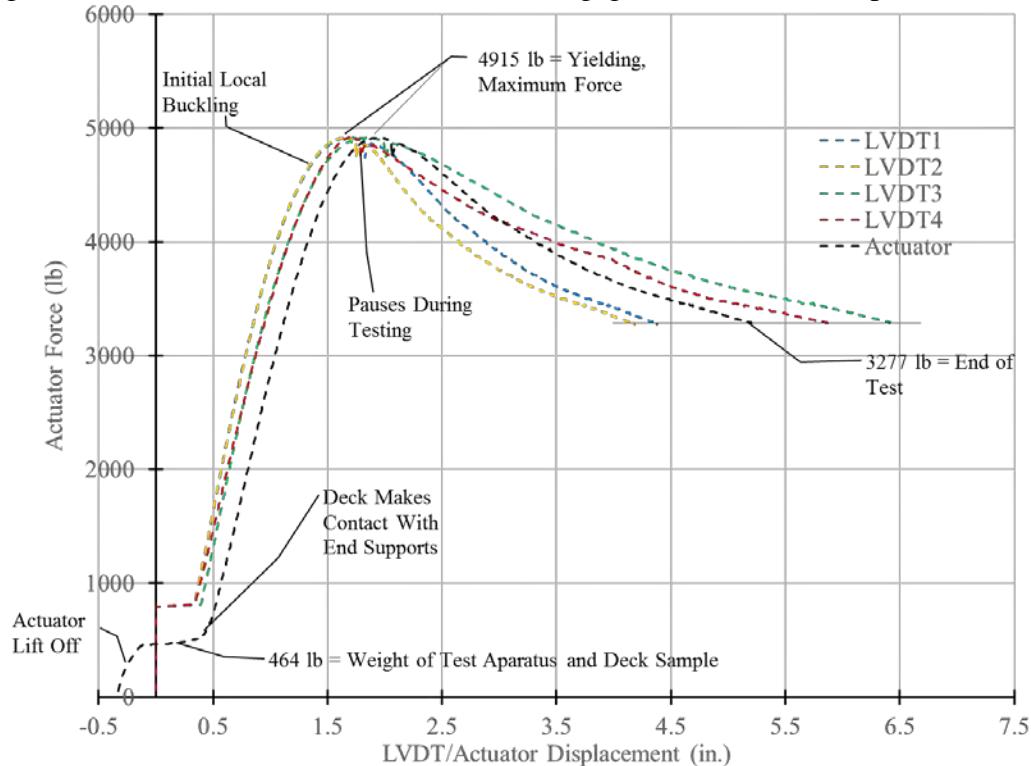


Figure 27: Results for Test 16-POS-02102017-01.

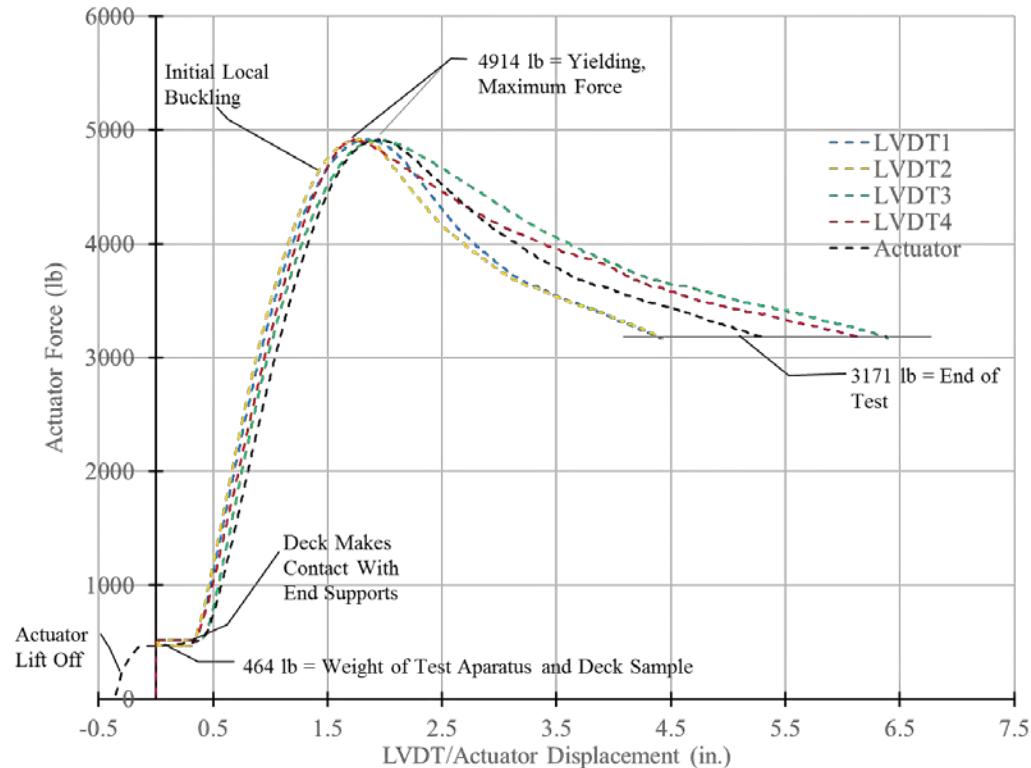


Figure 28: Results for Test 16-POS-02172017-02.

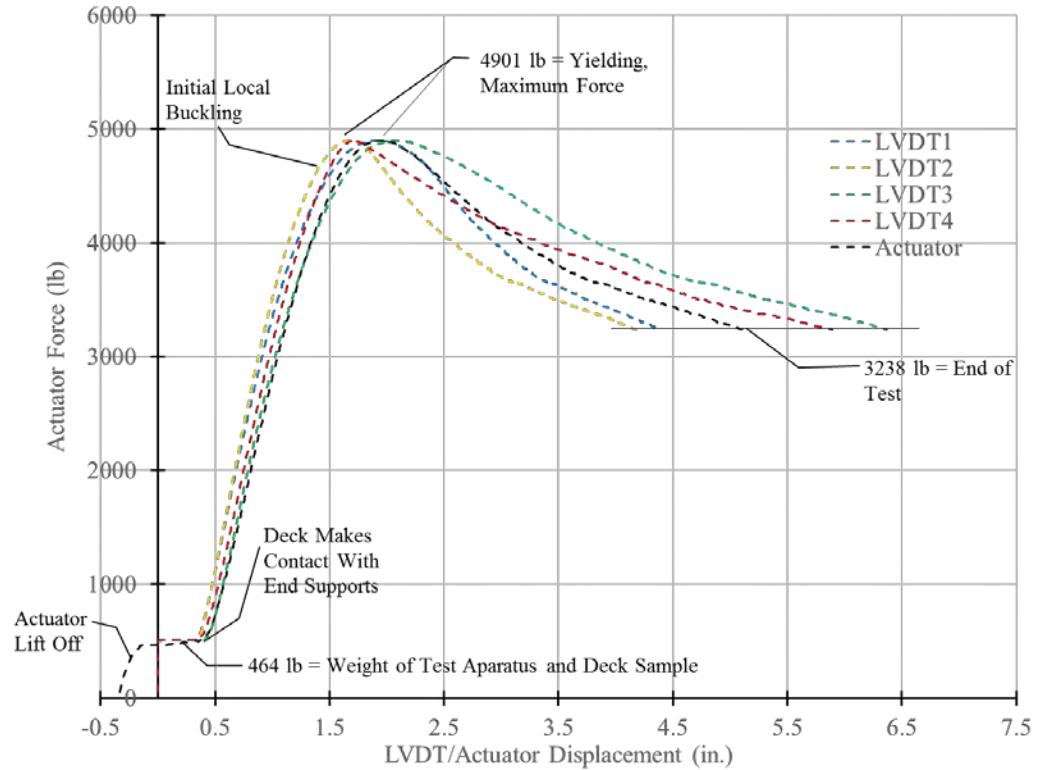


Figure 29: Results for Test 16-POS-02172017-03.

Figure 30 shows the results from each of the three 16 gage positive tests overlaid on one another. As with the negative tests, there is excellent consistency among the results.

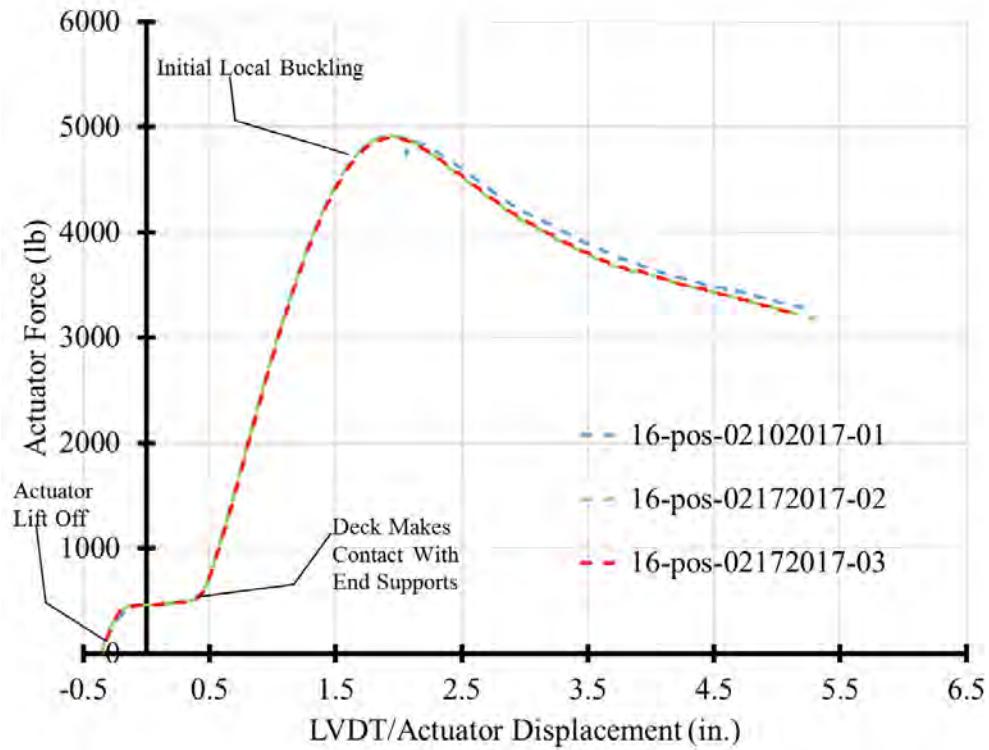


Figure 30: Overlay of 16 Gage Positive Test Results.

Figure 31 is a photograph of 16 gage deck in positive bending showing the early signs of local buckling within the ribs.

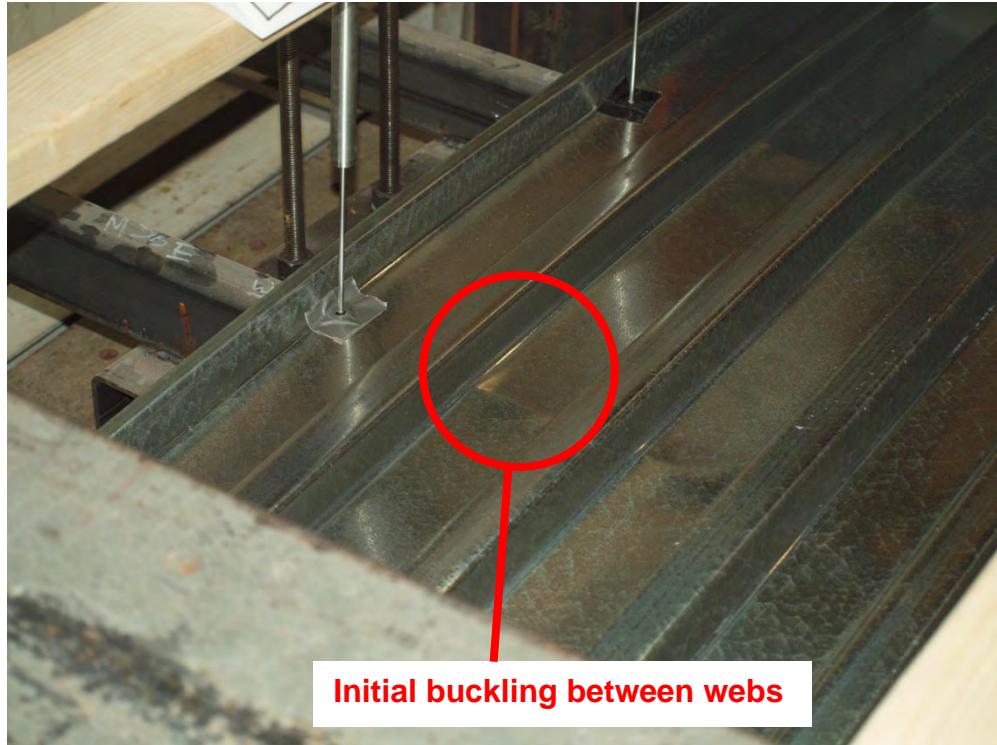


Figure 31: 16 Gage Deck Positive Bending - Initial Buckling.

Figure 32 is a photograph of 16 gage deck in positive bending showing additional deformation in the ribs and the webs.



Figure 32: 16 Gage Deck Positive Bending - Further Buckling.

Figure 33 is a photograph of 16 gage deck in positive bending showing the webs severely buckled along with the ribs.

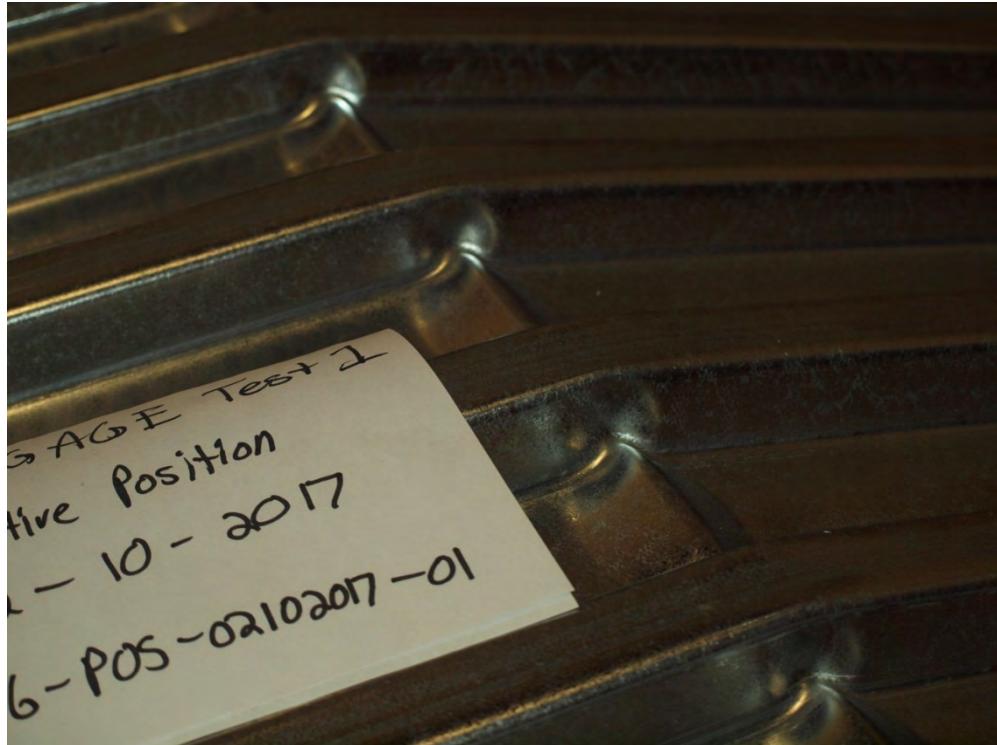


Figure 33: 16 Gage Deck Positive Bending – Both Ribs and Webs Buckling.

Figure 34 is a photograph of 16 gage deck in positive bending removed from the test frame in its final state.



Figure 34: 16 Gage Deck Positive Bending - Final State.

Figures 35, 36 and 37 show the results for the 18 gage roof deck tests for negative bending.

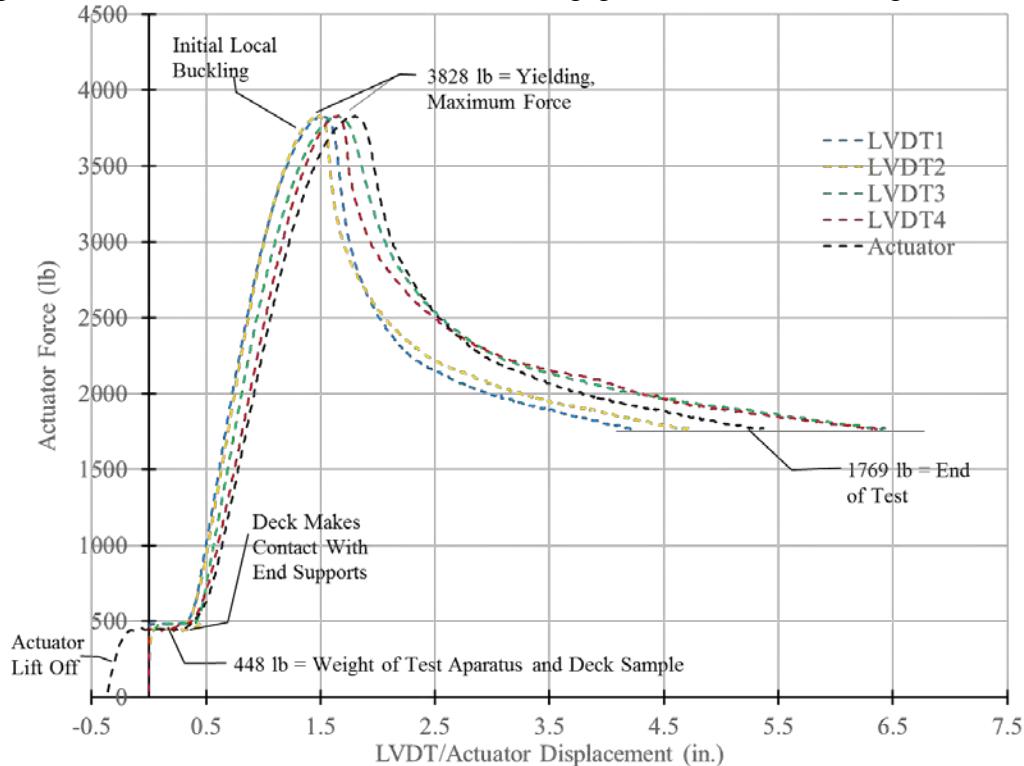


Figure 35: Results for Test 18-NEG-02172017-01.

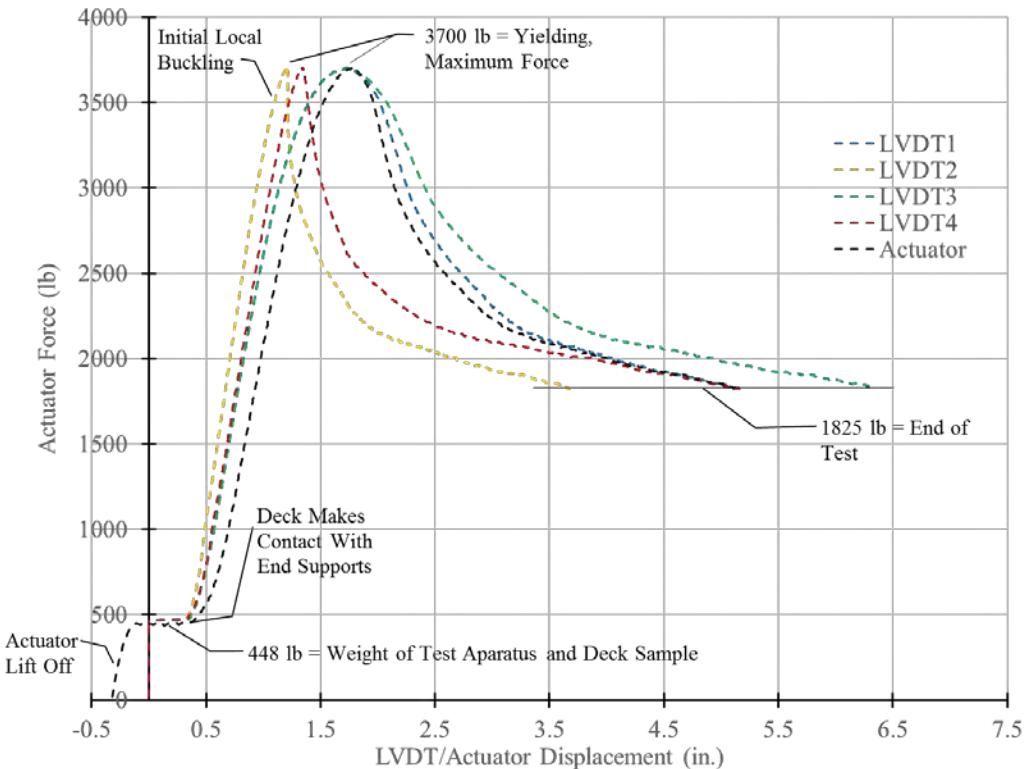


Figure 36: Results for Test 18-NEG-02222017-02.

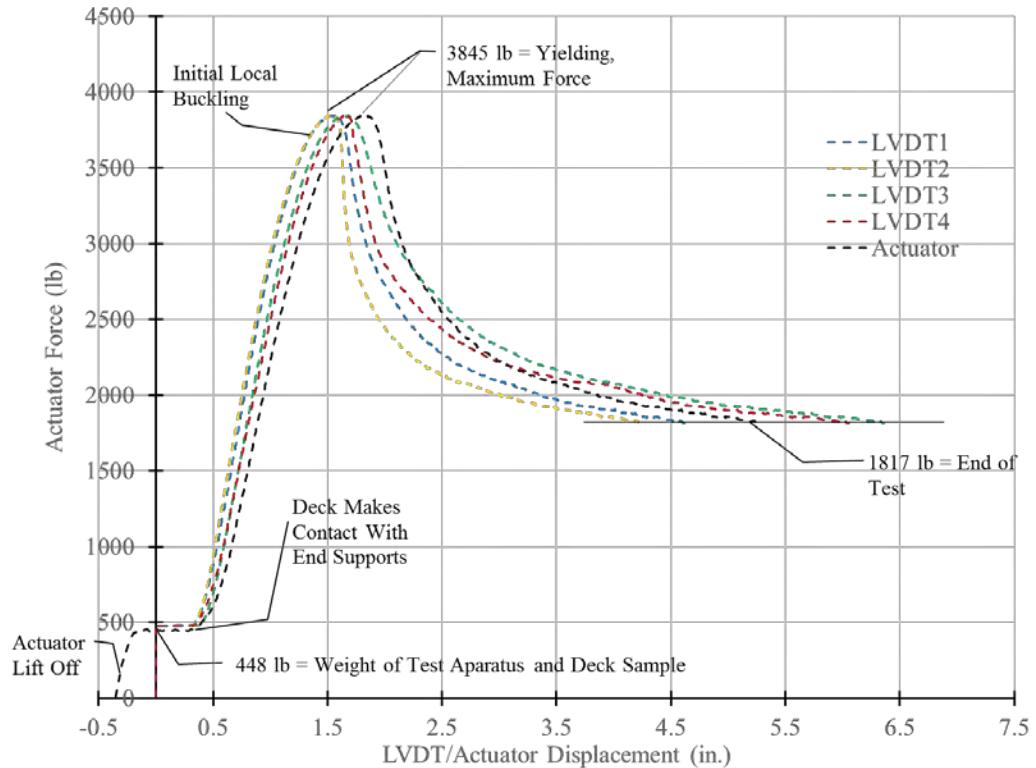


Figure 37: Results for Test 18-NEG-02222017-03.

Figure 38 shows the results from each of the three 18 gage negative tests overlaid on one another. As with the 16 gage tests, there is excellent consistency among results.

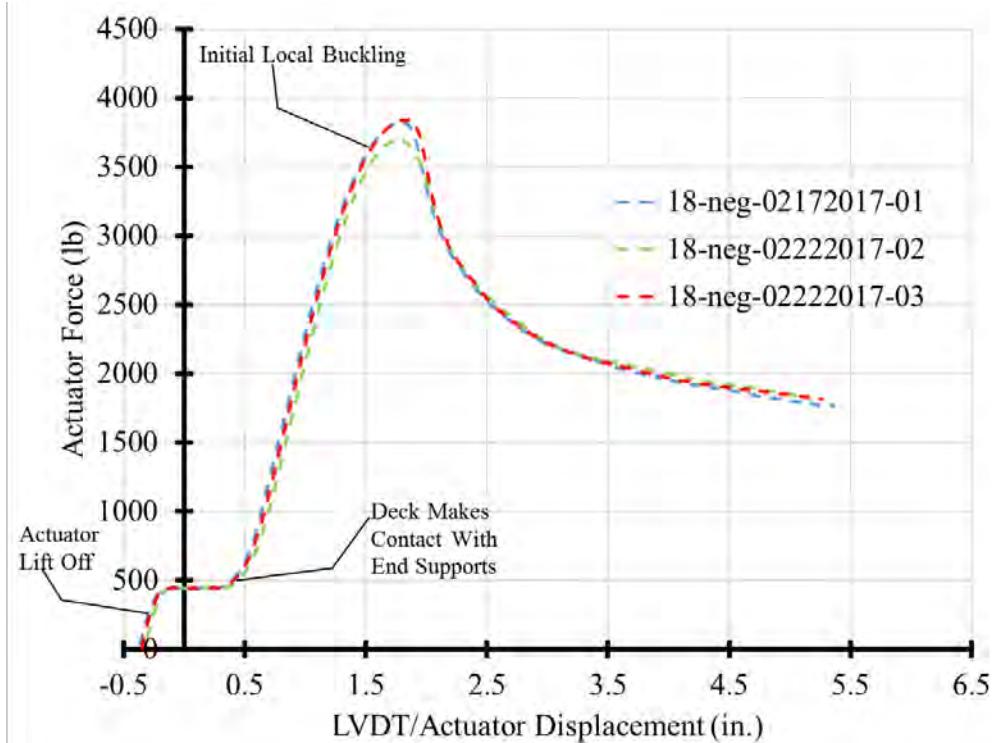


Figure 38: Overlay of 18 Gage Negative Test Results.

Figure 39 is a photograph of 18 gage deck in negative bending showing the initial signs of local buckling in the ribs and the webs.

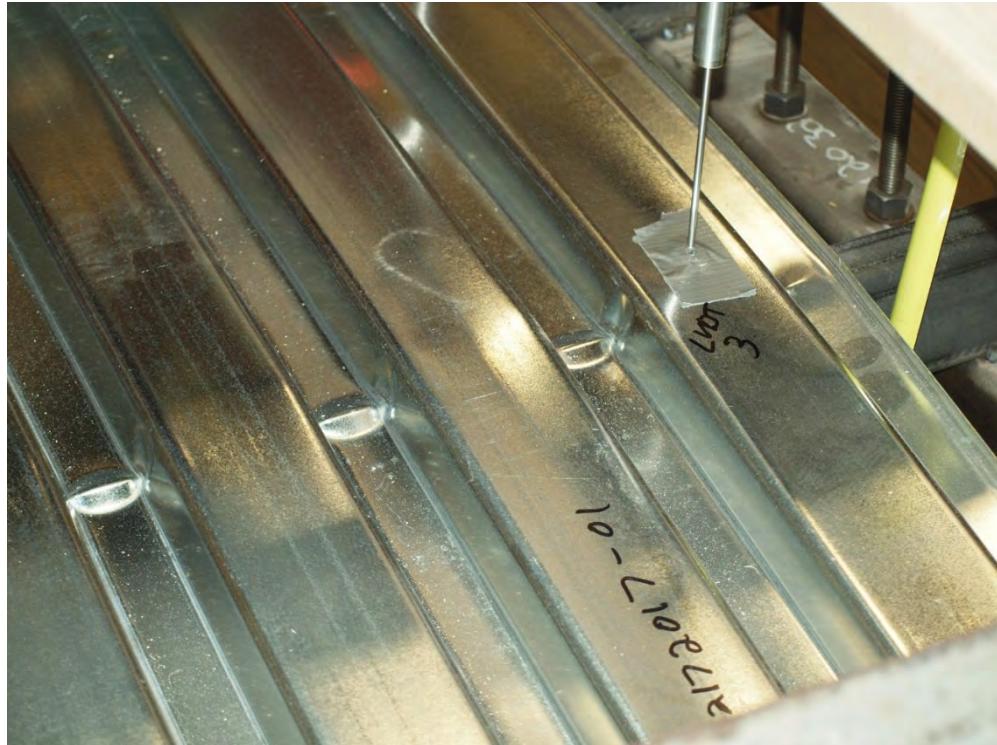


Figure 39: 18 Gage Deck Negative Bending - Initial Buckling.

Figure 40 is a photograph of 18 gage deck in negative bending severely deformed from local buckling and nearing the end of the test.



Figure 40: 18 Gage Deck Negative Bending - Further Buckling.

Figure 41 is a photograph of 18 gage deck in negative bending after being removed from the test frame in its final state.



Figure 41: 18 Gage Deck Negative Bending - Final State.

Figures 42, 43 and 44 show the results for the 18 gage roof deck tests for positive bending.

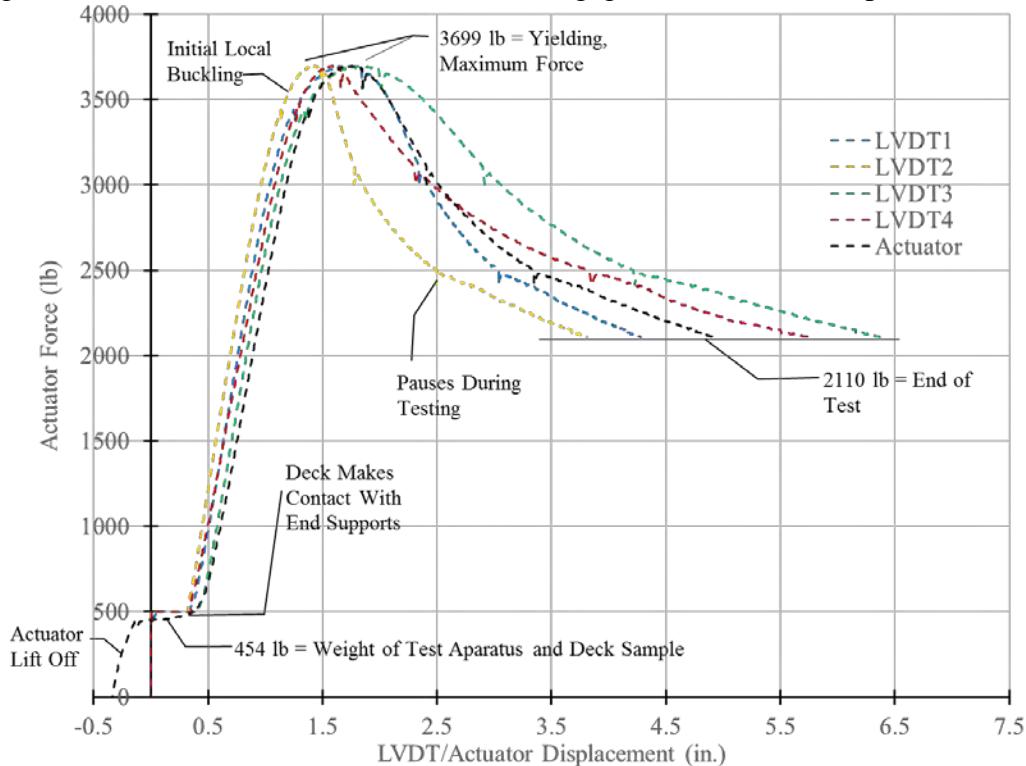


Figure 42: Results for Test 18-POS-02102017-01.

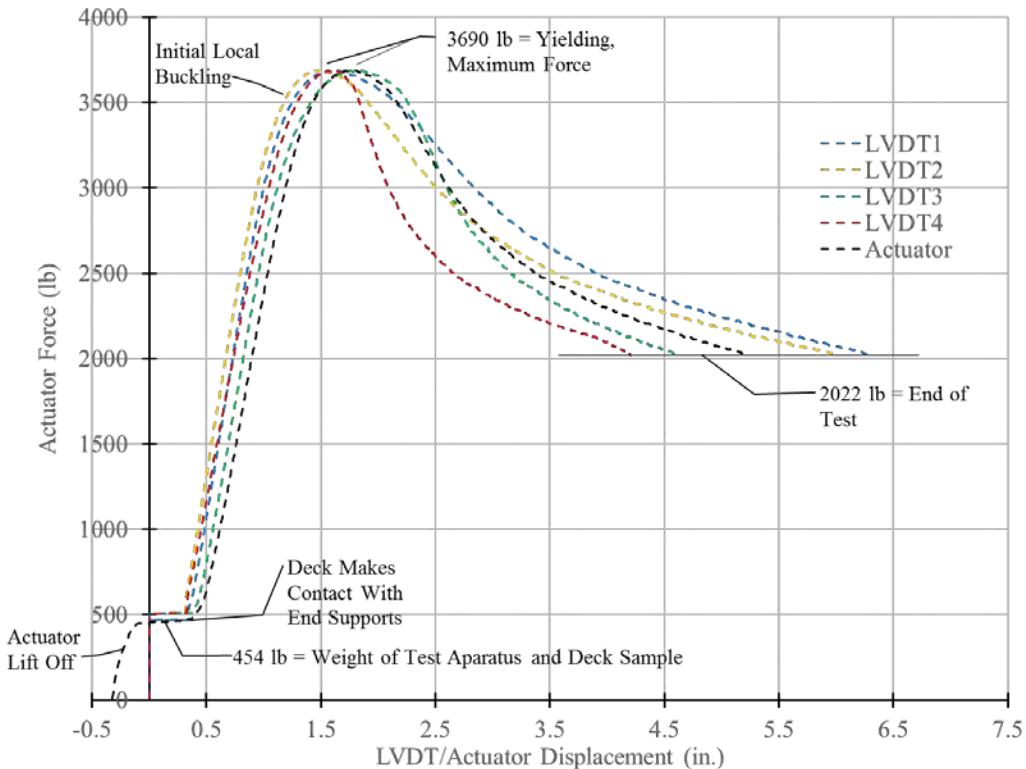


Figure 43: Results for Test 18-POS-02172017-02.

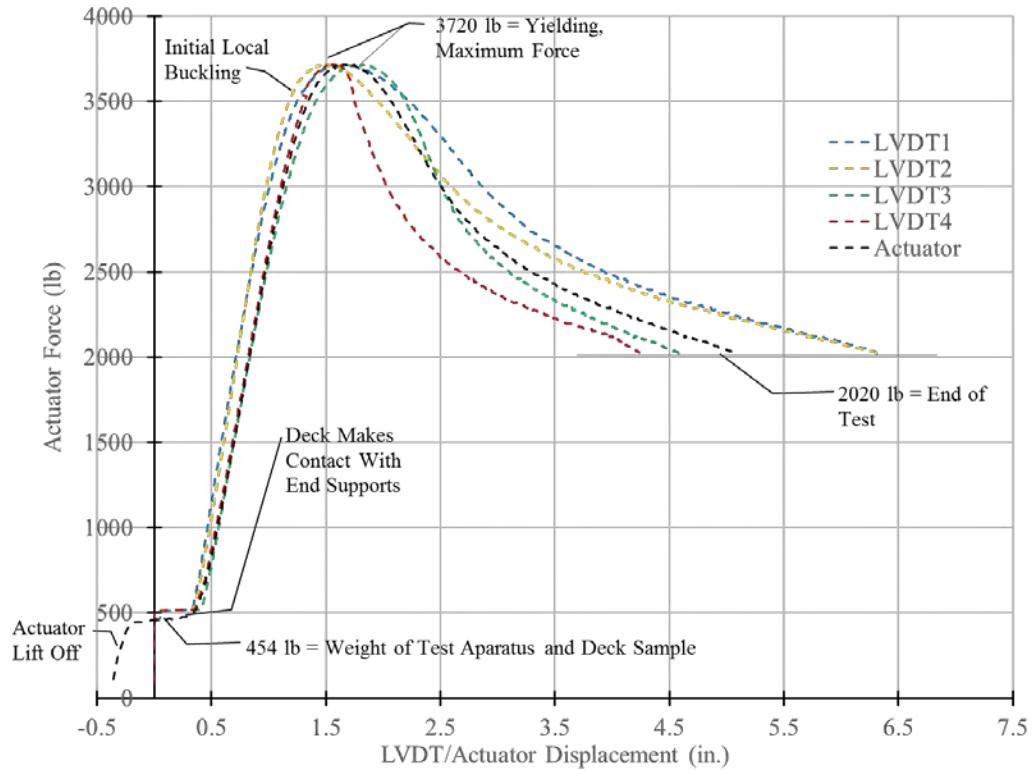


Figure 44: Results for Test 18-POS-02172017-03.

Figure 45 shows the results from each of the three 16 gage positive tests overlaid on one another. Once again, the plots show excellent consistency among tests.

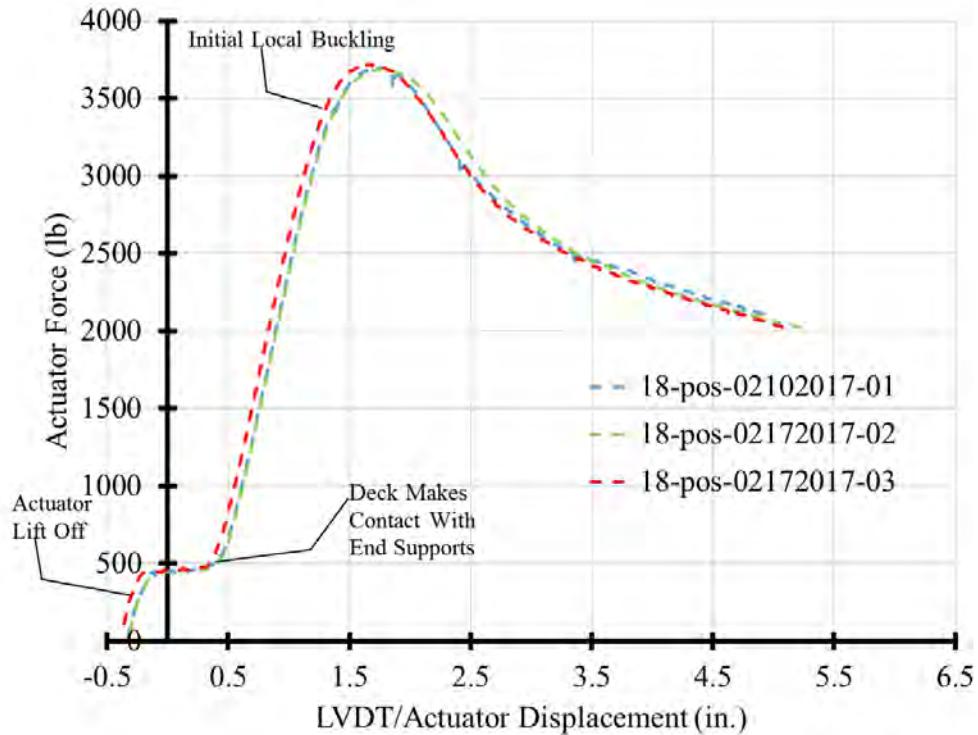


Figure 45: Overlay of 18 Gage Positive Test Results.

Figure 46 shows a photograph of 18 gage deck in positive bending test in place prior to testing.

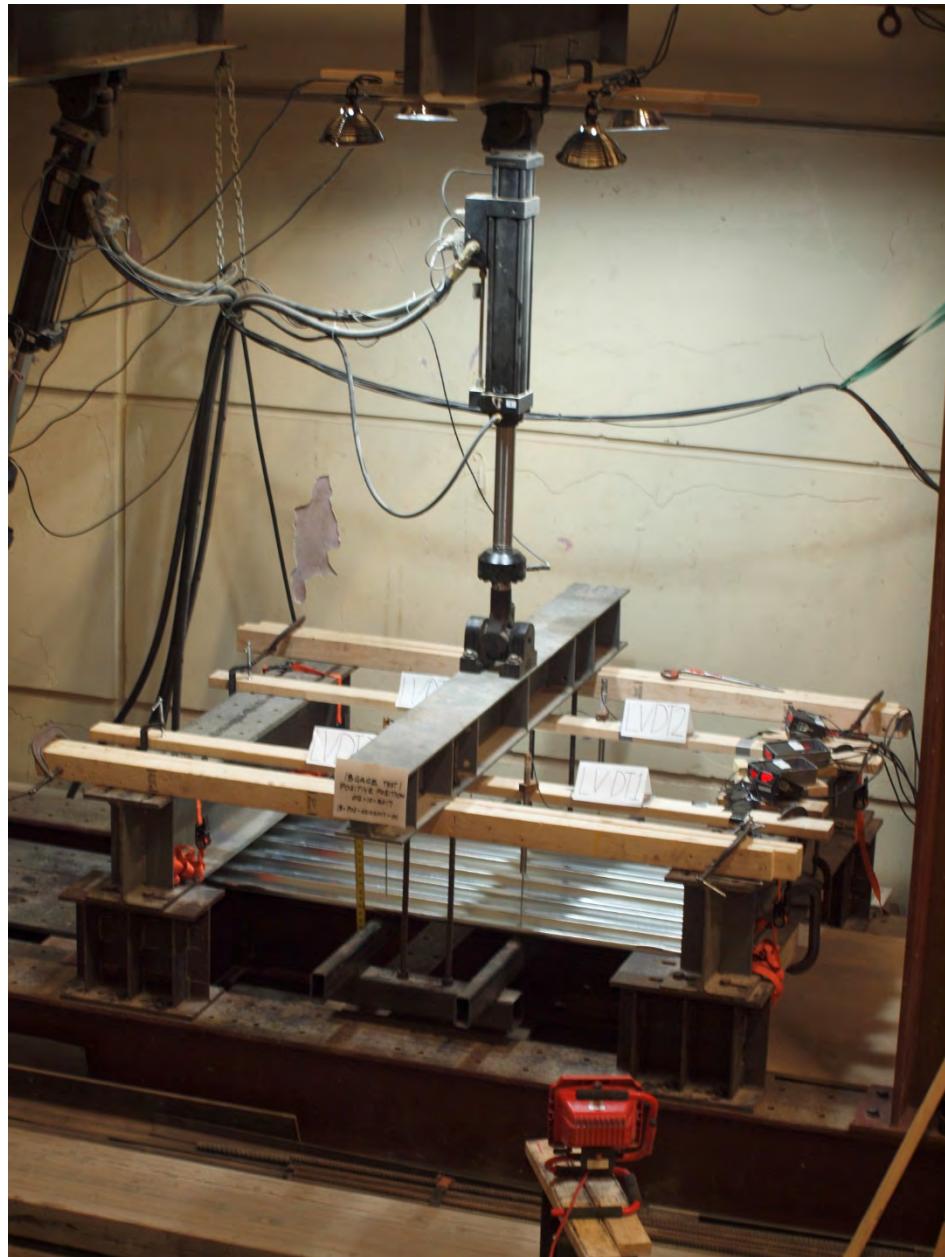


Figure 46: 18 Gage Deck Positive Bending - Initial Setup.

Figure 47 is a photograph of 18 gage deck in positive bending with slight local buckling beginning in the webs and the ribs.

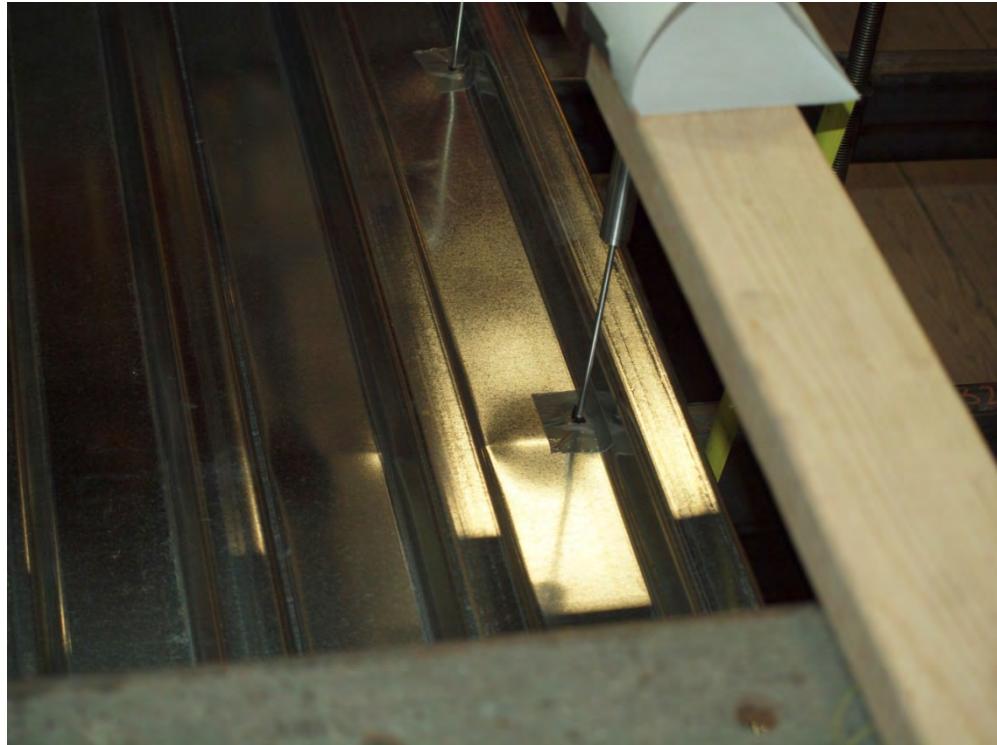


Figure 47: 18 Gage Deck Positive Bending - Initial Buckling.

Figure 48 is a photograph of 18 gage deck in positive bending with more severe local buckling and deformation. Notice the ribs at the application of the load have severely buckled.



Figure 48: 18 Gage Deck Positive Bending - Further Buckling.

Figures 49, 50 and 51 show the results for the 20 gage roof deck tests for negative bending.

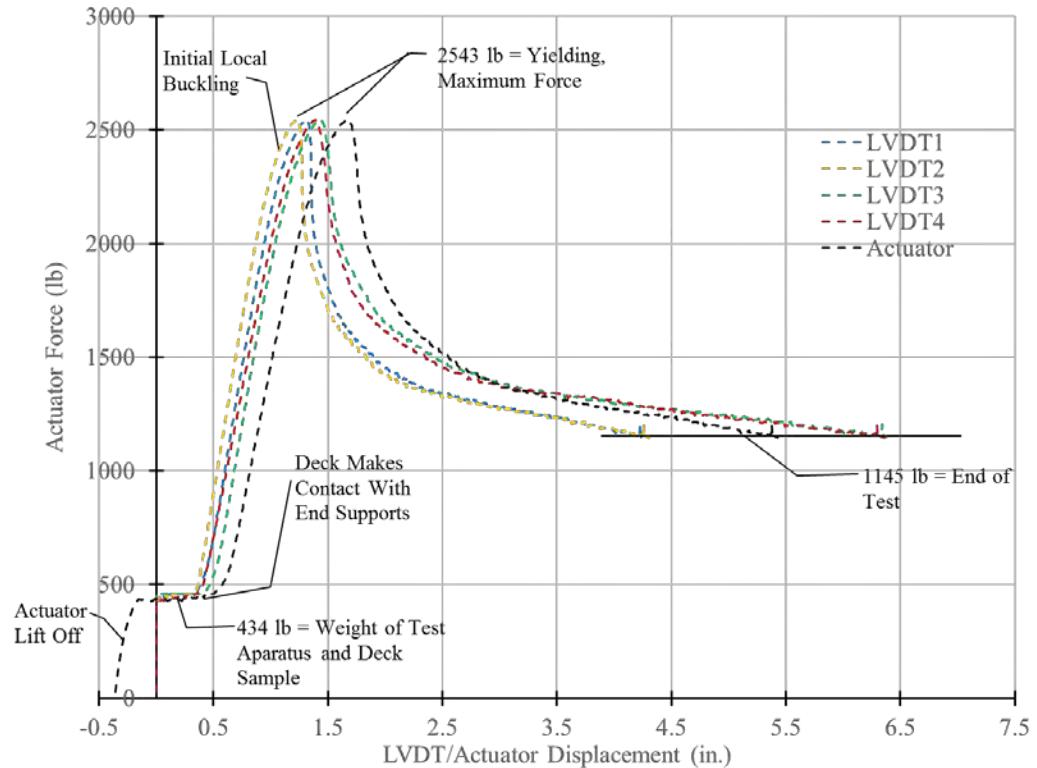


Figure 49: Results for Test 20-NEG-02172017-01.

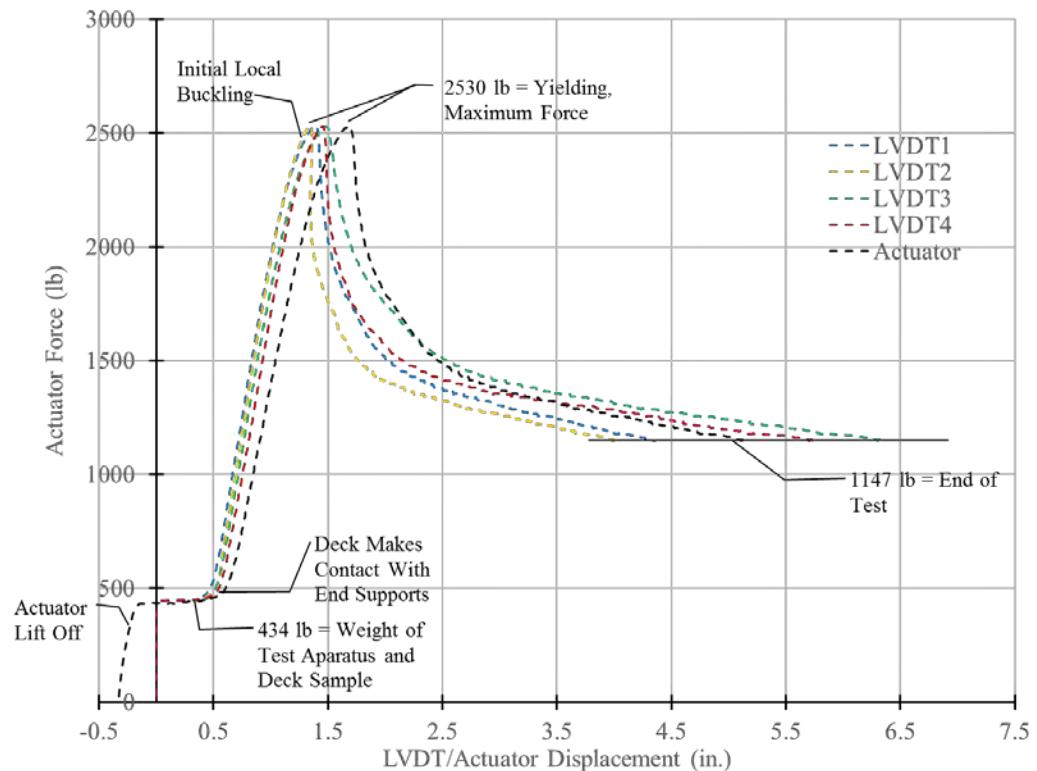


Figure 50: Results for Test 20-NEG-02222017-02.

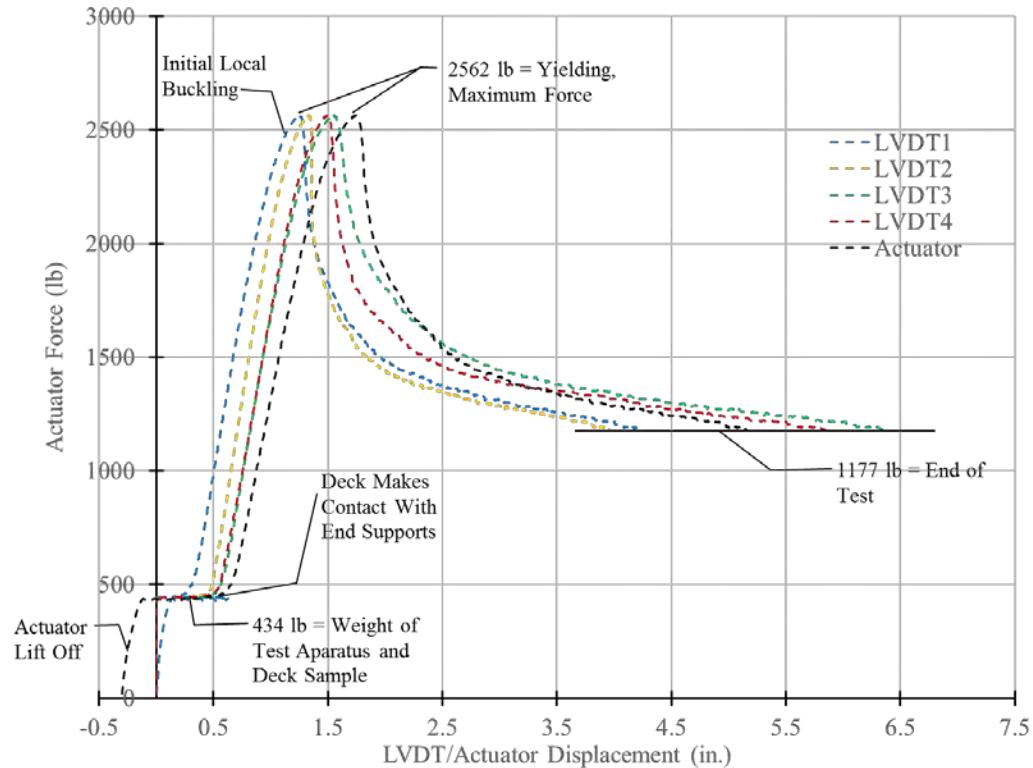


Figure 51: Results for Test 20-NEG-02222017-03.

Figure 52 shows the results from each of the three 20 gage negative tests overlaid on one another. Results among tests are consistent.

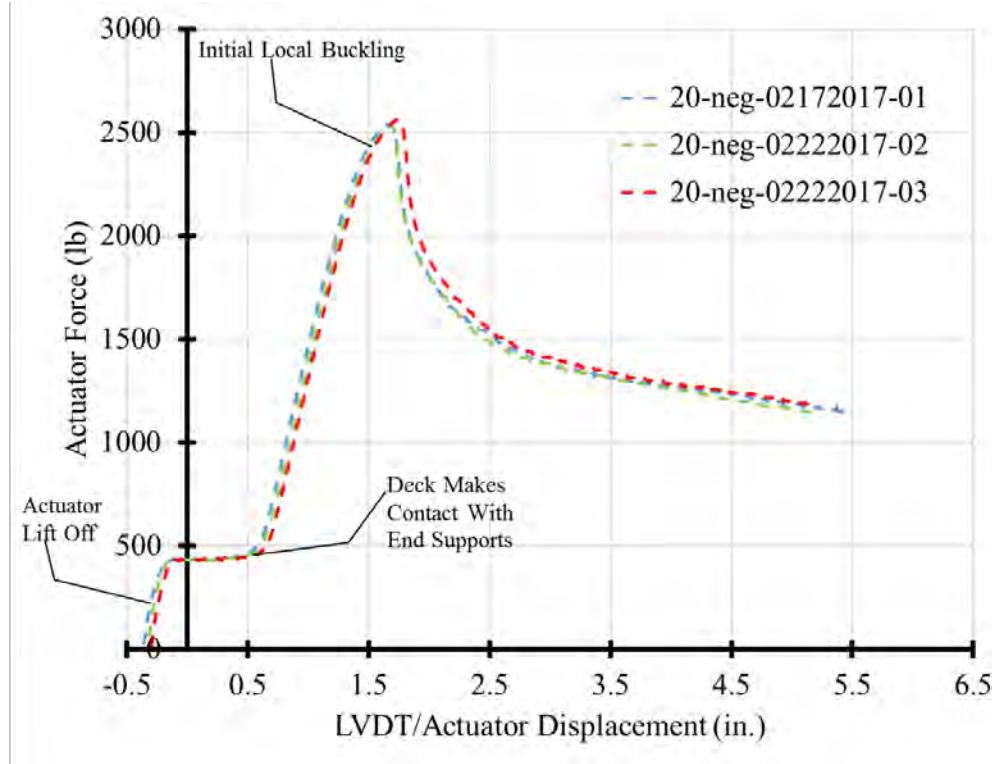


Figure 52: Overlay of 20 Gage Negative Test Results.

Figure 53 is a photograph of 20 gage deck in negative bending showing the initial signs of local buckling. This is typical after reaching the highest force reading and starting to decrease in applied load.



Figure 53: 20 Gage Deck Negative Bending - Initial Buckling.

Figure 54 is a photograph of 20 gage deck in negative bending with severe local buckling nearing the end of the test.

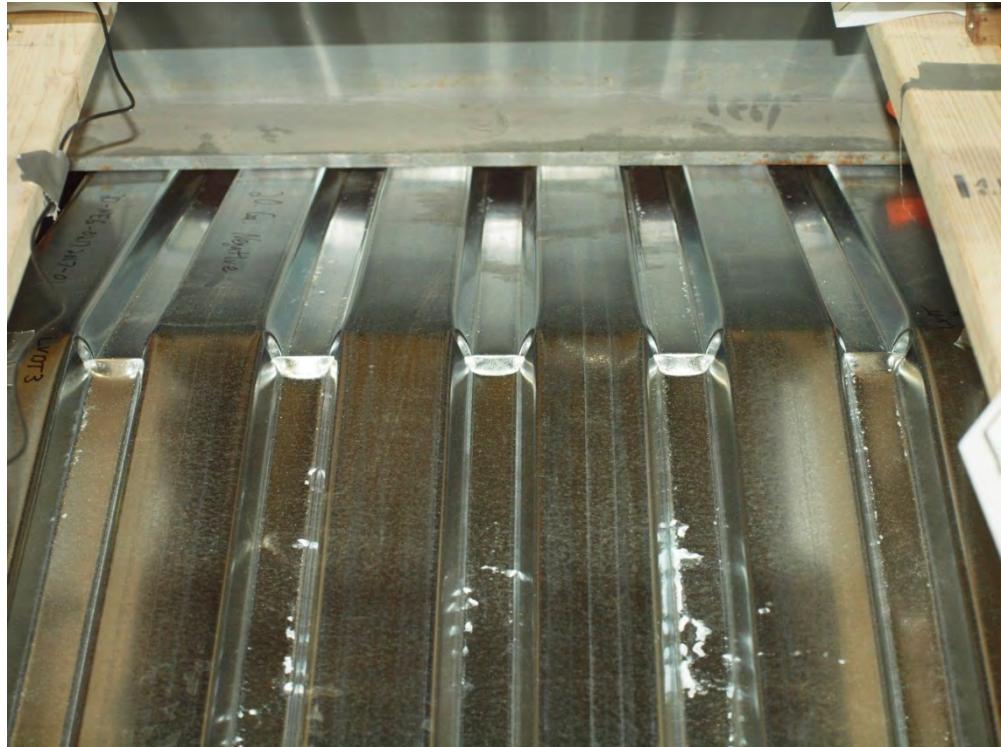


Figure 54: 20 Gage Deck Negative Bending - Further Buckling.

Figure 55 shows the results of the first 20 gage steel roof deck test for positive bending. This test had an issue with LVDT 3 and the signal conditioner returned fuzzy data. However, the maximum force at yielding is still useful as the load sensor was still reporting the data accurately. These data were still used in the average yielding force to compare with the analytical values.

Figures 56 through 58 show the results of the second through fourth 20 gage tests in the positive bending position, respectively. One additional test was conducted with this configuration.

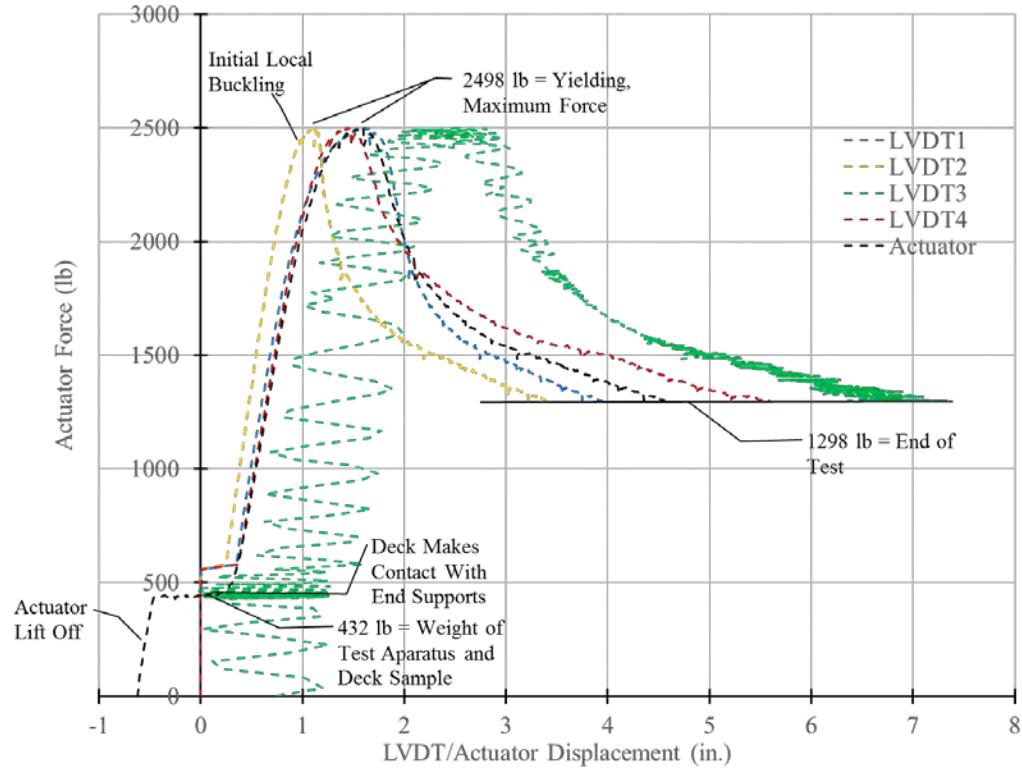


Figure 55: Results for Test 20-POS-01202017-01.

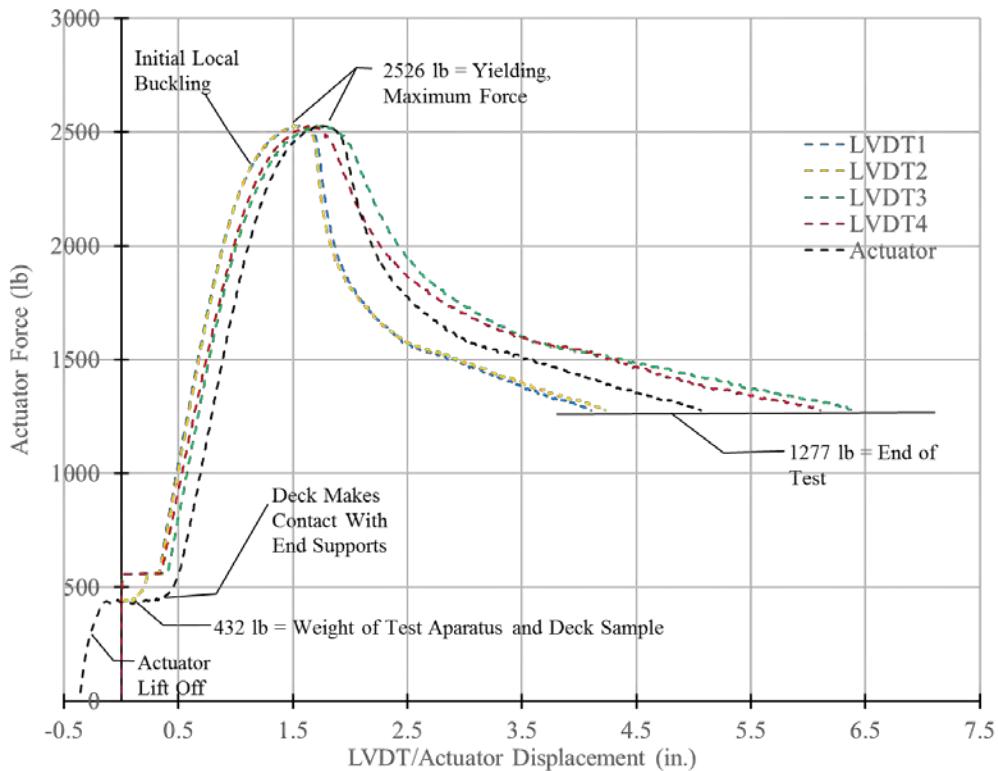


Figure 56: Results for Test 20-POS-02172017-02.

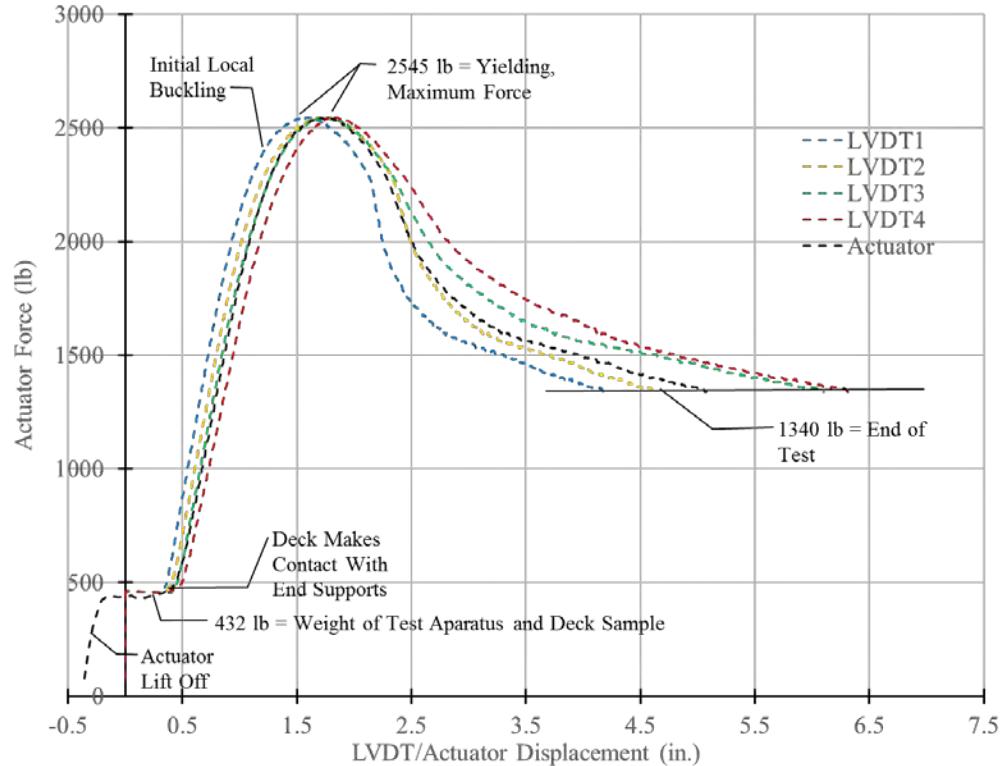


Figure 57: Results for Test 20-POS-02172017-03.

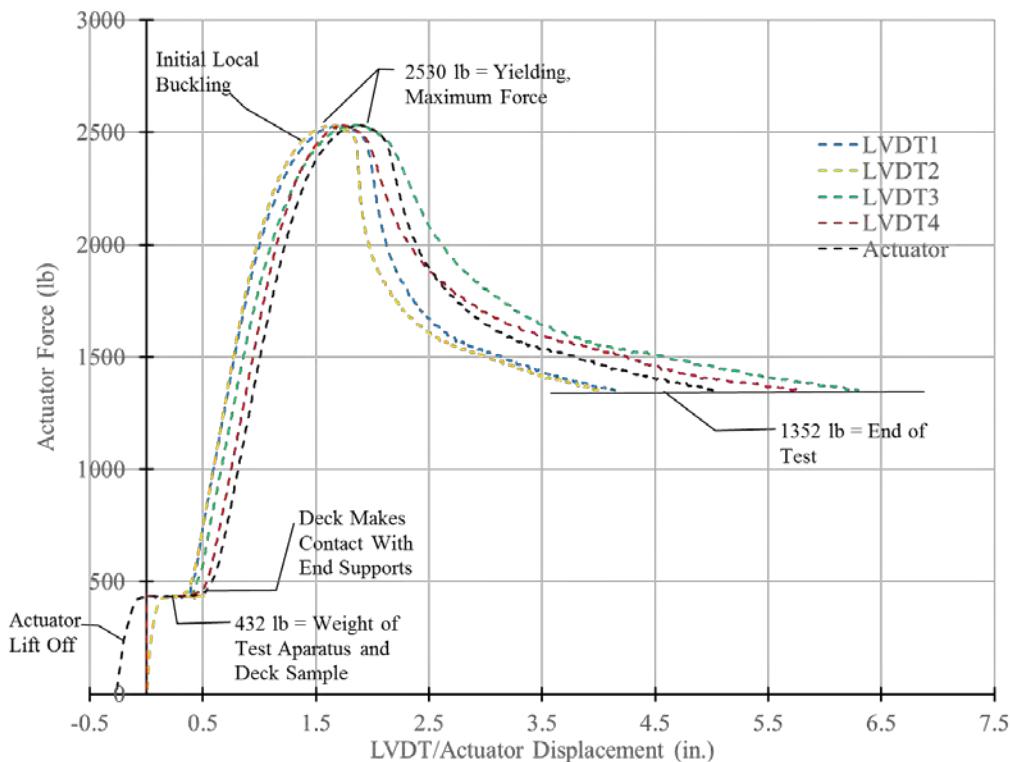


Figure 58: Results for Test 20-POS-03172017-04.

Figure 59 shows each of the 20 gage positive tests overlaid on one another. As with the tests of other gages, the 20 gage positive bending tests show consistent data.

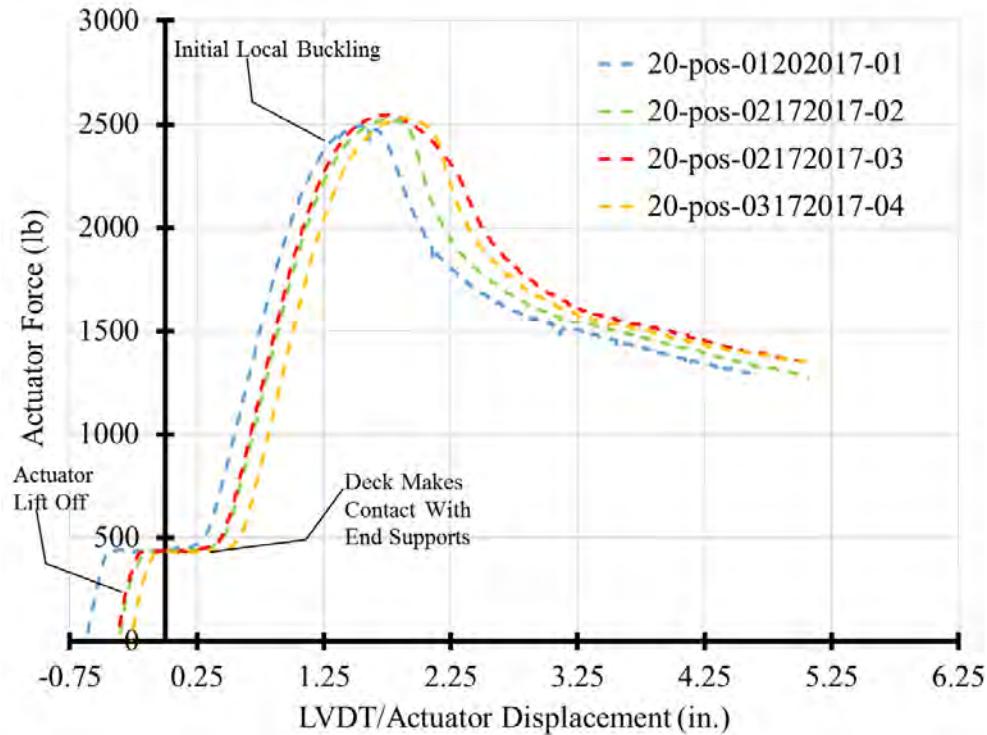


Figure 59: Overlay of 20 Gage Positive Test Results.

Figure 60 is a photograph of 20 gage deck in positive bending showing the early signs of local buckling. Notice the ripples in the ribs between the load points. This photograph was taken near the point of highest applied load during a test.



Figure 60: 20 Gage Deck Positive Bending - Initial Buckling.

Figure 61 is a photograph of 20 gage deck in positive bending with further local buckling. This would be typically seen just after maximum load.



Figure 61: 20 Gage Deck Positive Bending - Further Buckling.

Figure 62 is a photograph of 20 gage deck in positive bending nearing the end of the test with significant local buckling.



Figure 62: 20 Gage Deck Positive Bending - Final State.

Figures 63, 64 and 65 show the results for the 22 gage roof deck tests for negative bending

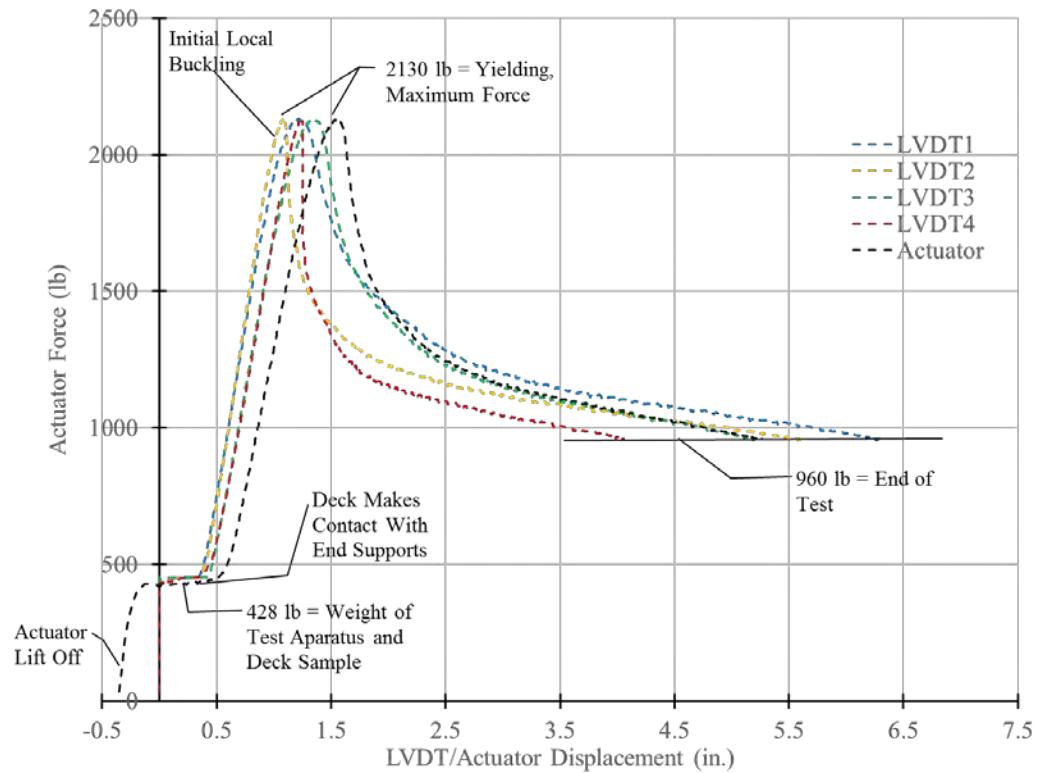


Figure 63: Results for Test 22-NEG-02172017-01.

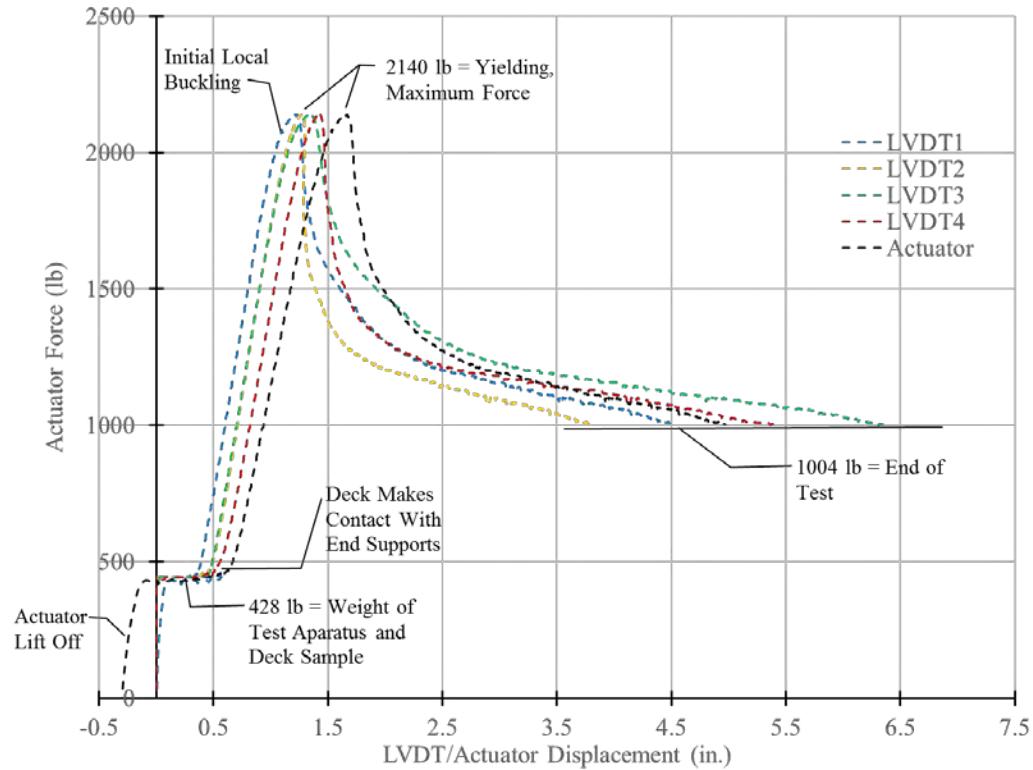


Figure 64: Results for Test 22-NEG-02222017-02.

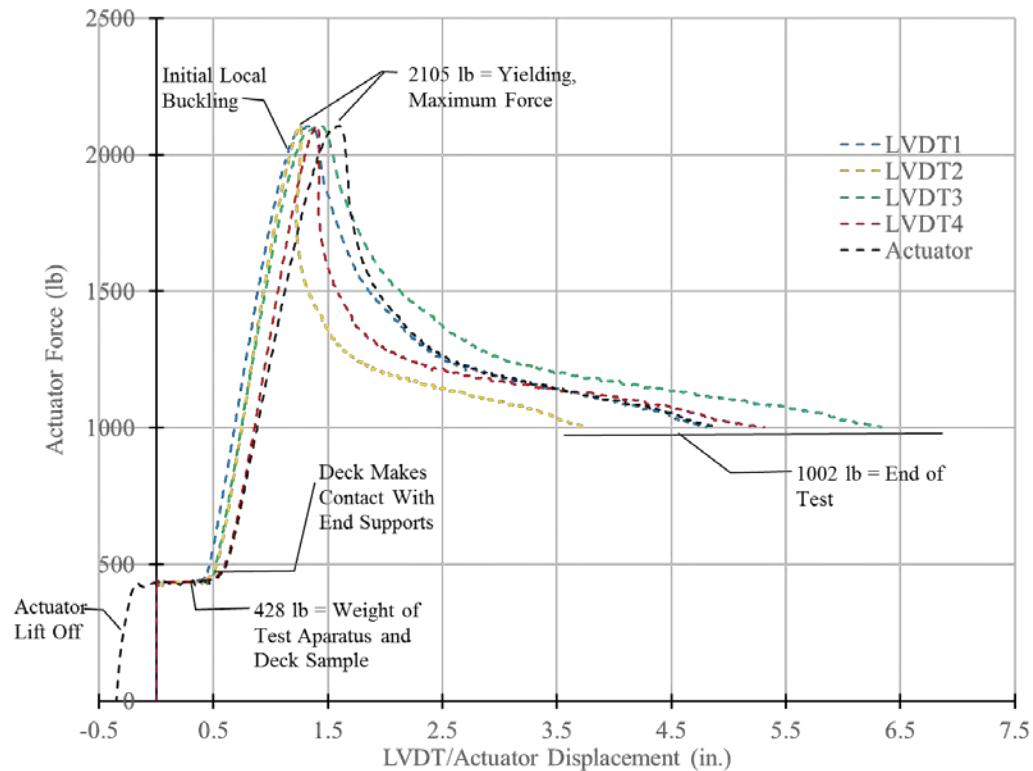


Figure 65: Results for Test 22-NEG-02222017-03.

Figure 66 shows each of the three 22 gage negative tests overlaid on one another. As with other sets of tests, results are very consistent.

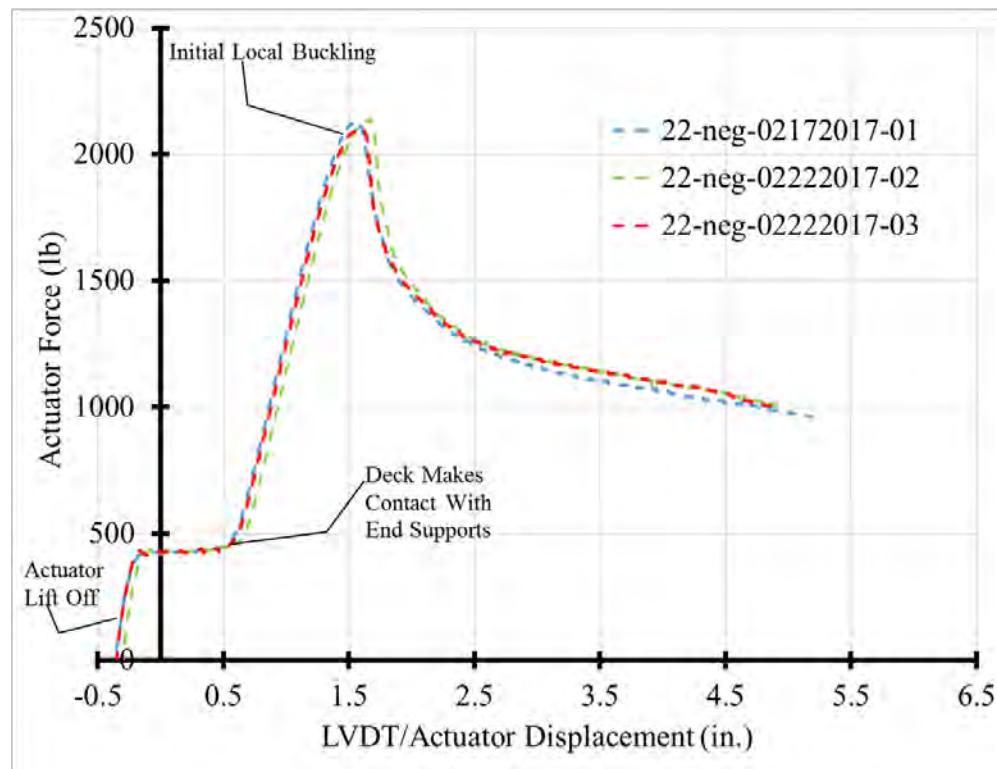


Figure 66: Overlay of 22 Gage Negative Test Results.

Figure 67 is a photograph of 22 gage deck in negative bending in the early stages of local buckling. Notice the webs and ribs buckling near the application of load as well as the exterior web starting to buckle outward.



Figure 67: 22 Gage Deck Negative Bending - Initial Buckling.

Figure 68 is a photograph of 22 gage deck in negative bending in the test frame in its final state. Notice the severe buckling of the exterior unsupported web.



Figure 68: 22 Gage Deck Negative Bending - Final State.

Figure 69 shows the first 22 gage steel roof deck test results for positive bending. This test had an issue with LVDT 3 and the signal conditioner reported fuzzy data. However, the maximum force at yielding is still useful as the load sensor was still reporting the data accurately. These data were still used in the average yielding force to compare with the analytical values.

Figures 70 through 72 show load versus displacement plots for 22 gage roof deck in positive bending. Four tests were conducted with 22 gage deck to ensure enough tests were conducted after the first test returned questionable data for LVDT 3.

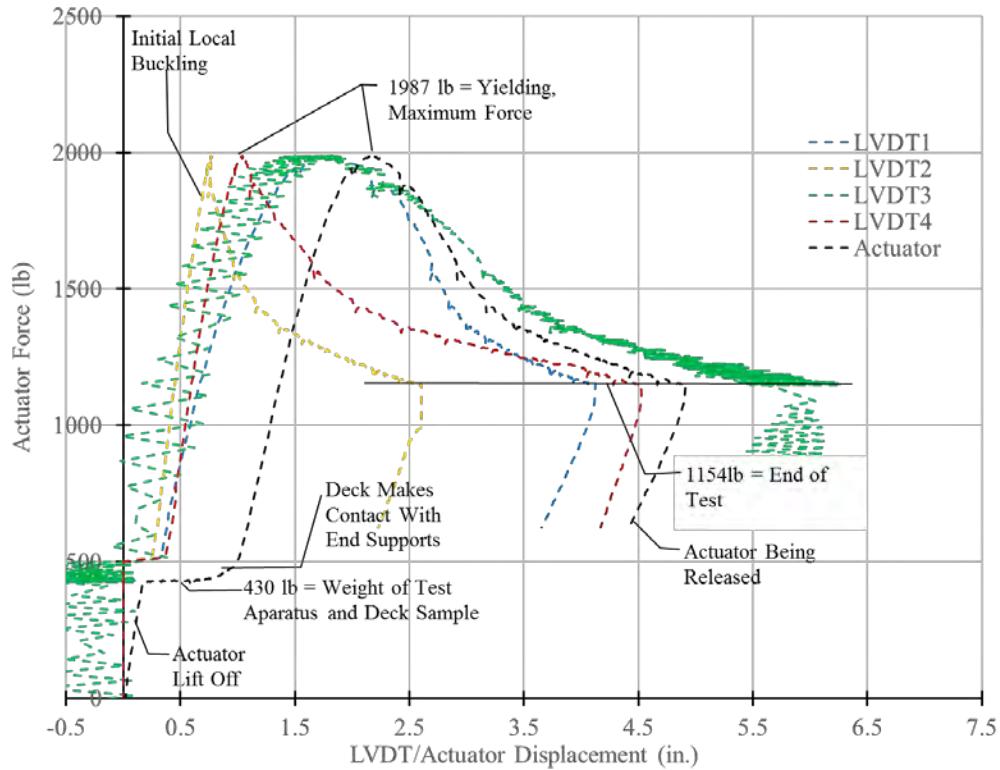


Figure 69: Results for Test 22-POS-01202017-01.

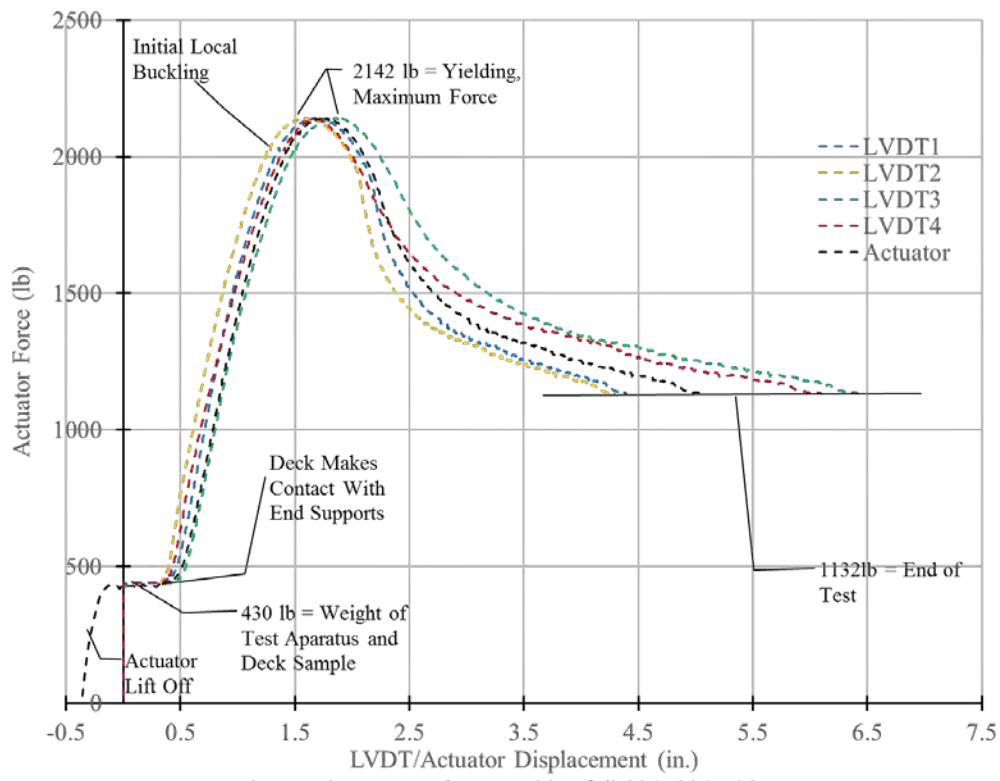


Figure 70: Results for Test 22-POS-02172017-02.

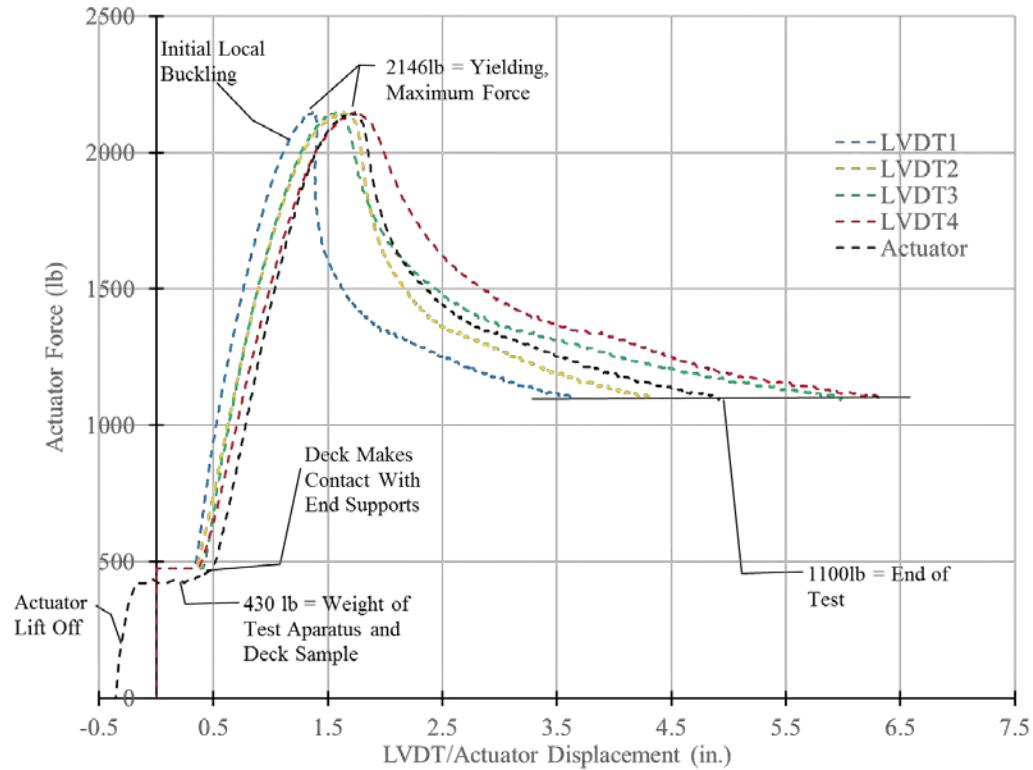


Figure 71: Results for Test 22-POS-02172017-03.

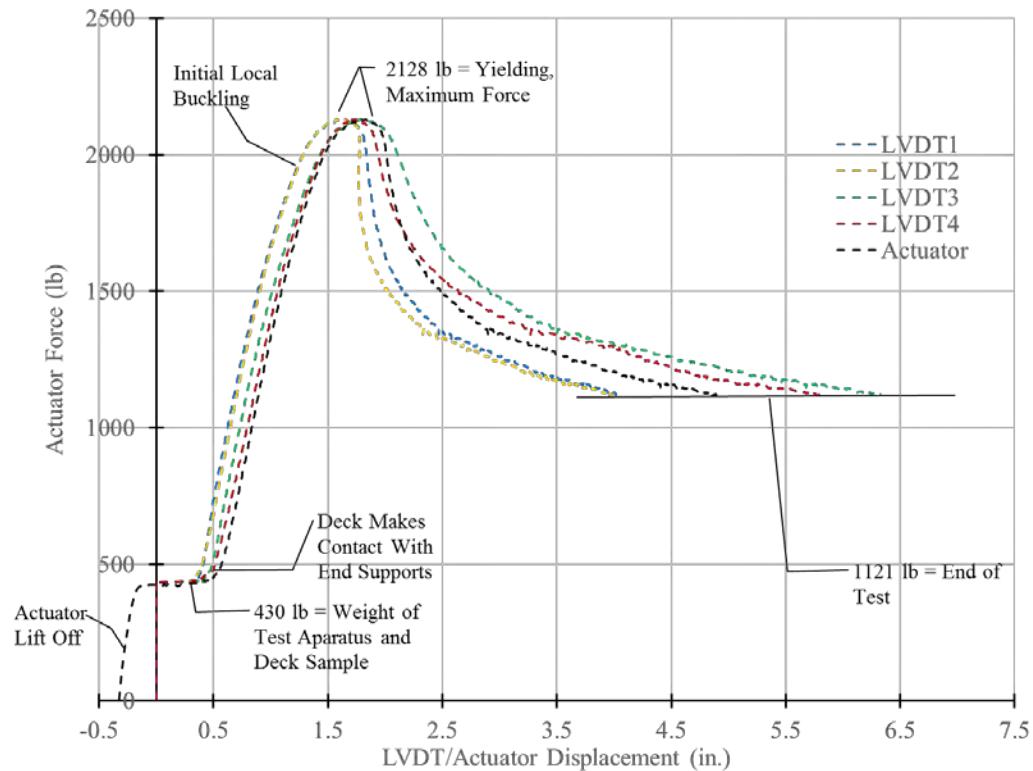


Figure 72: Results for Test 22-POS-03172017-04.

Figure 73 shows each of the 22 gage positive tests overlaid on one another. Tests 02, 03 and 04 are very consistent, but test 01 shows a lower maximum force and a somewhat shifted force versus displacement trace. However, the general trend is similar to the other tests.

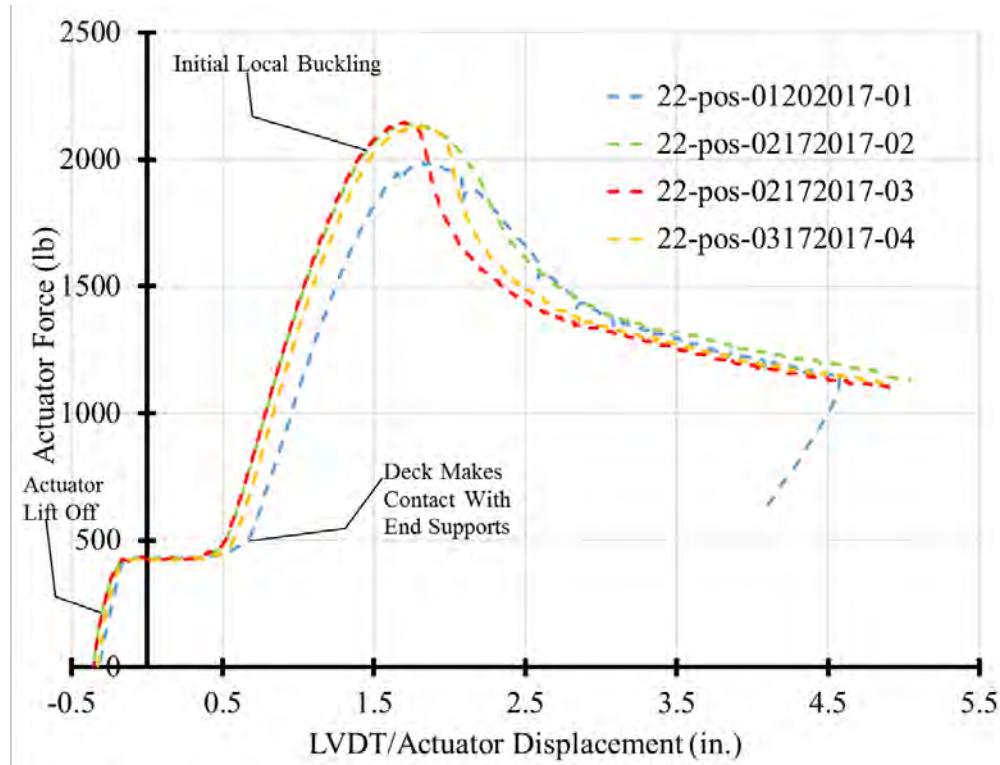


Figure 73: Overlay of 22 Gage Positive Test Results.

Figure 74 is a photograph of 22 gage deck in positive bending showing the signs of initial local buckling. Notice the bottom ribs buckling in the constant moment region between the load points. This photograph was taken just before maximum applied load was reached.



Figure 74: 22 Gage Deck Positive Bending - Initial Buckling.

Figure 75 is a photograph of 22 gage deck in positive bending showing more pronounced local buckling in the webs and ribs.



Figure 75: 22 Gage Deck Positive Bending - Further Buckling.

Figure 76 is a photograph of 22 gage deck in positive bending after being removed from the test frame and in its final state.



Figure 76: 22 Gage Deck Positive Bending - Final State.

3.1.2 Summary of Key Data Points

Several key points were extracted from the data and summarized in Table 20.

Note that even though test 01 was reported for both the 22 gage and 20 gage deck under positive bending, these data were not used in calculating the maximum moment capacity because of the LVDT malfunction mentioned previously.

Table 20: Summary of Key Data Points.

Deck	Orientation	DL (lb)*	T1 Yield (lb)	T2 Yield (lb)	T3 Yield (lb)	T4 Yield (lb)
1.5WR22	Positive	430	1987	2142	2146	2128
1.5WR20	Positive	432	2498	2526	2545	2530
1.5WR18	Positive	454	3699	3690	3720	-
1.5WR16	Positive	464	4915	4914	4901	-
1.5WR22	Negative	428	2130	2140	2105	-
1.5WR20	Negative	434	2543	2530	2562	-
1.5WR18	Negative	448	3828	3700	3845	-
1.5WR16	Negative	459	4938	5052	5049	-

*DL is the weight of the test frame pieces, deck and actuator clevis

The test data were averaged and used for comparison to the EWM results and the DSM results. Table 21 summarizes the average nominal moment capacity as well as the corresponding load applied to produce that moment magnitude.

Table 21: Average Nominal Moment Capacity.

Deck	Orientation	Ave. Yield (lb)	Applied Load Ave. (lb)	Applied Mn (kip-in.)
1.5WR22	Positive	2101	1671	22.56
1.5WR20	Positive	2525	2093	28.26
1.5WR18	Positive	3703	3249	43.86
1.5WR16	Positive	4910	4446	60.02
1.5WR22	Negative	2125	1697	22.91
1.5WR20	Negative	2545	2111	28.50
1.5WR18	Negative	3791	3343	45.13
1.5WR16	Negative	5013	4554	61.48

3.2 Discussion

3.2.1 Comparison of Effective Width Method Results and Experimental Results

Figure 77 illustrates the average nominal moment capacities as determined from test data as compared to the nominal moment capacity and calculated using the Effective Width Method.

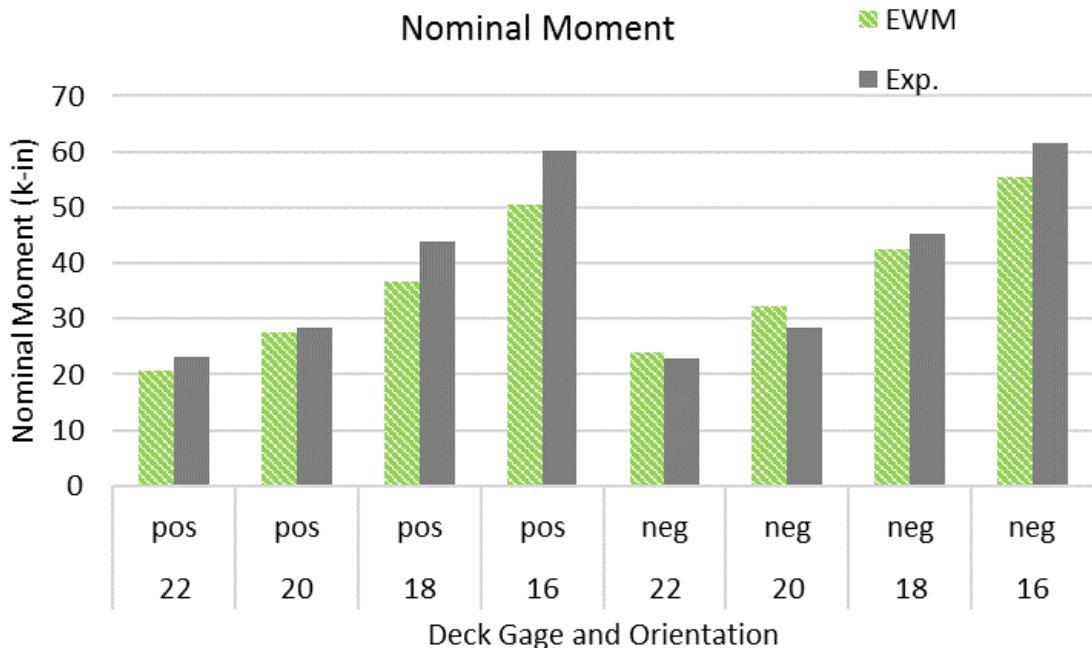


Figure 77: EWM Nominal Moment versus Experimental Nominal Moment.

The EWM results compare well with the experimental results. For positive bending, as the deck thickness increases, the nominal moment magnitude that the EWM predicts separates from the magnitude calculated using experimental results. For negative bending, the EWM over predicted nominal moment capacity for both the 22 gage and 20 gage decks, but underestimated the moment capacity for the heavier decks. The underestimation is less than what was observed with the positive bending results. It is possible that, as the thinner deck started to buckle locally when in the negative bending position, the effective section decreased leading to a lower effective section in the experiment, thus leading to a lower nominal moment. The EWM assumes the effective section remains the same throughout the test up to the point of first failure, thus it may not completely capture this behavior as observed in the experimental tests. Furthermore, the possibility of the section flattening out due to the effects of buckling could be

considered as a mechanism for reducing the depth of the section, resulting in a lower maximum moment capacity than reported using the EWM.

The typical installation method for these steel roof decks differs from that in the experimental setup. Typical installation includes panels laying side by side and usually being attached along their length, known as “sidelap” connections. Without the sidelap connections, the steel roof deck in the laboratory experiments was free to deform at its sides. This may have contributed to a “flattening” effect and a reduction in the effective section modulus, whereas the typical in situ installation would restrain such movement.

3.2.2 Comparison of Direct Strength Method Results and Experimental Results

Figure 78 compares the average nominal moment capacities as calculated using the DSM against the nominal moment capacities as calculated using experimental results.

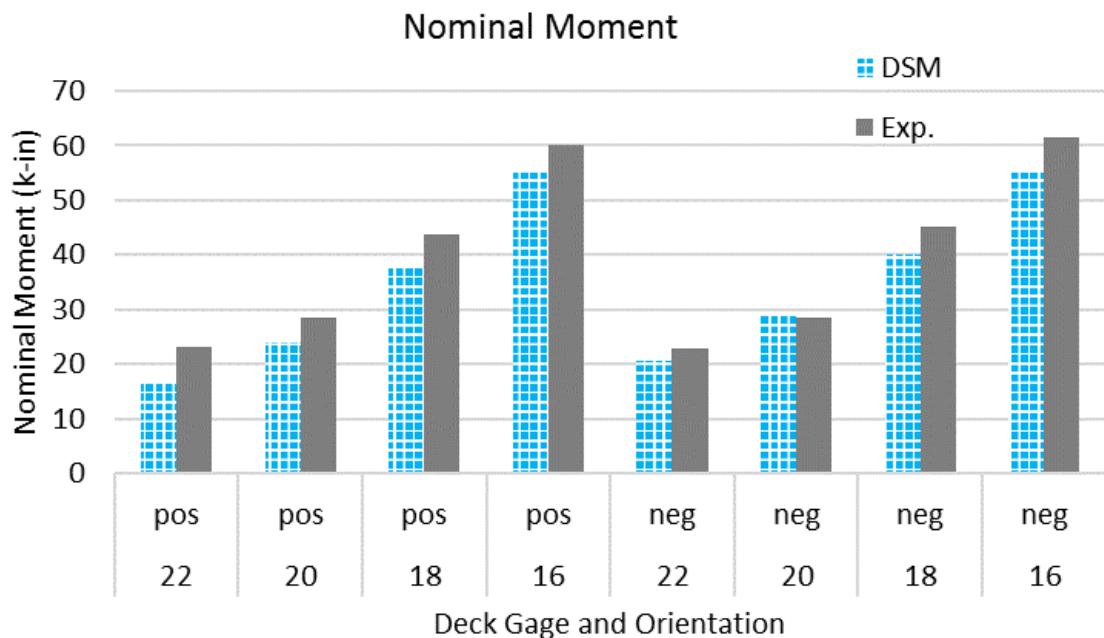


Figure 78: DSM Nominal Moment versus Experimental Nominal Moment.

Similar to that of the EWM, the results under predicted the nominal moment capacity as compared to the experimental nominal moment capacity. One observation is that the difference between the DSM and experimental value stays more consistent as deck thickness increases. The DSM results for 20 gage deck in negative bending slightly overestimated the moment capacity as compared to the experimental. Similar reasoning as that used in the EWM comparison section can be made.

Figure 79 compares the nominal moment capacities using the EWM, DSM and the experimental results.

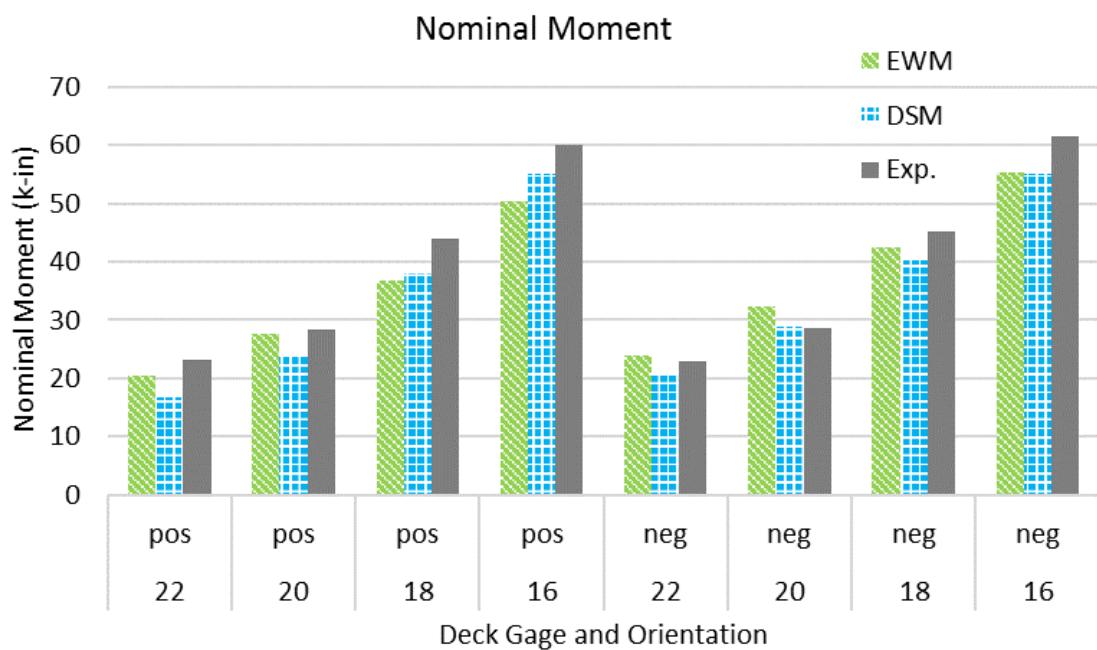


Figure 79: Nominal Moment Capacities: EWM versus DSM versus Experimental.

Table 22 compares the nominal moment capacities as calculated using the EWM, the DSM and experimental data. Also included in this table is the theoretical yield moment as calculated using basic mechanics. The yield moment is calculated using the

average yield stress from Table 10 multiplied by the section modulus published by CANAM [7] for a three-foot wide deck specimen. An excerpt from the CANAM steel roof deck table is included in Appendix C. For example, a 16 gage deck specimen in positive bending has a yield moment calculated as

$$M_y = S_p F_y = (0.41 \text{ in.}^3/\text{ft})(3 \text{ ft})(44.7 \text{ ksi}) = 54.98 \text{ kip-in.} \quad (15)$$

The percent differences calculated use the experimental magnitude as a basis.

Table 22: Summary of Nominal Moment Results (Experimental as Base Value).

Deck	Exp Mn (kip-in.)	EWM Mn (kip-in.)	SR	DSM Mn (kip-in.)	SR	Yield My (kip-in.)	SR
1.5WR22 (Pos)	22.56	20.53	0.91	16.67	0.74	25.37	1.12
1.5WR20 (Pos)	28.26	27.66	0.98	23.98	0.85	34.02	1.20
1.5WR18 (Pos)	43.86	36.81	0.84	37.93	0.86	41.71	0.95
1.5WR16 (Pos)	60.02	50.38	0.84	54.98	0.92	54.98	0.92
1.5WR22 (Neg)	22.91	23.96	1.05	20.53	0.90	25.37	1.11
1.5WR20 (Neg)	28.50	32.29	1.13	28.91	1.01	34.02	1.19
1.5WR18 (Neg)	45.13	42.53	0.94	40.22	0.89	41.71	0.92
1.5WR16 (Neg)	61.48	55.41	0.90	54.98	0.89	54.98	0.89

A trend between the DSM and the EWM was noticed that is consistent with Dudenbostel's study [1]. For positive bending, the EWM results are higher than the DSM for the thinner gage decks (22, 20 gage). As the deck thickness increases, the DSM magnitudes surpass the EWM (18, 16 gage). However, for negative bending, the DSM always results in lower magnitudes than the EWM.

Chapter 4: Conclusions and Recommendations

4.0 Conclusions

4.0.1 Effective Width Method Conclusions

The Effective Width Method was observed to provide more comparable results to the experimental data than the Direct Strength Method for the thinner gage decks, but that observation was not completely consistent. For the 20 gage specimen in its negative bending position, the EWM overestimated the strength by approximately 13%.

An observation was made regarding the computation time necessary to produce EWM results. One must investigate each unique element of a given shape's cross-section. One must also consider the geometric properties of the element and an effective width for that element is calculated given an assumed centroidal location. Furthermore, this is an iterative process so multiple iterations are necessary in a software program to generate a solution that converges.

4.0.2 Direct Strength Conclusion

The Direct Strength Method was observed as typically under predicting the capacity of the thinner decks as compared to the effective width method. In one case (20 gage, negative bending) the DSM resulted in a nominal moment capacity slightly (1%) larger than experimental results. Although it is true that the EWM compared well to the results of 22 and 20 gage decks in positive bending, the DSM shows reasonable and typically conservative results as compared to all experimental results.

A benefit observed in the DSM is the ease of using the CUFSM program and coming up with capacities for a given cross-section with all failure modes (local, distortional and global buckling) assessed and a graphical read-out of the first failure.

Some computational effort is also necessary using the DSM, and development of the point-based model for analysis by the program. However, once the user had a shape drawn in the program, adjusting the thickness was a simple input change. Multiple shapes could be run in a short amount of time.

4.1 Recommendations

4.1.1 Analysis Method

The analysis of steel roof deck without stiffeners is one where different methods may be necessary to produce an accurate solution. To that end, the EWM is most appropriate for analyzing thinner roof deck (e.g., 20 or 22 gage). The DSM is more suitable to thicker roof decks, but is suitable to evaluate all gages and bending positions examined in this study. Thus, the general recommendation resulting from this study is for the Direct Strength Method to be the preferred method when evaluating flexural strength of cold-formed metal deck.

4.2 Suggestions for Future Research

Further research is necessary. An obvious next step is to study steel floor deck with stiffeners in the flanges of the deck. The impact of these stiffeners would be interesting to observe in the lab in full scale testing and comparing the results to both the EWM and the DSM. Additional tests could be run where the loading is altered with a single line load perpendicular to the span of the deck sample instead of a constant moment region. Also, tests could then include a uniform pressure applied to the deck sample as opposed to a line load. Both of these could be run in the laboratory with full scale specimens and observations and data collected could be compared to the EWM and

the DSM results. These tests could prove valuable as a constant moment region is not as common as a uniform pressure or point load on a roof deck.

References

- [1] Dudenbostel, Randall. 2015. *Direct Strength Method For Steel Deck*. Master's thesis, University of Florida, Gainesville.
- [2] Li, Z and Schafer, B. "Buckling Analysis of Cold-Formed Steel Members with General Boundary Conditions using CUFSM: Conventional and Constrained Finite Strip Methods." In American Iron and Steel Institute *et al.* 3-4 November 2010. *Twentieth International Specialty Conference on Cold-Formed Steel Structures -- Recent Research and Developments in Cold-Formed Steel Design and Construction*. University of Missouri-Rolla, pp. 17-31.
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- [4] Schafer, B W and Adany, S. "Buckling Analysis of Cold-Formed Steel Members Using CUFSM: Conventional and Constrained Finite Strip Methods." In *Eighteenth International Specialty Conference on Cold-Formed Steel Structures: Recent Research and Developments in Cold-Formed Steel Design and Construction*, 26-27 October 2006. University of Missouri-Rolla, pp. 39-54.
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- [7] CANAM Solutions + Service. 2010. *Steel Deck Manual*. Point of Rocks, MD: CANAM. *1.5 Type B Roof Deck Data Base*. [Internet, WWW, PDF].
ADDRESS: <https://www.canam-construction.com/wp-content/uploads/2014/11/canam-steel-deck.pdf>

Appendix A: Hand Calculations

A.1 Effective Width Method

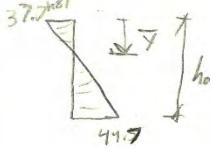
			<p>Example Calc. Positive bending - 16 Ga.</p> <p>Yield: 44.7 ksi</p> <p>Thickness: 0.0598 in. = t</p> <p>Total height: 1.54 in. = h_0</p> <p>Radius 0.2179</p> <p>$\theta = 72.5^\circ$</p> <p>$\phi = 1.36536 \text{ radians}$</p> <p>Assume $\bar{y} = 0.696681 \text{ in}$ From Top of Deck</p> <p>Tension Controlled</p> <p>$f_t = 44.7 \text{ ksi}$</p>  <p>$\frac{(h_0 - \bar{y})}{44.5} = \text{slope} = 0.018481$</p> <p>$\bar{y}/\text{slope} = f_c = \frac{0.696681}{0.018481} = 37.7 \text{ ksi}$</p> <p><u>Effective Width Top Flange</u></p> <p>$w = 3.1644 \text{ in.}$</p> <p>$\lambda = \sqrt{\frac{f_t}{F_{cr}}} = \dots$</p> <p>$F_{cr} = \frac{k \pi^2 E}{12(1-\mu^2)} \left(\frac{t}{w}\right)^2$</p> <p>$\mu = 0.28 \text{ (from testing)}$</p> <p>$E = 29000 \text{ ksi}$</p> <p>$k = 4$</p> <p>$F_{cr} = 36.97$</p>	1
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Figure A1: 16 Gage EWM Example Calculations.

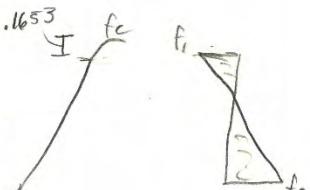
			2
	Since $\lambda > 0.673$		
	$b = \rho w$	$\rho = (1 - 0.022/\lambda)/2$	
	$b = 0.77(3.1644)$	$\rho = 0.77$	
	<u>$b = 2.45 \text{ in}$</u>		
	Effective width web.		
	$w = 1.1825 \text{ in}$		
	$\lambda = \sqrt{\frac{F_{cr}}{F_{cr}}}$	$f_1 = \frac{(Y - 1653)}{\text{slope}}$ $f_1 = 30.6933 \text{ ksi}$	
	$\lambda = 0.14$	$F_{cr} = \frac{k \cdot \gamma^2 E}{12(1 - \mu^2)} \left(\frac{t}{w}\right)^2$	
	$b_e = w$	$k = Y + 2(1 + \gamma)^3 + 2(1 + \gamma)$	
	Since $\lambda \leq 0.673$	$\gamma = f_a/f_i$	
	$\frac{h_o}{b_o} \leq 4$	$\gamma = 1.19$	$f_2 = \frac{(h_o - Y - 1653)}{\text{slope}}$
	$\Rightarrow \frac{3.1644}{1.54} = 2.05$	$k = 29.26$	
		$F_{cr} = 19.20 \text{ ksi}$	
	$b_1 = b_e/(3 + \gamma)$		
	$b_2 = b_e/2 \quad (\gamma > 0.236)$		
	$b_1 = 0.28$	$> 0.87 > Y \therefore \text{full section}$	
	$b_2 = 0.59$	effective	

Figure A2: 16 Gage EWM Example Calculations.

3

Effective Width bottom Flange

$$w = 1.6354h$$

Effective width Corners

$$w = 0.04388 = \frac{\phi}{(2\pi)} \times \text{Radius}$$

Eff. width unshnt up @ bott flg.

same as top flg. but $k=0.43$

$$w = 0.5522$$

$$b = 0.5522 \quad b/c \quad x = 0.537$$

Eff. width unshnt web. (part)

$$w = 0.5 \quad k = 0.43$$

$$b = 0.5 \quad \text{same as top flg.}$$

$$x = 0.48$$

Element	$L_{(in)}$	γ_{top}	Quantity
-In Excel		$b/10$	0.09

solve so $\frac{\sum L_y}{\sum L} = \bar{Y}$

-then reduce areas as necessary.

-put into autocad, region, massprop.

Figure A3: 16 Gage EWM Example Calculations.

Deck	1.5B	pos bend	Tension Controlled			Tension Controlled			Comp Controlled		
Gage	16	GA				y bar	0.696681	in			
Yield	44.7	ksi				fc	37.69636				
Thickness	0.0598	in				ft	44.7				
Total Height	1.54	in				slope	0.018481				
Radius	0.2179	in				Element	L (in)	y from top (in.)	Quantity	ΣL	ΣLy
θ	72.5	degrees				Lip	0.5522	1.5101	1	0.5522	0.833877
θ	1.265363708	radian				T, Corners	0.043883	0.0878	12	0.526592	0.046235
Curve l'x	0.000592	in^3				B, Corners	0.043883	1.4522	13	0.570474	0.828443
						Top Flg.	2.451019	0.0299	6	14.70612	0.439713
						Web, b1	0	0	12	0	0
						Web, b2	0	0	12	0	0
						Lip up	0.5	1.136270762	1	0.5	0.568135
						Web, Ten	0	0	12	0	0
						Web	1.1875	0.77	12	14.25	10.9725
						Bot. Flg.	1.6354	1.5101	6	9.8124	14.81771
										40.91778	28.50661
											33.95011
E	29000	ksi									
μ	0.28	-									
t	0.0598	in									
Fcr	36.97035653	ksi									

Effective Width Web	
w	1.1875 in
be	1.1875
λ	0.14010535
p	-4.07012977
f1	37.69330737
f2	44.69694503
k	29.25806784 -
E	29000 ksi
μ	0.28 -
t	0.0598 in
Fcr	1920.236874 ksi
Ψ	1.185805867
b1	0.283696865
b2	0.59375
w in comp	0.557168384
Check	0.877446865
ho/bo	2.054805195 -

Effective Width Bottom Flange	
w	1.6354 in

Effective Width Corners	
w	0.043882639 in

Effective Width Unstiff. Lip Horiz.		Effective Width Unstiff. Lip Vert.	
w	0.5522 in	w	0.5 in
b	0.5522	b	0.5
λ	0.537432216	λ	0.486628
p	1.09901497	p	1.12593
f	37.69636234	f	37.69636
k	0.43 -	k	0.43 -
E	29000 ksi	E	29000 ksi
μ	0.28 -	μ	0.28 -
t	0.0598 in	t	0.0598 in
Fcr	130.5124824 ksi	Fcr	159.186 ksi

Figure A4: 16 Gage Positive EWM Example Calculation.

Deck	1.5B	pos bend	Tension Controlled			Tension Controlled			Comp Controlled		
Gage	18	GA				y bar	0.731233	in	y bar	0.731233	in
Yield	43.45	ksi				fc	35.14091		fc	43.45	
Thickness	0.0474	in				ft	43.45		ft	48.05704	
Total Height	1.54	in				slope	0.020809		slope	0.016829	
Radius	0.2179	in	Element	L (in)	y from top (in.)	Quantity	ΣL	ΣLy	ΣLy^2		
θ	72.5	degrees	Lip	0.5522	1.5163	1	0.5522	0.837301	1.269599		
θ	1.265363708	radian	T, Corners	0.043883	0.0878	12	0.526592	0.046235	0.004059		
Curve I'x	0.000592	in^3	B, Corners	0.043883	1.4522	13	0.570474	0.828443	1.203065		
			Top Flg.	2.112538	0.0237	6	12.67523	0.300403	0.00712		
Effective Width Top Flange			Web, b1	0	0	12	0	0	0		
w	3.1644		Web, b2	0	0	12	0	0	0		
b	2.112538049		Lip up	0.5	1.136270762	1	0.5	0.568135	0.645556		
λ	1.229992711	1.051862	Web, Ten	0	0	12	0	0	0		
ρ	0.667595136	0.525931	Web	1.1875	0.77	12	14.25	10.9725	8.448825		
f	35.14091212		Bot. Flg.	1.6354	1.5163	6	9.8124	14.87854	22.56033		
k	4	-					38.88689	28.43156	34.13856		
E	29000	ksi									
μ	0.28	-									
t	0.0474	in									
Fcr	23.22779338	ksi									
Effective Width Web											
w	1.1875	in									
be	1.1875										
λ	0.461555069										
ρ	1.13388525										
f1	35.13747246										
f2	43.44656034										
k	4	-									
E	29000	ksi									
μ	0.28	-									
t	0.0474	in									
Fcr	164.9390426	ksi									
ψ	1.236473693										
b1	0.280303877										
b2	0.59375										
w in comp	0.593397572										
Check	0.874053877										
Effective Width Bottom Flange											
w	1.6354	in									
Effective Width Corners											
w	0.043882639	in									
Effective Width Unstiff. Lip											
w	0.5522	in									
b	0.5522										
λ	0.654641197										
ρ	1.014201442										
f	35.14091212										
k	0.43	-									
E	29000	ksi									
μ	0.28	-									
t	0.0474	in									
Fcr	81.9985864	ksi									
Effective Width Unstiff. Lip											
w	0.5	in									
b	0.5										
λ	0.592757										
ρ	1.060895										
f	35.14091										
k	0.43	-									
E	29000	ksi									
μ	0.28	-									
t	0.0474	in									
Fcr	100.0136	ksi									

Figure A5: 18 Gage Positive EWM Example Calculation.

Deck	1.5B	pos bend	Tension Controlled			Tension Controlled			Comp Controlled		
Gage	20	GA				y bar	0.781893	in			
Yield	47.25	ksi				fc	35.82056				
Thickness	0.0358	in				ft	47.25				
Total Height	1.54	in				slope	0.021828				
Radius	0.2179	in									
θ	72.5	degrees									
θ	1.265363708	radian									
Curve l'x	0.000592	in ³									
Effective Width Top Flange											
w	3.1644										
b	1.667057613										
λ	1.644211016	1.497342									
ρ	0.526816336	0.748671									
f	35.82056497										
k	4	-									
E	29000	ksi									
μ	0.28	-									
t	0.0358	in									
Fcr	13.25004411	ksi									

Effective Width Web	
w	1.1875 in
be	1.1875
λ	0.616989711
ρ	1.042853751
f1	35.81695679
f2	47.24639182
k	4 -
E	29000 ksi
μ	0.28 -
t	0.0358 in
Fcr	94.08769718 ksi
ψ	1.319106816
b1	0.274941105
b2	0.59375
w in comp	0.646515514
Check	0.868691105
Effective Width Bottom Flange	
w	1.6354 in
Effective Width Corners	
w	0.043882639 in

Effective Width Unstiff. Lip		Effective Width Unstiff. Lip			
w	0.5522 in	0.079824	w	0.5 in	0.044185
b	0.472376401		b	0.455815	
λ	0.875101338		λ	0.792377	
ρ	0.855444406		ρ	0.91163	
f	35.82056497		f	35.82056	
k	0.43 -		k	0.43 -	
E	29000 ksi		E	29000 ksi	
μ	0.28 -		μ	0.28 -	
t	0.0358 in		t	0.0358 in	
Fcr	46.77520886 ksi		Fcr	57.05169 ksi	

Figure A6: 20 Gage Positive EWM Example Calculation.

Deck	1.5B	pos bend	Tension Controlled			Tension Controlled			Comp Controlled		
Gage	22	GA				y bar	0.807177	in	y bar	0.807177	in
Yield	44.5	ksi				fc	32.61064		fc	44.5	
Thickness	0.0295	in				ft	44.5		ft	40.40087	
Total Height	1.54	in				slope	0.024752		slope	0.018139	
Radius	0.2179	in	Element	L (in)	y from top (in.)	Quantity	ΣL	ΣLy	ΣLy^2		
θ	72.5	degrees	Lip	0.42664	1.52525	1	0.42664	0.650733	0.99253		
θ	1.265363708	radian	T, Corners	0.043883	0.0878	12	0.526592	0.046235	0.004059		
Curve I'x	0.000592	in^3	B, Corners	0.043883	1.4522	13	0.570474	0.828443	1.203065		
Effective Width Top Flange			Top Flg.	1.470043	0.01475	6	8.820256	0.130099	0.001919		
w	3.1644		Web, b1	0	0	12	0	0	0		
b	1.47004269		Web, b2	0	0	12	0	0	0		
λ	1.903846842	1.694357	Lip up	0.414288	1.177143488	1	0.414288	0.487676	0.574064		
ρ	0.464556532	0.847179	Web, Ten	0	0	12	0	0	0		
f	32.61063973		Web	1.1875	0.77	12	14.25	10.9725	8.448825		
k	4	-	Bot. Flg.	1.6354	1.52525	6	9.8124	14.96636	22.82745		
E	29000	ksi					34.82065	28.08205	34.05191		
μ	0.28	-									
t	0.0295	in									
Fcr	8.996949914	ksi									
Effective Width Web											
w	1.1875	in									
be	1.150339688										
λ	0.714409143										
ρ	0.968707106										
f1	32.60654823										
f2	44.4959085										
k	4	-									
E	29000	ksi									
μ	0.28	-									
t	0.0295	in									
Fcr	63.88675328	ksi									
ψ	1.364631061										
b1	0.263559433										
b2	0.575169844										
w in comp	0.673026347										
Check	0.838729277										
Effective Width Bottom Flange											
w	1.6354	in									
Effective Width Corners											
w	0.043882639	in									
Effective Width Unstiff. Lip						Effective Width Unstiff. Lip					
w	0.5522	in	0.12556	w	0.5	in	0.085712				
b	0.426639988			b	0.414288						
λ	1.013287773			λ	0.917501						
ρ	0.772618595			ρ	0.828575						
f	32.61063973			f	32.61064						
k	0.43	-		k	0.43	-					
E	29000	ksi		E	29000	ksi					
μ	0.28	-		μ	0.28	-					
t	0.0295	in		t	0.0295	in					
Fcr	31.76096682	ksi		Fcr	38.73883	ksi					

Figure A7: 22 Gage Positive EWM Example Calculation.

Deck	1.5B	neg bend	Tension Controlled				Tension Controlled				Comp Controlled			
Gage	16	GA					y bar	0.606023	in		y bar	0.606023	in	
Yield	44.7	ksi					fc	41.74876			fc	44.7		
Thickness	0.0598	in					ft	44.7			ft	68.8897		
Total Height	1.54	in					slope	0.014516			slope	0.013558		
Radius	0.2179	in					Element	L (in)	y from top (in.)	y for neg	Quantity	ΣL	ΣLy	ΣLy^2
θ	72.5	degrees					Lip	0.5522	1.5101	0.0299	1	0.5522	0.016511	1.259238
θ	1.265363708	radian					T, Corners	0.043883	0.0878	1.4522	12	0.526592	0.764716	0.004059
Curve I'x	0.000592	in ³					B, Corners	0.043883	1.4522	0.0878	13	0.570474	0.050088	1.203065
Effective Width Top Flange							Top Flg.	1.6354	0.0299	1.5101	6	9.8124	14.81771	0.008772
w	1.6354						Web, b1	0	0	1.54	12	0	0	0
b	1.6354						Web, b2	0	0	1.54	12	0	0	0
λ	0.549196292	0					Lip up	0.5	1.136270762	0.403729	1	0.5	0.201865	0.645556
ρ	1.091439688	0					Web, Ten	0	0	1.54	12	0	0	0
f	41.74876149						Web	1.1875	0.77	0.77	12	14.25	10.9725	8.448825
k	4	-					Bot. Flg.	3.1644	1.5101	0.0299	6	18.9864	0.567693	43.29662
E	29000	ksi										45.19807	27.39108	54.86614
μ	0.28	-												
t	0.0598	in												
Fcr	138.4166722	ksi												

Effective Width Web	
w	1.1875 in
be	1.1875
λ	0.398772077
ρ	1.124217147
f1	41.746362
f2	44.69760051
k	4 -
E	29000 ksi
μ	0.28 -
t	0.0598 in
Fcr	262.5240852 ksi
ψ	1.070694508
b1	0.291719263
b2	0.59375
w in comp	0.462111146
Check	0.885469263
Effective Width Bottom Flange	
w	3.1644 in
Effective Width Corners	
w	0.043882639 in

Effective Width Unstiff. Lip		Effective Width Unstiff. Lip			
w	0.5522 in	0	w	0.5 in	0
b	0.5522		b	0.5	
λ	0.565582252		λ	0.512117	
ρ	1.080338578		ρ	1.113829	
f	41.74876149		f	41.74876	
k	0.43 -		k	0.43 -	
E	29000 ksi		E	29000 ksi	
μ	0.28 -		μ	0.28 -	
t	0.0598 in		t	0.0598 in	
Fcr	130.5124824 ksi		Fcr	159.186 ksi	

Figure A8: 16 Gage Negative EWM Example Calculation.

Effective Width Web		
w	1.1875	in
be	1.1875	
λ	0.49675572	
p	1.12152989	
f1	40.70138833	
f2	43.44755037	
k	4	-
E	29000	ksi
μ	0.28	-
t	0.0474	in
Fcr	164.9390426	ksi
Ψ	1.067470967	
b1	0.291950455	
b2	0.59375	
w in comp	0.4591515849	
Check	0.885700455	
Effective Width Bottom Flange		
w	3.1644	in
Effective Width Corners		
w	0.043882639	in

Effective Width Unstiff. Lip			Effective Width Unstiff. Lip				
w	0.5522	in	0.013174	w	0.5	in	0
b	0.53902623			b	0.5		
λ	0.704554345			λ	0.637952		
ρ	0.976143119			ρ	1.026952		
f	40.70383796			f	40.70384		
k	0.43	-		k	0.43	-	
E	29000	ksi		E	29000	ksi	
μ	0.28	-		μ	0.28	-	
t	0.0474	in		t	0.0474	in	
Fcr	81.9985864	ksi		Fcr	100.0136	ksi	

Figure A9: 18 Gage Negative EWM Example Calculation.

Deck	1.5B	neg bend	Tension Controlled			Tension Controlled			Comp Controlled		
Gage	20	GA				y bar	0.563185	in	y bar	0.563185	in
Yield	47.25	ksi				fc	46.15451		fc	47.25	
Thickness	0.0358	in				ft	47.25		ft	81.95266	
Total Height	1.54	in				slope	0.012202		slope	0.011919	
Radius	0.2179	in									
θ	72.5	degrees									
θ	1.265363708	radian									
Curve I'x	0.000592	in^3									
Effective Width Top Flange											
w	1.6354										
b	1.308771855										
λ	0.964563946	0.326628									
ρ	0.800276296	0.163314									
f	46.15450929										
k	4	-									
E	29000	ksi									
μ	0.28	-									
t	0.0358	in									
Fcr	49.60804233	ksi									

Effective Width Web	
w	1.1875 in
be	1.1875
λ	0.282304064
ρ	0.78177561
f1	46.15249227
f2	47.24798298
k	24.62 -
E	29000 ksi
μ	0.28 -
t	0.0358 in
Fcr	579.1097761 ksi
ψ	1.023736328
b1	0.295123712
b2	0.59375
w in comp	0.417193999
Check	0.888873712
Effective Width Bottom Flange	
w	3.1644 in
Effective Width Corners	
w	0.043882639 in

Effective Width Unstiff. Lip		Effective Width Unstiff. Lip		
w	0.5522 in	0.119417	w	0.5 in
b	0.432782922		b	0.419929
λ	0.993342921		λ	0.899441
ρ	0.783743067		ρ	0.839859
f	46.15450929		f	46.15451
k	0.43 -		k	0.43 -
E	29000 ksi		E	29000 ksi
μ	0.28 -		μ	0.28 -
t	0.0358 in		t	0.0358 in
Fcr	46.77520886 ksi		Fcr	57.05169 ksi

Figure A10: 20 Gage Negative EWM Example Calculation.

Deck	1.5B	neg bend	Tension Controlled				Tension Controlled		Comp Controlled			
Gage	22	GA			y bar	0.541271	in		y bar	0.541271	in	
Yield	44.5	ksi			fc	44.44344			fc	44.5		
Thickness	0.0295	in			ft	44.5			ft	82.10938		
Total Height	1.54	in			slope	0.012179			slope	0.012163		
Radius	0.2179	in										
θ	72.5	degrees										
θ	1.265363708	radian										
Curve l'x	0.000592	in^3										
Effective Width Top Flange												
w	1.6354											
b	1.151064906											
λ	1.148652806	0.484335										
ρ	0.703843039	0.242168										
f	44.44343556											
k	4	-										
E	29000	ksi										
μ	0.28	-										
t	0.0295	in										
Fcr	33.68449708	ksi										

Effective Width Web		
w	1.1875	in
be	1.048227236	
λ	0.834043239	
ρ	0.882717672	
f1	44.44142239	
f2	44.49798683	
k	4	-
E	29000	ksi
μ	0.28	-
t	0.0295	in
Fcr	63.88675328	ksi
ψ	1.001272786	
b1	0.26197345	
b2	0.524113618	
w in comp	0.39421666	
Check	0.786087068	
Effective Width Bottom Flange		
w	3.1644	in
Effective Width Corners		
w	0.043882639	in

Effective Width Unstiff. Lip		Effective Width Unstiff. Lip				
w	0.5522	in	0.172208			
b	0.379992164		w	0.5	in	0.129072
λ	1.182924304		b	0.370928		
ρ	0.688142275		λ	1.071101		
f	44.44343556		ρ	0.741857		
k	0.43	-	f	44.44344		
E	29000	ksi	k	0.43	-	
μ	0.28	-	E	29000	ksi	
t	0.0295	in	μ	0.28	-	
Fcr	31.76096682	ksi	t	0.0295	in	
			Fcr	38.73883	ksi	

Figure A11: 22 Gage Negative EWM Example Calculation.

From AutoCAD				
Gage	Orientation	Se	Fy	Mn
22	pos	0.4614	44.5	20.5323
20	pos	0.5853	47.25	27.65543
18	pos	0.8471	43.45	36.8065
16	pos	1.1271	44.7	50.38137
22	neg	0.5384	44.5	23.9588
20	neg	0.6834	47.25	32.29065
18	neg	0.9788	43.45	42.52886
16	neg	1.2396	44.7	55.41012

Figure A12: EWM Effective Section Modulus.

A.2 Direct Strength Method

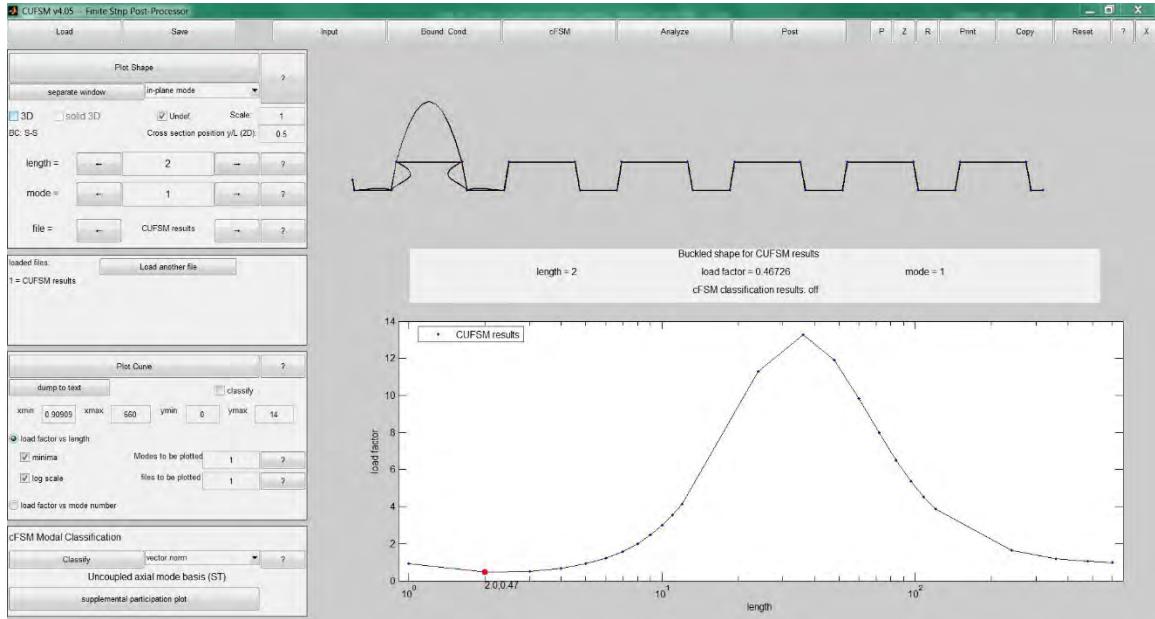


Figure A13: 22 Gage Positive DSM Output.

Section Prop.		Sn used	0.19	My	
Sn	0.57 in^3	Snp	0.19	Positive	25.365
Fy	44.5 ksi	Snn	0.19	Negative	25.365
My	25.365 k-in	Fy flute	47.1		
		Fy flange	41.9		
Local					
		Mcrl/My	0.47	-	
		Mcrl	11.9216	k-in	
Distortional					
		Mcrd/My	11.2779	-	
		Mcrd	286.064	k-in	
LTB					
		Mcrlt/My	11.2779	-	
		Mcrlt	286.064	k-in	
Mne					
		Mne	25.365	k-in	
Local Buck. 1.3.2					
		λ_1	1.45865	-	
		Limit	0.776	-	
		Mnl	16.6734	k-in	
Dist. Buck 1.3.3					
		λ_d	0.29777	-	
		Limit	0.673	-	
		Mnd	25.365	k-in	
Nominal Moment					
		Mn	16.6734	k-in	

Figure A14: 22 Gage Positive DSM Example Calculation.

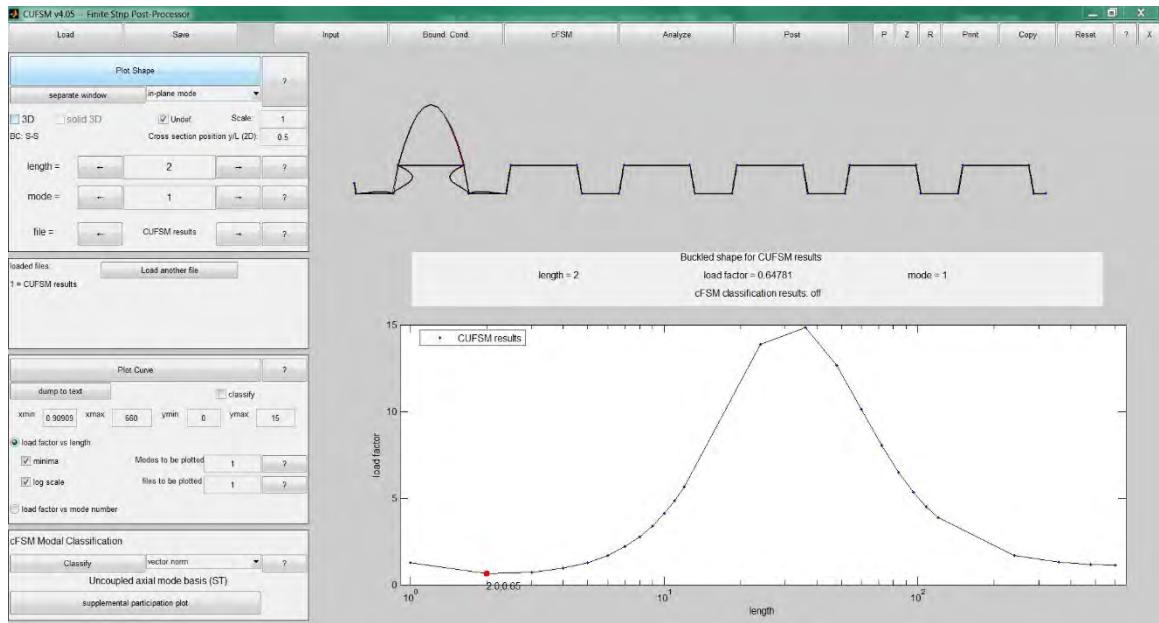


Figure A15: 20 Gage Positive DSM Output.

Section Prop.		Sn used	0.23	My	
Sn	0.69 in^3	Snp	0.23	Positive	32.6025
Fy	47.25 ksi	Snn	0.24	Negative	34.02
My	32.6025 k-in	Fy flute	48.6		
		Fy flange	45.9		
Local					
		Mcrl/My	0.65 -		
		Mcrl	21.19163 k-in		
Distortional					
		Mcrd/My	13.8554 -		
		Mcrd	451.7207 k-in		
LTB					
		Mcrlt/My	13.8554 -		
		Mcrlt	451.7207 k-in		
Mne					
		Mne	32.6025 k-in		
Local Buck. 1.3.2					
		λ_1	1.240347 -		
		Limit	0.776 -		
		Mnl	23.97727 k-in		
Dist. Buck 1.3.3					
		λ_d	0.268652 -		
		Limit	0.673 -		
		Mnd	32.6025 k-in		
Nominal Moment					
		Mn	23.97727 k-in		

Figure A16: 20 Gage Positive DSM Example Calculation.

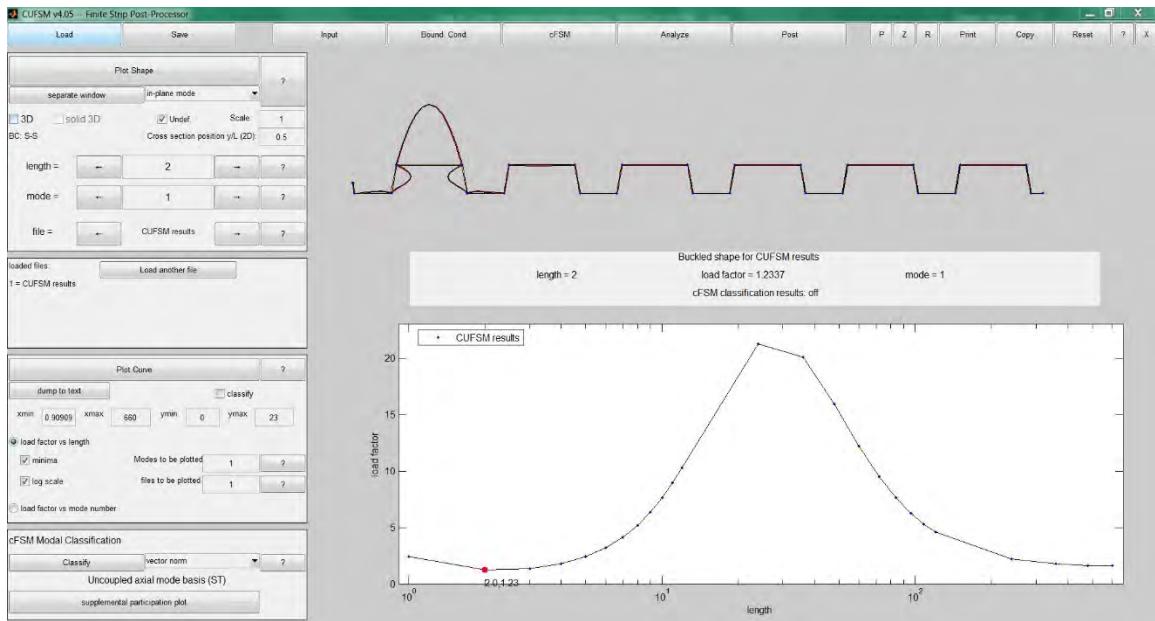


Figure A17: 18 Gage Positive DSM Output.

Section Prop.		Sn used	0.32	My	
Sn	0.96 in ³	Snp	0.32	Positive	41.712
Fy	43.45 ksi	Snn	0.32	Negative	41.712
My	41.712 k-in	Fy flute	42.6		
		Fy flange	44.3		
Local					
		Mcrl/My	1.23	-	
		Mcrl	51.3058	k-in	
Distortional					
		Mcrd/My	21.2747	-	
		Mcrd	887.41	k-in	
LTB					
		Mcrlt/My	21.2747	-	
		Mcrlt	887.41	k-in	
Mne					
		Mne	41.712	k-in	
Local Buck. 1.3.2					
		λ_1	0.90167	-	
		Limit	0.776	-	
		Mnl	37.9293	k-in	
Dist. Buck 1.3.3					
		λ_d	0.2168	-	
		Limit	0.673	-	
		Mnd	41.712	k-in	
Nominal Moment					
		Mn	37.9293	k-in	

Figure A18: 18 Gage Positive DSM Example Calculation.

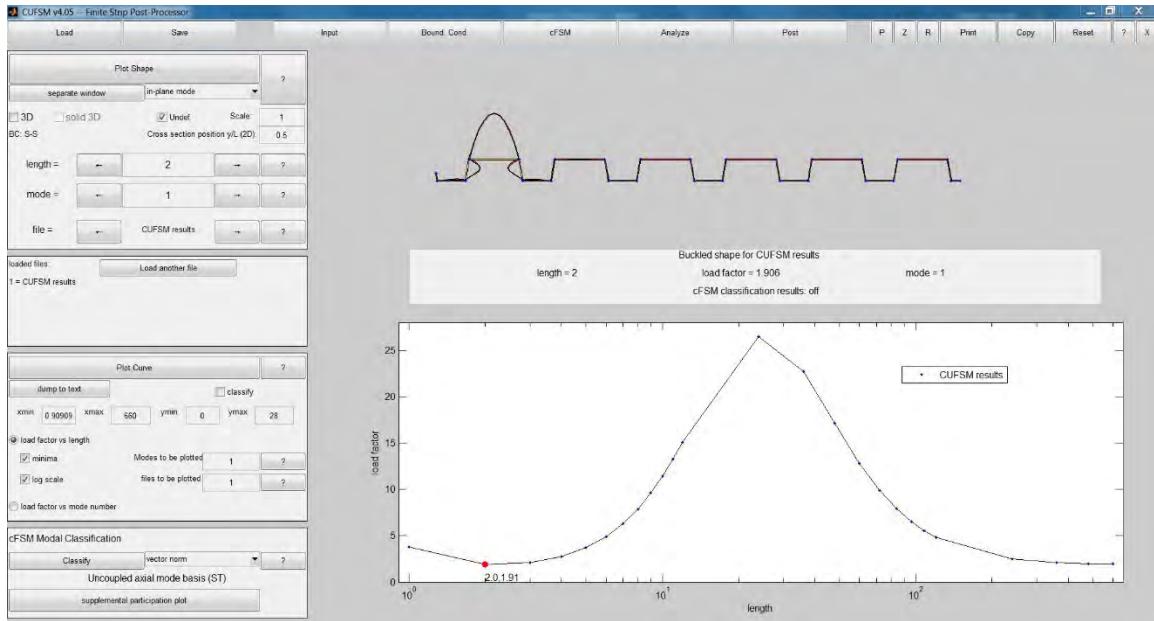


Figure A19: 16 Gage Positive DSM Output.

Section Prop.		Sn used	0.41	My	
Sn	1.23 in ³	Snp	0.41	Positive	54.981
Fy	44.7 ksi	Snn	0.41	Negative	54.981
My	54.981 k-in	Fy flute	44.9		
		Fy flange	44.5		
		Local			
		Mcrl/My	1.91	-	
		Mcrl	105.014	k-in	
		Distortional			
		Mcrd/My	26.464	-	
		Mcrd	1455.02	k-in	
		LTB			
		Mcrlt/My	26.464	-	
		Mcrlt	1455.02	k-in	
		Mne			
		Mne	54.981	k-in	
		Local Buck. 1.3.2			
		λ1	0.72357	-	
		Limit	0.776	-	
		Mnl	54.981	k-in	
		Dist. Buck 1.3.3			
		λd	0.19439	-	
		Limit	0.673	-	
		Mnd	54.981	k-in	
		Nominal Moment			
		Mn	54.981	k-in	

Figure A20: 16 Gage Positive DSM Example Calculation.

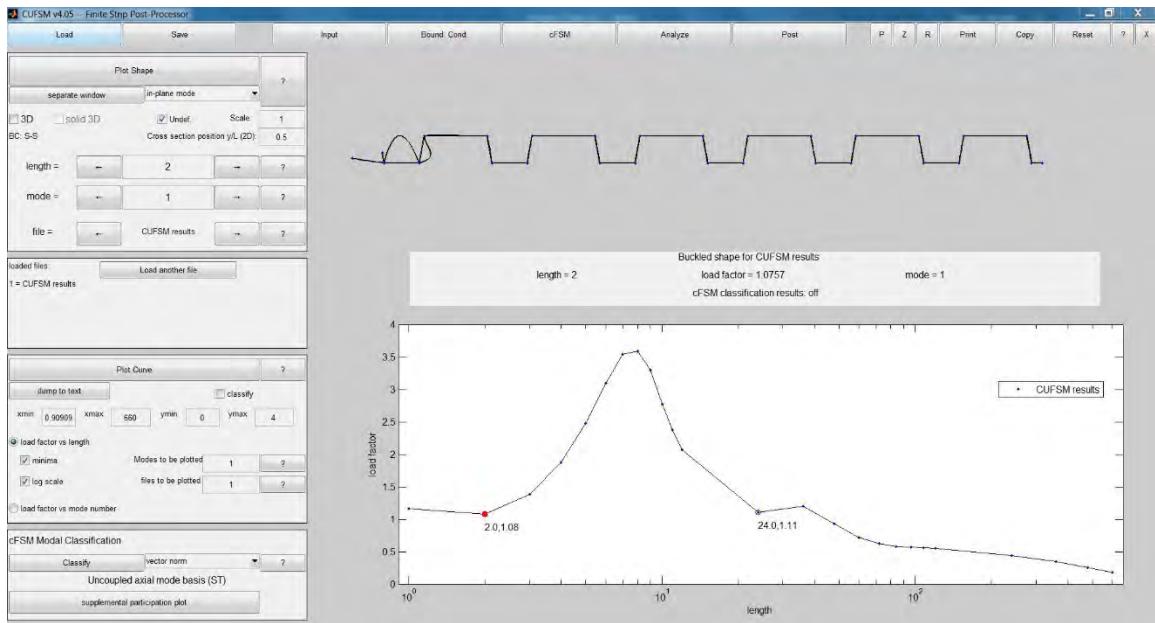


Figure A21: 22 Gage Negative DSM Output.

Section Prop.		Sn used	0.19	My	
Sn	0.57	in^3		Snp	0.19
Fy	44.5	ksi		Snn	0.19
My	25.365	k-in		Fy flute	47.1
				Fy flange	41.9
Local					
Mcrl/My	1.08	-		Mcrl	27.3942 k-in
Distortional					
Mcrd/My	1.11	-		Mcrd	28.1552 k-in
LTB					
Mcrlt/My	10	-		Mcrlt	253.65 k-in
Mne					
Mne	25.365	k-in			
Local Buck. 1.3.2					
λ1	0.96225	-		Limit	0.776 -
Mnl	22.1116	k-in			
Dist. Buck 1.3.3					
λd	0.94916	-		Mnd	20.5296 k-in
Nominal Moment					
Mn	20.5296	k-in			

Figure A22: 22 Gage Negative DSM Example Calculation.

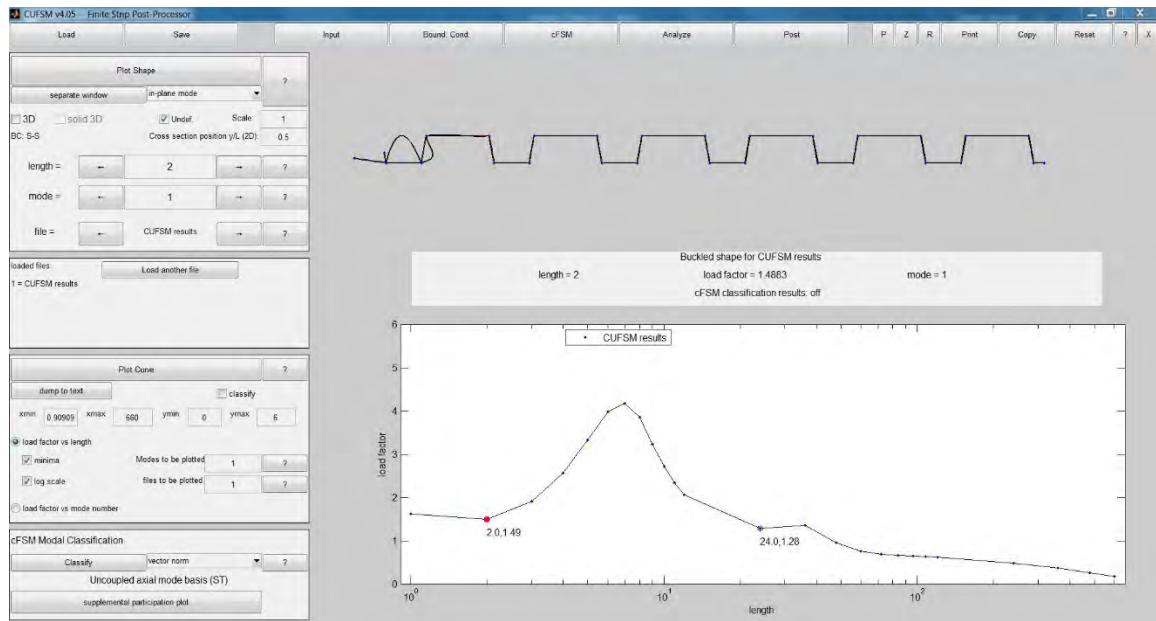


Figure A23: 20 Gage Negative DSM Output.

Section Prop.		Sn used	0.24	My	
Sn	0.72 in^3	Snp	0.23	Positive	32.6025
Fy	47.25 ksi	Snn	0.24	Negative	34.02
My	34.02 k-in	Fy flute	48.6		
		Fy flange	45.9		
		Local			
		Mcrl/My	1.49	-	
		Mcrl	50.6898	k-in	
		Distortional			
		Mcrd/My	1.28	-	
		Mcrd	43.5456	k-in	
		LTB			
		Mcrlt/My	10	-	
		Mcrlt	340.2	k-in	
		Mne			
		Mne	34.02	k-in	
		Local Buck. 1.3.2			
		λ_1	0.81923	-	
		Limit	0.776	-	
		Mnl	32.8827	k-in	
		Dist. Buck 1.3.3			
		λ_d	0.88388	-	
		Limit	0.673	-	
		Mnd	28.9092	k-in	
		Nominal Moment			
		Mn	28.9092	k-in	

Figure A24: 20 Gage Negative DSM Example Calculation.

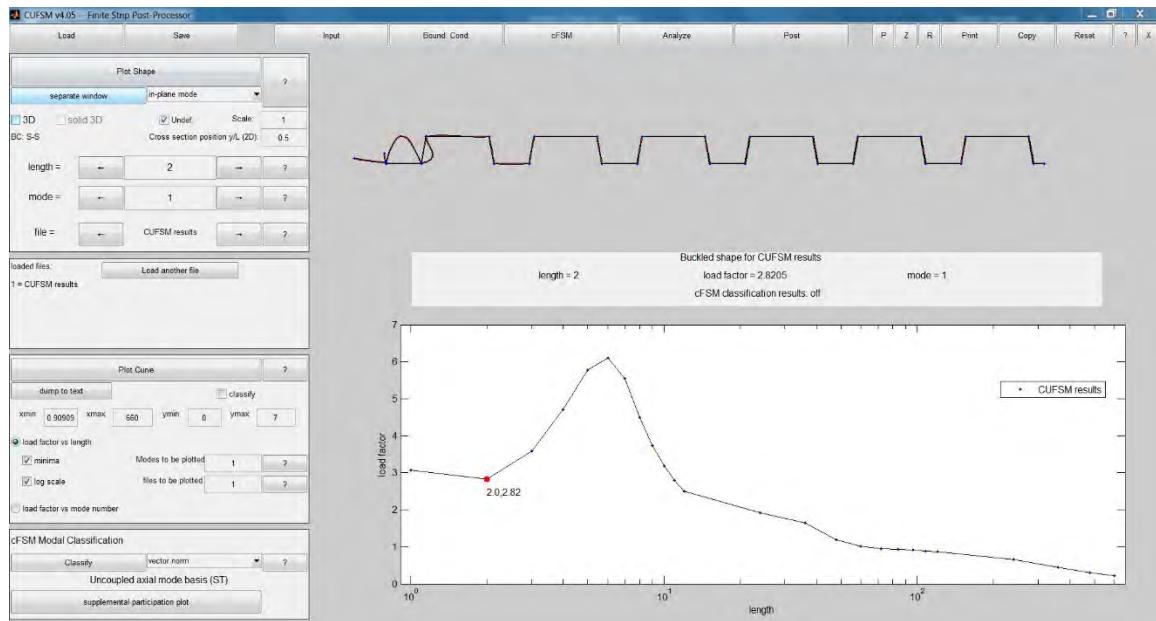


Figure A25: 18 Gage Negative DSM Output.

Section Prop.		Sn used	0.32	My	
Sn	0.96 in ³	Snp	0.32	Positive	41.712
Fy	43.45 ksi	Snn	0.32	Negative	41.712
My	41.712 k-in	Fy flute	42.6		
		Fy flange	44.3		
		Local			
		Mcrl/My	2.82	-	
		Mcrl	117.628	k-in	
		Distortional			
		Mcrd/My	1.9266	-	
		Mcrd	80.3623	k-in	
		LTB			
		Mcrlt/My	10	-	
		Mcrlt	417.12	k-in	
		Mne			
		Mne	41.712	k-in	
		Local Buck. 1.3.2			
		λ1	0.59549	-	
		Limit	0.776	-	
		Mnl	41.712	k-in	
		Dist. Buck 1.3.3			
		λd	0.72045	-	
		Limit	0.673	-	
		Mnd	40.2174	k-in	
		Nominal Moment			
		Mn	40.2174	k-in	

Figure A26: 18 Gage Negative DSM Example Calculation.

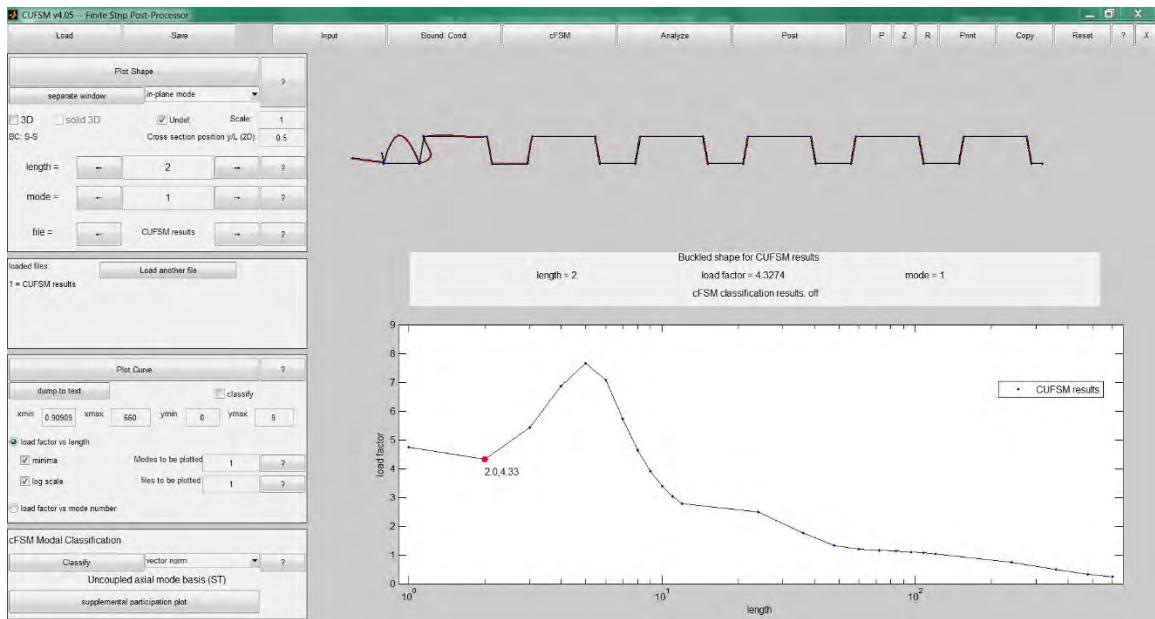


Figure A27: 16 Gage Negative DSM Output.

Section Prop.		Sn used	0.41	My	
Sn	1.23 in^3	Snp	0.41	Positive	54.981
Fy	44.7 ksi	Snn	0.41	Negative	54.981
My	54.981 k-in	Fy flute	44.9		
		Fy flange	44.5		
Local					
		Mcrl/My	4.33	-	
		Mcrl	238.068	k-in	
Distortional					
		Mcrd/My	2.4852	-	
		Mcrd	136.639	k-in	
LTB					
		Mcrlt/My	10	-	
		Mcrlt	549.81	k-in	
Mne					
		Mne	54.981	k-in	
Local Buck. 1.3.2					
		λ_1	0.48057	-	
		Limit	0.776	-	
		Mnl	54.981	k-in	
Dist. Buck 1.3.3					
		λ_d	0.63434	-	
		Limit	0.673	-	
		Mnd	54.981	k-in	
Nominal Moment					
		Mn	54.981	k-in	

Figure A28: 16 Gage Negative DSM Example Calculation.

Appendix B: Initial Project Synthesis Documents

I have attached a spreadsheet that shows 16 tests. Perhaps we could delete the 20 and 18 gage and only test the limits at 22 and 16 gage, and do multiple tests. I am suggesting also testing floor deck in order to capture the effect of flange stiffeners ... adding flange stiffeners back to WR roof deck may be a possibility, but FM would have to be brought on board.

The tested strength would have to be compared to the predicted strength by Direct Strength and Effective Width at the actual Fy of the deck that is tested. You could get the mill test reports on the coils used, but it would be good to pull standard ASTM coupons to verify.

Let me know what you think. As soon as the SDI sees the proposal, we can get a check over to MSOE. We would need to know how to make the check out, etc.

MSOE Testing

For the testing, the Excel Spreadsheet shows the following:

1. 1.5WR
roof deck in 22, 20, 18, 16 gage, which is the range of deck thickness that are used. WR deck produced currently does not have a flange stiffener. In the past, WR deck did have a flange stiffener, however around 25-30 years ago, at the insistence of Factory Mutual, the industry removed the flange stiffener because it was felt that the stiffener created a "channel" that held the asphalt that was used to adhere the insulation boards to the deck, and weakened the bond. Currently, insulation board is attached with screws, so potentially the flange stiffener could be reintroduced.
2. 2C and 3C composite floor deck, which does have a flange stiffener; 22, 20, 18, and 16 gage. These tests would show if the presence of the flange stiffener does increase deck flexural strength to the extend that the DSM method predicts.
3. The table shows deck with a nominal yield of 50 ksi. This is pretty common for the deck that is currently produced, so it was used in the table to get a feel for what loads would be required.
4. The testing would be done with a single 36 inch wide deck panel, in 4 point loading. The spreadsheet is showing a 6 foot span and 18 inches between the center load points. The load could be applied as a single load, with a spreader bar.

$$M = P(L-S)/4$$

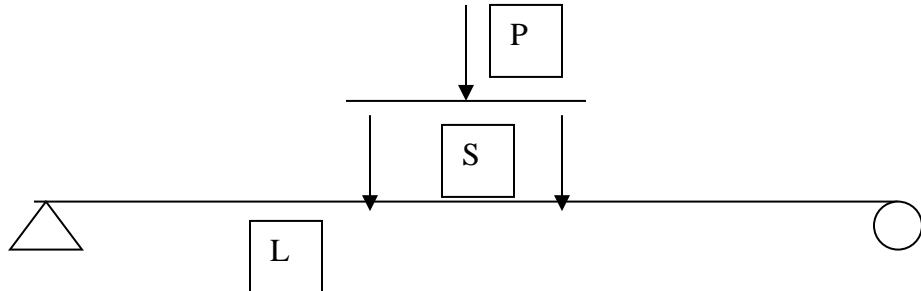


Figure B1: Proposed Testing Diagram.

Appendix C: Material Sources and Testing Documents



Test Report (Page 1 of 1)

MAI Report No:	217-1-177	Date:	March 23, 2017
Client:	Milwaukee School of Engineering	Contact:	Dr. Christopher Rabel
P.O. No:	Verbal	Date Rec'd.:	March 8, 2017
Description:	16, 18, 20, and 22 gage Corrugated Steel Sheets	Actual Material:	See Notes
Specified Material:	ASTM A1008		

Tensile Properties

Property	16 gage		18 gage		ASTM A1008, SS Grade 40
	Flange	Flute	Flange	Flute	
Test Bar Dimensions					
Width, inch	0.511	0.512	0.510	0.508	0.500
Thickness, inch	0.060	0.060	0.050	0.048	Mat'l Thickness
Gage Length, inches	2.0	2.0	2.0	2.0	2.0
Tensile Strength, psi	51,500	57,500	52,000	52,500	52,000 min.
Yield Strength, psi (1)	44,500	44,900	44,300	42,600	40,000 min.
Elongation, %	27	29	27	29	20 min.

Property	20 gage		22 gage		ASTM A1008, SS Grade 40
	Flange	Flute	Flange	Flute	
Test Bar Dimensions					
Width, inch	0.507	0.517	0.513	0.507	0.500
Thickness, inch	0.038	0.036	0.034	0.030	Mat'l Thickness
Gage Length, inches	2.0	2.0	2.0	2.0	2.0
Tensile Strength, psi	52,000	56,500	53,000	61,000	52,000 min.
Yield Strength, psi (1)	45,900	48,600	41,900	47,100	40,000 min.
Elongation, %	29	29	29	26	20 min.

(1): At 0.2% offset.

Notes: Standard flat tensile bars were machined from each of the submitted corrugated sheets. The tensile properties of all eight samples are in conformance with structural steel (SS) Grade 40 as included in ASTM A1008, "Standard Specification for Steel, Sheet, Cold-Rolled, Carbon, Structural, High-Strength Low-Alloy and High-Strength Low-Alloy with Improved Formability."

Respectfully submitted,

Thomas C. Tefelske
President

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Figure C1: Material Testing Summary.

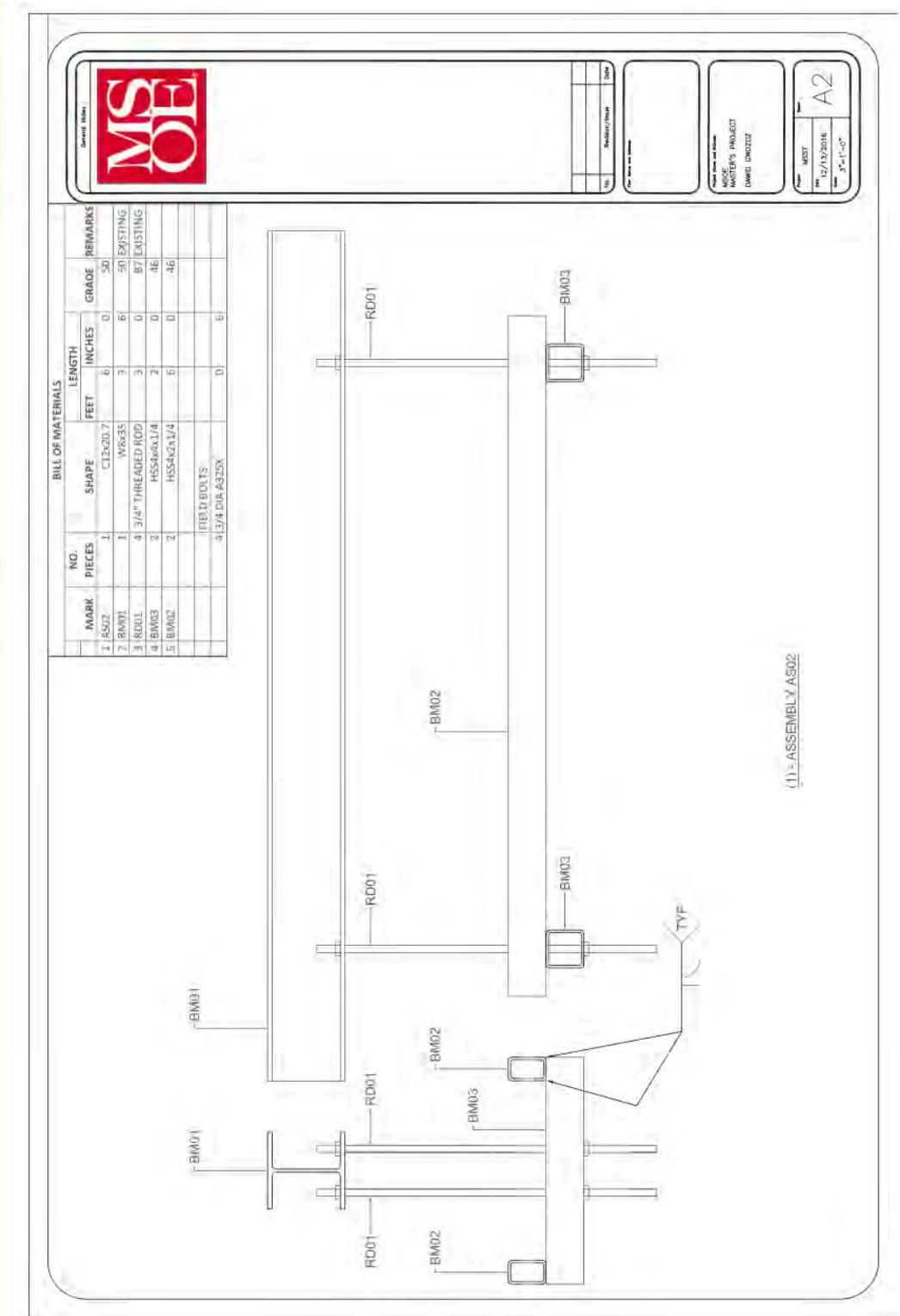


Figure C2: Test Frame Assembly Shop Drawing.

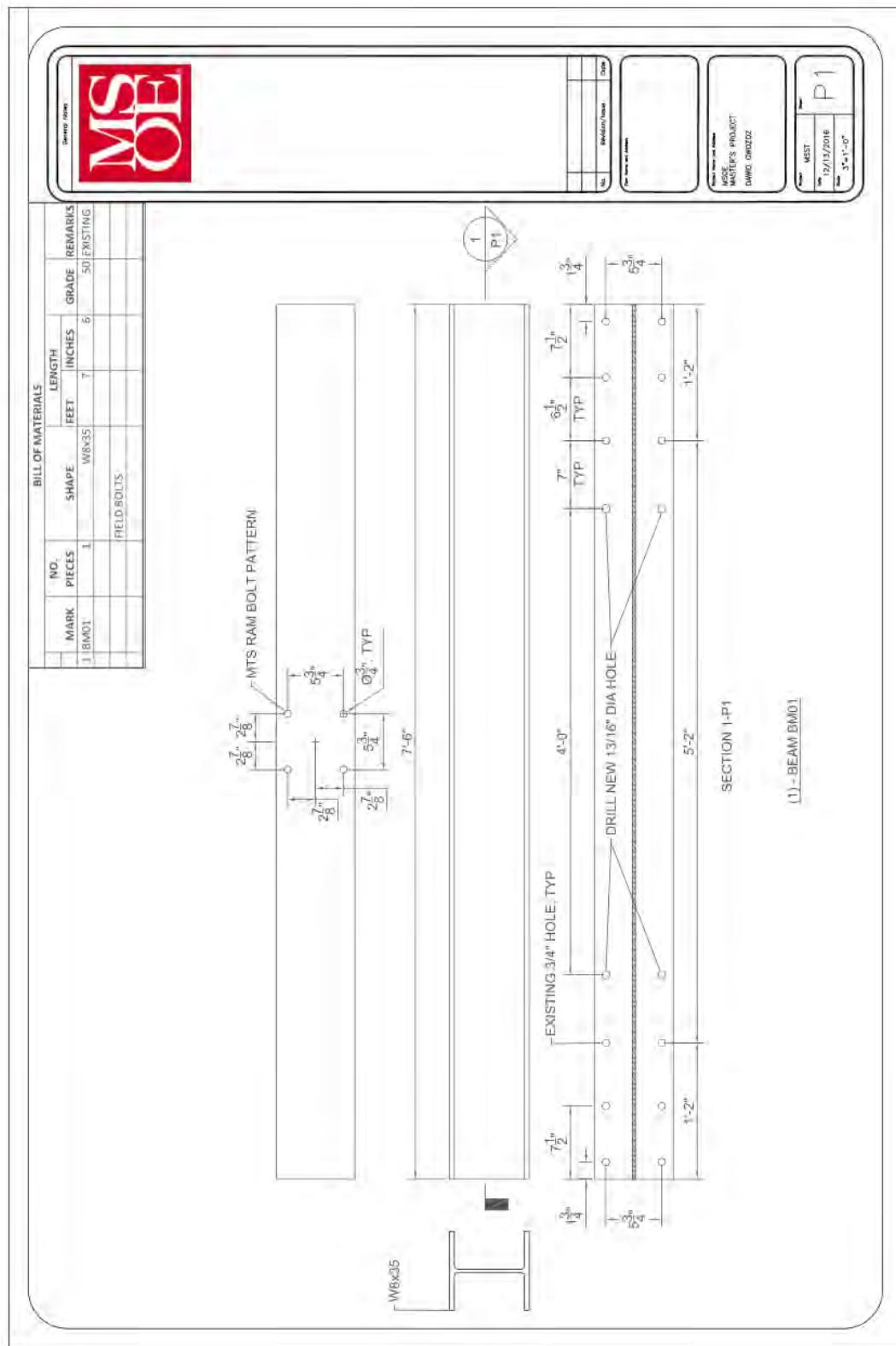


Figure C3: Cross Beam Shop Drawing.

BILL OF MATERIALS					
	NO.	PIECES	SHAPE	LENGTH FEET	INCHES
1	MARK	4	3/4" THREADED ROD	3	0
			FIELD BOLTS		
			8 3/4 DIA NUTS		

3 1/2"

$\odot \frac{3}{4}$

(4) ROD RD01

DESIGNER	REVISER	DATE
DAVID O. CHEN		
MASTER'S PROJECT		
DAVID O. CHEN		
MEST	P2	
12/13/2016		
8" - 1" - 1"		

Figure C4: Threaded Rod Shop Drawing.

Figure C5: Line Load HSS Shop Drawing.

					
DRAWN BY _____ CHECKED BY _____ APPROVED BY _____ DATE _____					
SHEET NO. _____ OF _____ PAGE NO. _____ OF _____ DRAWING NO. _____ DATE _____					
BILL OF MATERIALS NO. MARK NO. OF PIECES SHAPE LENGTH INCHES FEET INCHES 1 BIV03 2 HSS Schedule 1/4 2 0 FIELD BOATS					
GRADE 45 REMARKS					
1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20 21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 45 46 47 48 49 50 51 52 53 54 55 56 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 84 85 86 87 88 89 90 91 92 93 94 95 96 97 98 99 100 101 102 103 104 105 106 107 108 109 110 111 112 113 114 115 116 117 118 119 120 121 122 123 124 125 126 127 128 129 130 131 132 133 134 135 136 137 138 139 140 141 142 143 144 145 146 147 148 149 150 151 152 153 154 155 156 157 158 159 160 161 162 163 164 165 166 167 168 169 170 171 172 173 174 175 176 177 178 179 180 181 182 183 184 185 186 187 188 189 190 191 192 193 194 195 196 197 198 199 200 201 202 203 204 205 206 207 208 209 210 211 212 213 214 215 216 217 218 219 220 221 222 223 224 225 226 227 228 229 230 231 232 233 234 235 236 237 238 239 240 241 242 243 244 245 246 247 248 249 250 251 252 253 254 255 256 257 258 259 260 261 262 263 264 265 266 267 268 269 270 271 272 273 274 275 276 277 278 279 280 281 282 283 284 285 286 287 288 289 290 291 292 293 294 295 296 297 298 299 300 301 302 303 304 305 306 307 308 309 310 311 312 313 314 315 316 317 318 319 320 321 322 323 324 325 326 327 328 329 330 331 332 333 334 335 336 337 338 339 340 341 342 343 344 345 346 347 348 349 350 351 352 353 354 355 356 357 358 359 360 361 362 363 364 365 366 367 368 369 370 371 372 373 374 375 376 377 378 379 380 381 382 383 384 385 386 387 388 389 390 391 392 393 394 395 396 397 398 399 400 401 402 403 404 405 406 407 408 409 410 411 412 413 414 415 416 417 418 419 420 421 422 423 424 425 426 427 428 429 430 431 432 433 434 435 436 437 438 439 440 441 442 443 444 445 446 447 448 449 450 451 452 453 454 455 456 457 458 459 460 461 462 463 464 465 466 467 468 469 470 471 472 473 474 475 476 477 478 479 480 481 482 483 484 485 486 487 488 489 490 491 492 493 494 495 496 497 498 499 500 501 502 503 504 505 506 507 508 509 510 511 512 513 514 515 516 517 518 519 520 521 522 523 524 525 526 527 528 529 530 531 532 533 534 535 536 537 538 539 540 541 542 543 544 545 546 547 548 549 550 551 552 553 554 555 556 557 558 559 550 551 552 553 554 555 556 557 558 559 560 561 562 563 564 565 566 567 568 569 570 571 572 573 574 575 576 577 578 579 580 581 582 583 584 585 586 587 588 589 580 581 582 583 584 585 586 587 588 589 590 591 592 593 594 595 596 597 598 599 590 591 592 593 594 595 596 597 598 599 600 601 602 603 604 605 606 607 608 609 600 601 602 603 604 605 606 607 608 609 610 611 612 613 614 615 616 617 618 619 610 611 612 613 614 615 616 617 618 619 620 621 622 623 624 625 626 627 628 629 620 621 622 623 624 625 626 627 628 629 630 631 632 633 634 635 636 637 638 639 630 631 632 633 634 635 636 637 638 639 640 641 642 643 644 645 646 647 648 649 640 641 642 643 644 645 646 647 648 649 650 651 652 653 654 655 656 657 658 659 650 651 652 653 654 655 656 657 658 659 660 661 662 663 664 665 666 667 668 669 660 661 662 663 664 665 666 667 668 669 670 671 672 673 674 675 676 677 678 679 670 671 672 673 674 675 676 677 678 679 680 681 682 683 684 685 686 687 688 689 680 681 682 683 684 685 686 687 688 689 690 691 692 693 694 695 696 697 698 699 690 691 692 693 694 695 696 697 698 699 700 701 702 703 704 705 706 707 708 709 700 701 702 703 704 705 706 707 708 709 710 711 712 713 714 715 716 717 718 719 710 711 712 713 714 715 716 717 718 719 720 721 722 723 724 725 726 727 728 729 720 721 722 723 724 725 726 727 728 729 730 731 732 733 734 735 736 737 738 739 730 731 732 733 734 735 736 737 738 739 740 741 742 743 744 745 746 747 748 749 740 741 742 743 744 745 746 747 748 749 750 751 752 753 754 755 756 757 758 759 750 751 752 753 754 755 756 757 758 759 760 761 762 763 764 765 766 767 768 769 760 761 762 763 764 765 766 767 768 769 770 771 772 773 774 775 776 777 778 779 770 771 772 773 774 775 776 777 778 779 780 781 782 783 784 785 786 787 788 789 780 781 782 783 784 785 786 787 788 789 790 791 792 793 794 795 796 797 798 799 790 791 792 793 794 795 796 797 798 799 800 801 802 803 804 805 806 807 808 809 800 801 802 803 804 805 806 807 808 809 810 811 812 813 814 815 816 817 818 819 810 811 812 813 814 815 816 817 818 819 820 821 822 823 824 825 826 827 828 829 820 821 822 823 824 825 826 827 828 829 830 831 832 833 834 835 836 837 838 839 830 831 832 833 834 835 836 837 838 839 840 841 842 843 844 845 846 847 848 849 840 841 842 843 844 845 846 847 848 849 850 851 852 853 854 855 856 857 858 859 850 851 852 853 854 855 856 857 858 859 860 861 862 863 864 865 866 867 868 869 860 861 862 863 864 865 866 867 868 869 870 871 872 873 874 875 876 877 878 879 870 871 872 873 874 875 876 877 878 879 880 881 882 883 884 885 886 887 888 889 880 881 882 883 884 885 886 887 888 889 890 891 892 893 894 895 896 897 898 899 890 891 892 893 894 895 896 897 898 899 900 901 902 903 904 905 906 907 908 909 900 901 902 903 904 905 906 907 908 909 910 911 912 913 914 915 916 917 918 919 910 911 912 913 914 915 916 917 918 919 920 921 922 923 924 925 926 927 928 929 920 921 922 923 924 925 926 927 928 929 930 931 932 933 934 935 936 937 938 939 930 931 932 933 934 935 936 937 938 939 940 941 942 943 944 945 946 947 948 949 940 941 942 943 944 945 946 947 948 949 950 951 952 953 954 955 956 957 958 959 950 951 952 953 954 955 956 957 958 959 960 961 962 963 964 965 966 967 968 969 960 961 962 963 964 965 966 967 968 969 970 971 972 973 974 975 976 977 978 979 970 971 972 973 974 975 976 977 978 979 980 981 982 983 984 985 986 987 988 989 980 981 982 983 984 985 986 987 988 989 990 991 992 993 994 995 996 997 998 999 990 991 992 993 994 995 996 997 998 999 1000 1001 1002 1003 1004 1005 1006 1007 1008 1009 1000 1001 1002 1003 1004 1005 1006 1007 1008 1009 1010 1011 1012 1013 1014 1015 1016 1017 1018 1019 1010 1011 1012 1013 1014 1015 1016 1017 1018 1019 1020 1021 1022 1023 1024 1025 1026 1027 1028 1029 1020 1021 1022 1023 1024 1025 1026 1027 1028 1029 1030 1031 1032 1033 1034 1035 1036 1037 1038 1039 1030 1031 1032 1033 1034 1035 1036 1037 1038 1039 1040 1041 1042 1043 1044 1045 1046 1047 1048 1049 1040 1041 1042 1043 1044 1045 1046 1047 1048 1049 1050 1051 1052 1053 1054 1055 1056 1057 1058 1059 1050 1051 1052 1053 1054 1055 1056 1057 1058 1059 1060 1061 1062 1063 1064 1065 1066 1067 1068 1069 1060 1061 1062 1063 1064 1065 1066 1067 1068 1069 1070 1071 1072 1073 1074 1075 1076 1077 1078 1079 1070 1071 1072 1073 1074 1075 1076 1077 1078 1079 1080 1081 1082 1083 1084 1085 1086 1087 1088 1089 1080 1081 1082 1083 1084 1085 1086 1087 1088 1089 1090 1091 1092 1093 1094 1095 1096 1097 1098 1099 1090 1091 1092 1093 1094 1095 1096 1097 1098 1099 1100 1101 1102 1103 1104 1105 1106 1107 1108 1109 1100 1101 1102 1103 1104 1105 1106 1107 1108 1109 1110 1111 1112 1113 1114 1115 1116 1117 1118 1119 1110 1111 1112 1113 1114 1115 1116 1117 1118 1119 1120 1121 1122 1123 1124 1125 1126 1127 1128 1129 1120 1121 1122 1123 1124 1125 1126 1127 1128 1129 1130 1131 1132 1133 1134 1135					

Figure C6: Girder HSS Shop Drawing.

Data Base - Type B, F, N, J


ATTRIBUTE		TYPE B DECK (B, BI, BA, BIA)			
Note	Gage	22	20	18	16
	Thickness	.0295	.0358	.0474	.0598
	Weight, psf	1.6	1.9	2.6	3.3
1	I_p , in. ⁴	0.16	0.20	0.29	0.38
1	I_n , in. ⁴	0.18	0.23	0.30	0.38
1	S_p , in. ³	0.19	0.23	0.32	0.41
1	S_n , in. ³	0.19	0.24	0.32	0.41
2	Ext.R, lbs.	710	1010	1680	2560
3	Ext.R, lbs.	820	1160	1920	2910
4	Int.R, lbs.	1130	1640	2780	4300
5	Int.R, lbs.	1130	1640	2780	4300
6	V, lbs.	1860	2250	2960	3700
7	Max.1 span	5'9"	6'5"	7'9"	8'10"
8	Max.2 span	6'9"	7'6"	9'1"	10'5"
9	Max. Cant.	1'8"	1'10"	2'2"	2'8"
10	FM span	6'0"	6'6"	7'5"	9'6"
10	FM Acoustic span	5'11"	6'6"	7'5"	9'3"

Figure C7: Excerpt from CANAM Deck Table [7].



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